

Reproducible and replicable comparisons of  
methods controlling false discoveries in  
computational biology

**Patrick Kimes, PhD**  
Postdoctoral Fellow  
Dana-Farber Cancer Institute  
Harvard TH Chan School of Public Health

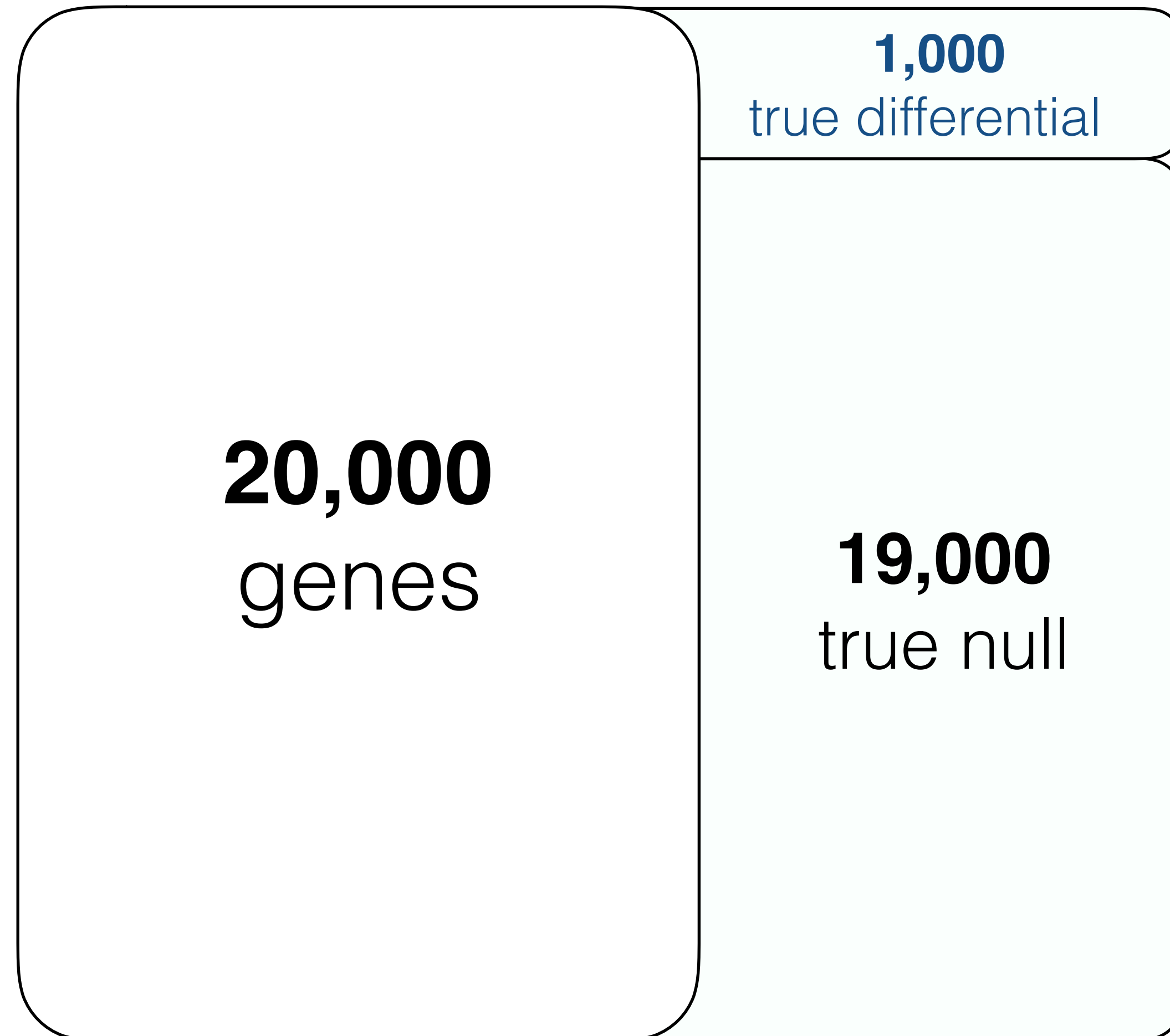
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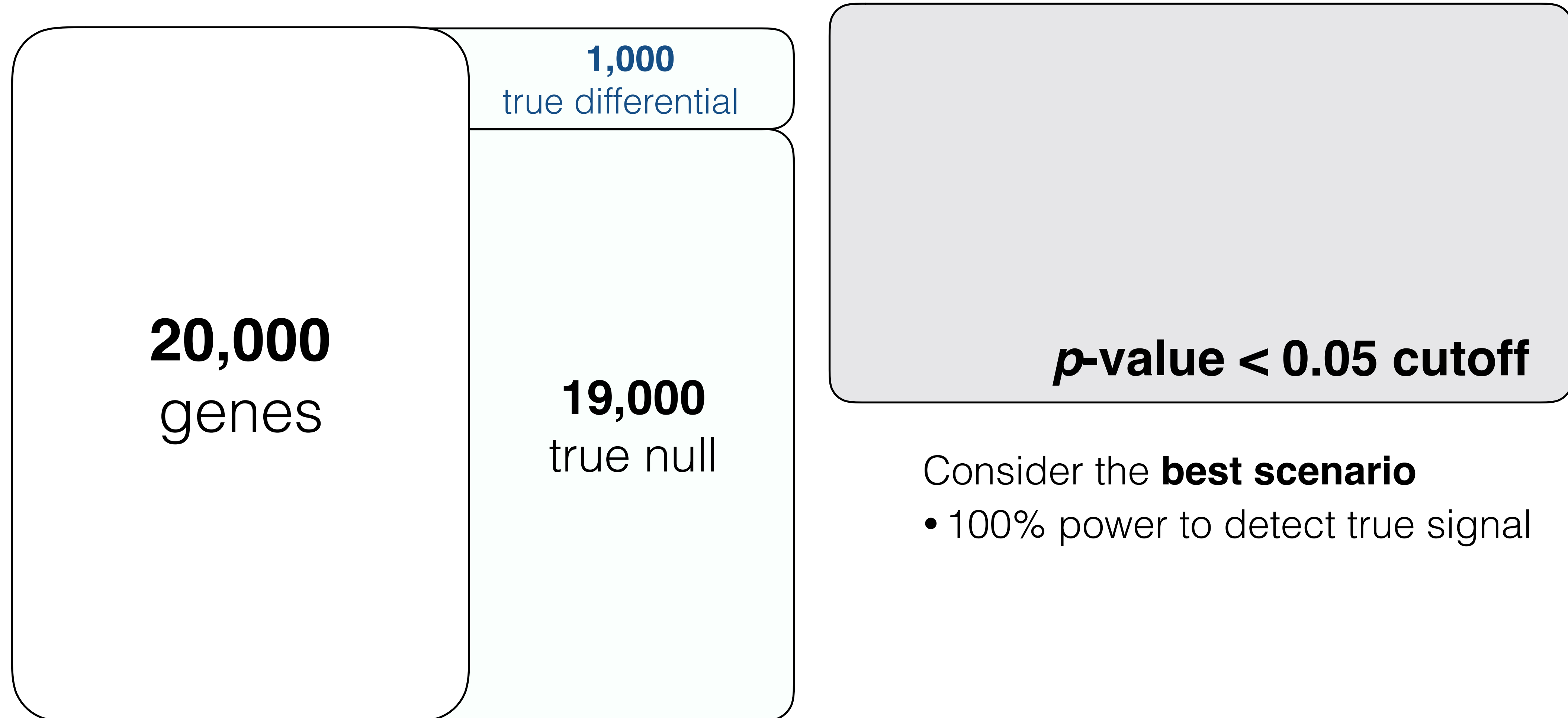
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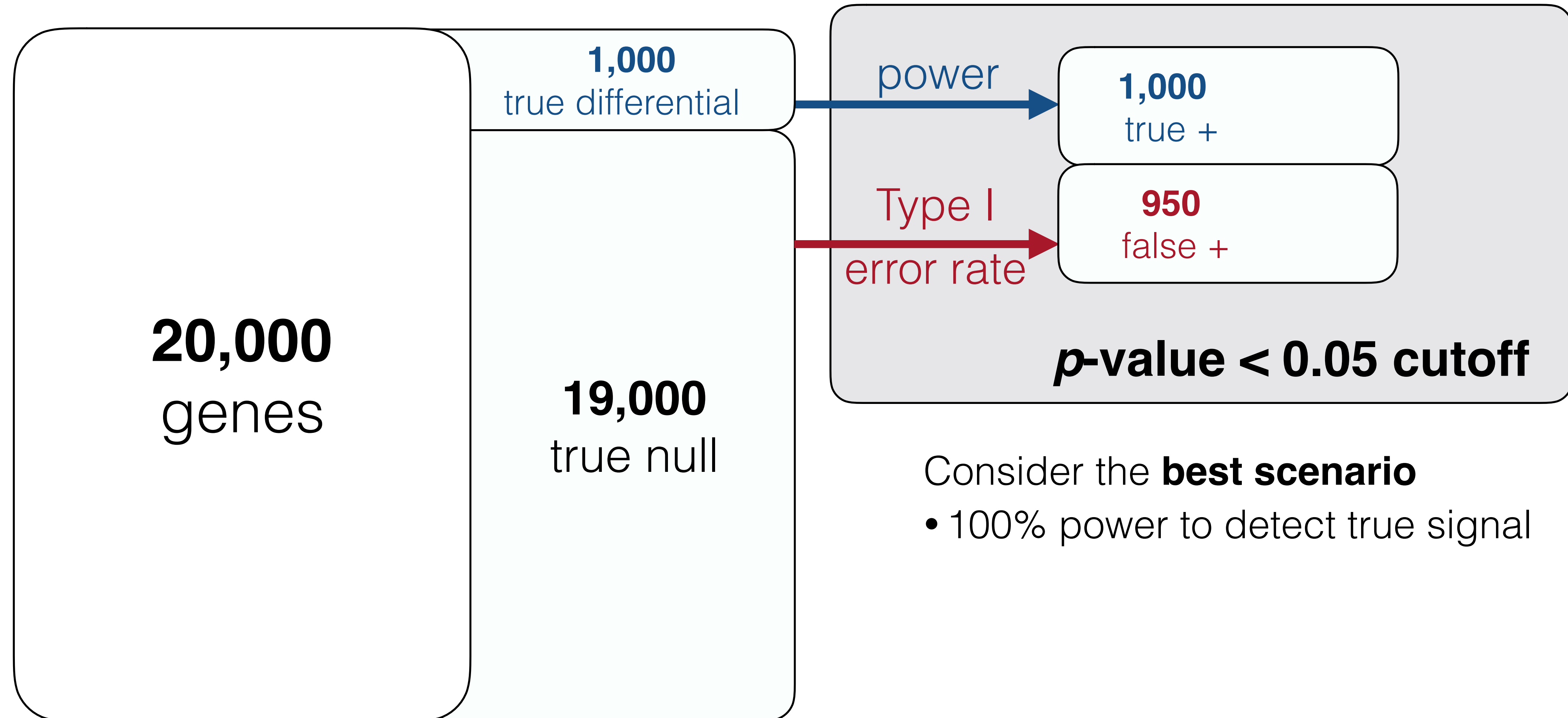
# The problem of multiple hypothesis testing



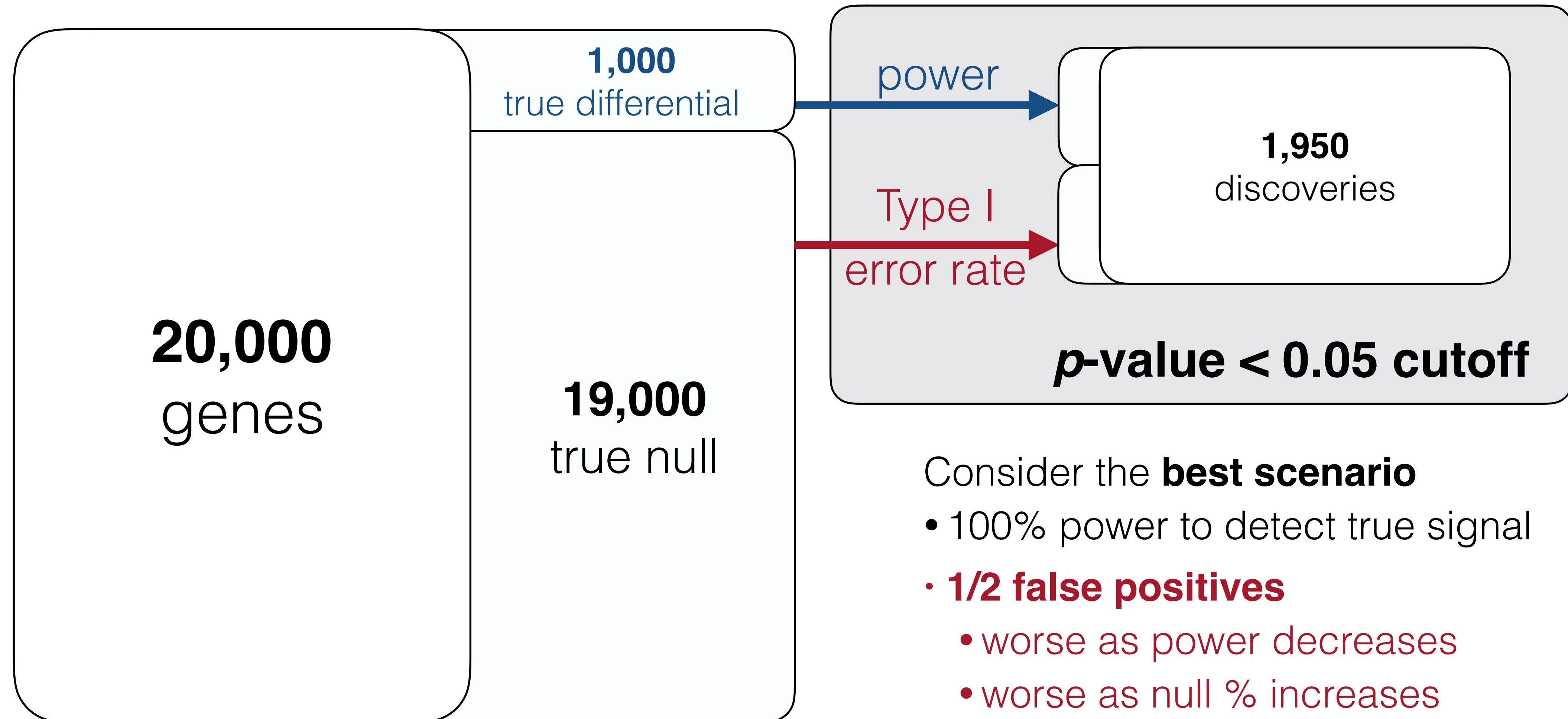
# The problem of multiple hypothesis testing



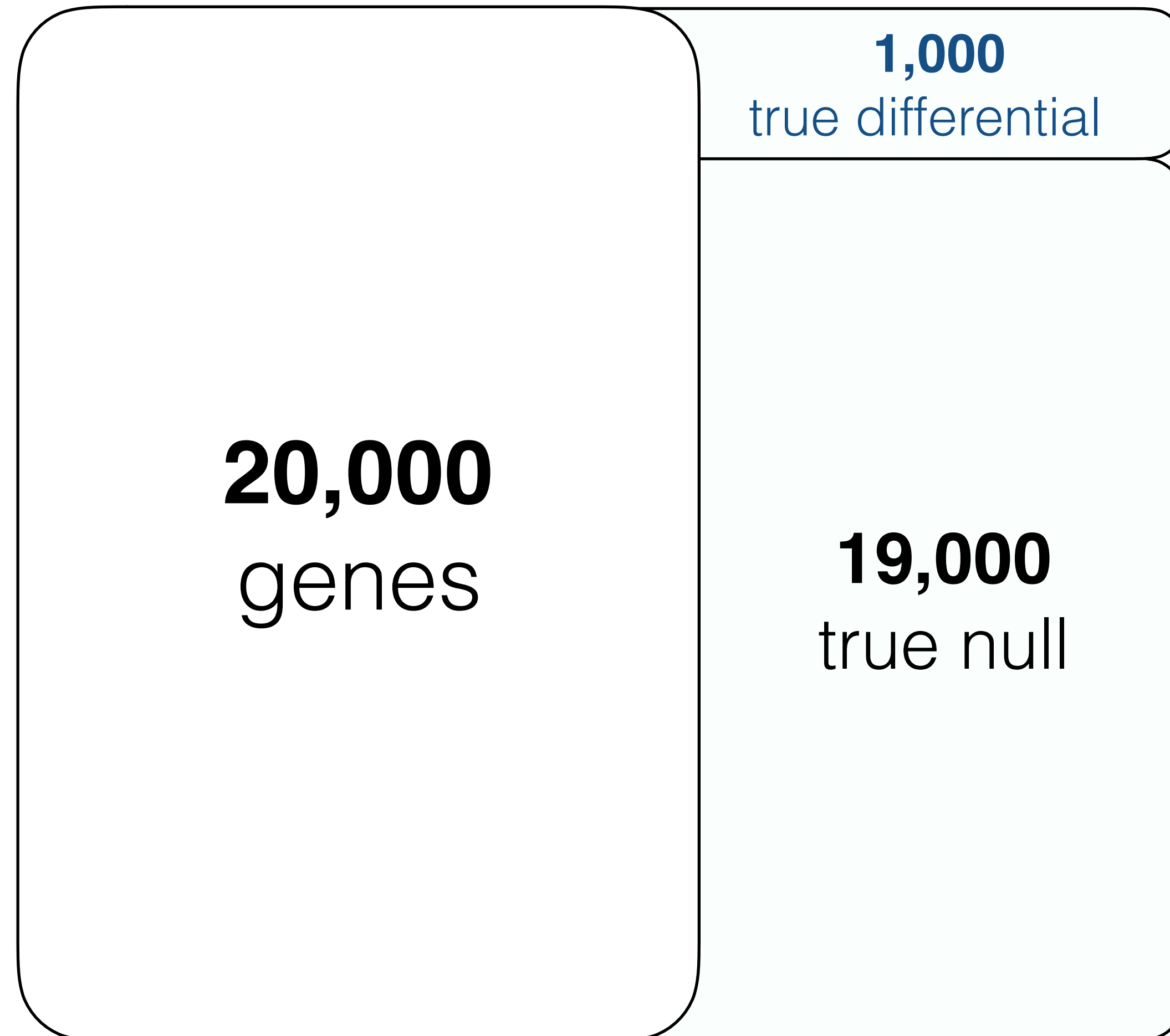
# The problem of multiple hypothesis testing



# The problem of multiple hypothesis testing



# Controlling false positives



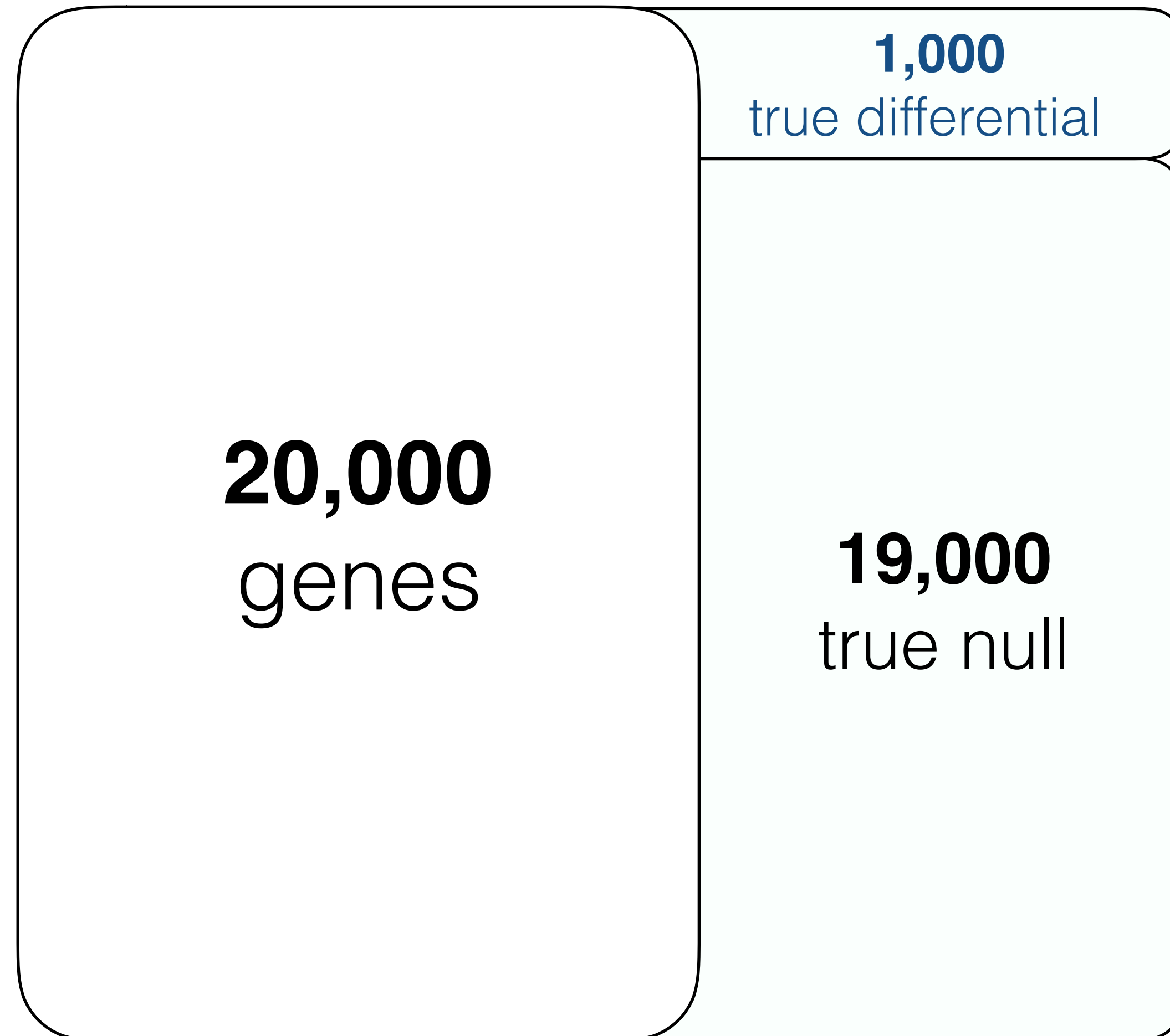
## Family-wise Error Rate (FWER)

- *Bonferroni correction*

$$P(\text{at least 1 false positive}) < \alpha$$



# Controlling false positives



## Family-wise Error Rate (FWER)

- *Bonferroni correction*

$$P(\text{at least 1 false positive}) < \alpha$$

## False Discovery Rate (FDR)

- *Benjamini-Hochberg (BH) procedure*
- *Storey's q-value*

$$E\left(\frac{\text{\# false positives}}{\text{\# total positives}}\right) < \alpha$$

# Moving beyond BH and Storey's $q$ -value

## **BH and $q$ -value**

- all tests treated equal

# Moving beyond BH and Storey's $q$ -value

## BH and $q$ -value

- all tests treated equal

## Reality

- all tests **not** equal
  - **eQTL** *cis* vs. *trans*
  - **RNA-seq** read depth

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## Covariate-aware methods

- model differences in tests via **covariates**
- recent explosion of methods

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  - **RNA-seq** read depth

## Covariate-aware methods

- model differences in tests via **covariates**
- recent explosion of methods

1995

BH procedure

2001

Storey's  $q$ -value

2009

conditional local FDR (**LFDR**)

2015

FDR regression (**FDRreg**)

2016

Independent Hypothesis Weighting (**IHW**)

2017

Adaptive Shrinkage (**ASH**)

Boca-Leek (**BL**)

2018

Adaptive  $p$ -value Thresholding (**AdaPT**)

# Understanding covariate-aware methods for FDR control

consider the two-groups model

$$p_i \sim \pi_0 f_0 + (1 - \pi_0) f_1$$

probability of test being null

distribution under **null** (uniform)

distribution under **alternative**

The diagram shows the equation  $p_i \sim \pi_0 f_0 + (1 - \pi_0) f_1$ . A red arrow points from the text 'probability of test being null' to the coefficient  $\pi_0$ . A blue arrow points from the text 'distribution under null (uniform)' to the term  $f_0$ . Another blue arrow points from the text 'distribution under alternative' to the term  $f_1$ .

# Understanding covariate-aware methods for FDR control

consider the two-groups model

**classic methods**

$$p_i \sim \pi_0 f_0 + (1 - \pi_0) f_1$$

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- Storey's  $q$ -value

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$$p_i \sim \pi_0 f_0 + (1 - \pi_0) f_1$$

- BH procedure
- Storey's  $q$ -value

## covariate-aware methods

$$p_i | x_i \sim \pi_0(x_i) f_0 + (1 - \pi_0(x_i)) f_1(x_i)$$



# Understanding covariate-aware methods for FDR control

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eQTL  
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eQTL  
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RNA-seq  
read depth

- IHW  
- BL 
- LFDR  
- AdaPT  
- FDRreg\* 
- ASH\* 

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$$p_i \sim \pi_0 f_0 + (1 - \pi_0) f_1$$

- BH procedure
- Storey's  $q$ -value

## covariate-aware methods

$$\cancel{p_i | x_i} \sim \pi_0(x_i) f_0 + (1 - \pi_0(x_i)) f_1(x_i)$$

$$z_i | x_i$$

- IHW  
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# Understanding covariate-aware methods for FDR control

consider the two-groups model

## classic methods










$$p_i \sim \pi_0 f_0 + (1 - \pi_0) f_1$$

- BH procedure
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## covariate-aware methods

$$\cancel{p_i | x_i} \sim \pi_0(x_i) f_0 + (1 - \pi_0(x_i)) f_1(x_i)$$

$$\hat{\beta}_i | \hat{s}_i$$

- IHW  
- BL 
- LFDR  
- AdaPT  
- FDRreg\* 
- ASH\* 

# Benchmarking for practical recommendations

- BH procedure
- Storey's  $q$ -value

- IHW
- BL
- AdaPT
- LFDR
- FDRreg
- ASH

## Simulated Data

- *in silico* experiments
- pure simulations

## Case Studies

- RNA-seq DE
- scRNA-seq DE
- 16S microbiome DA
- CHIP-seq DB
- GWAS
- Gene Set Analysis

# Benchmarking for practical recommendations

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**FDR control**

**Power**

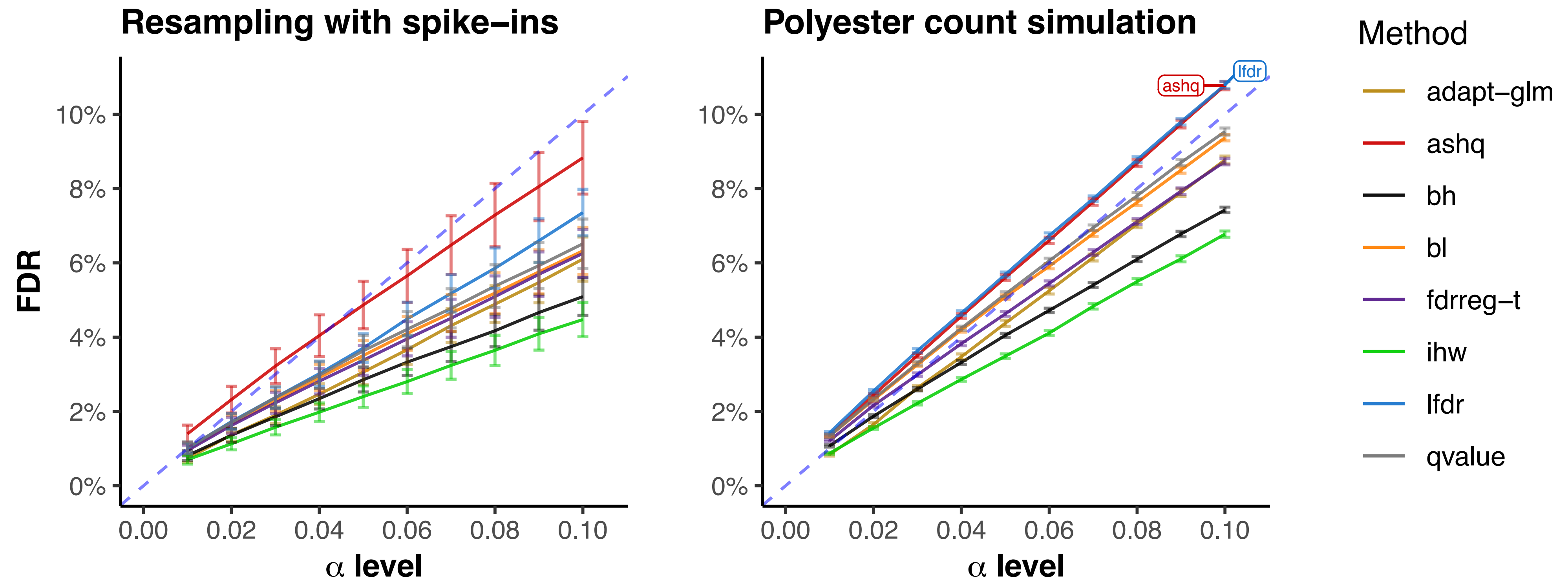
**Applicability**

**Consistency**

**Usability**

# Most covariate-aware methods control FDR

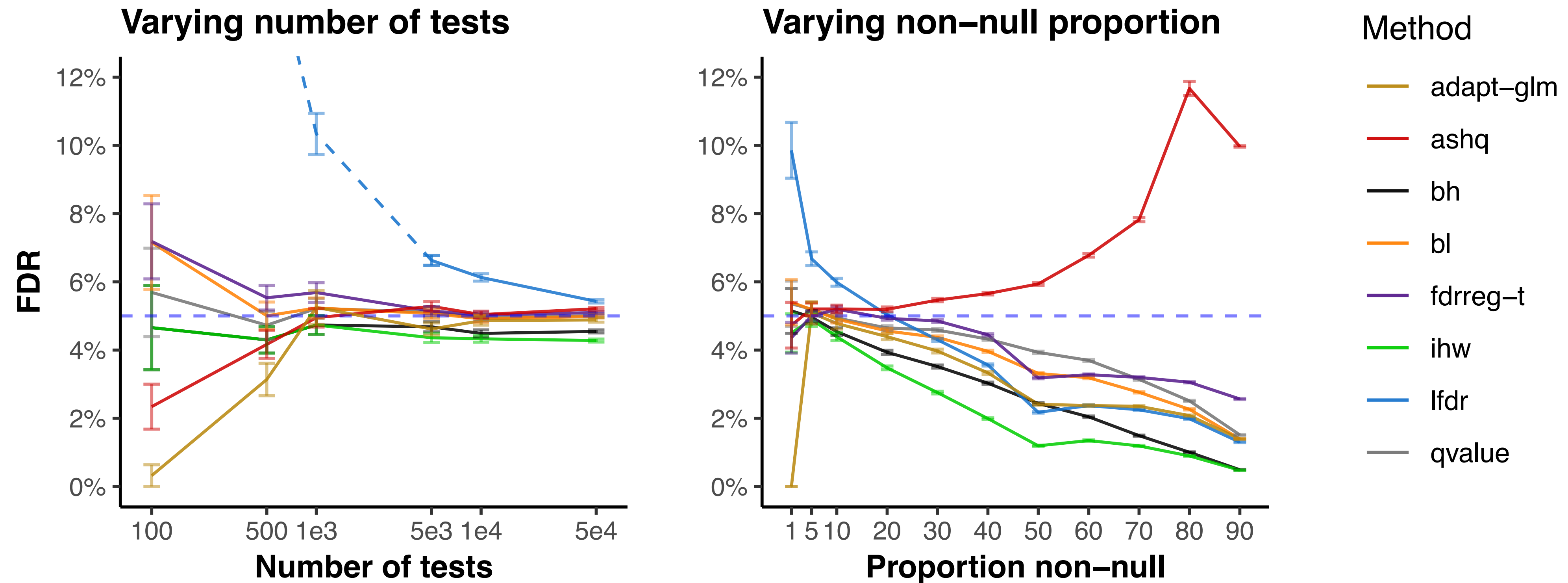
## FDR control in RNA-seq *in silico* experiments





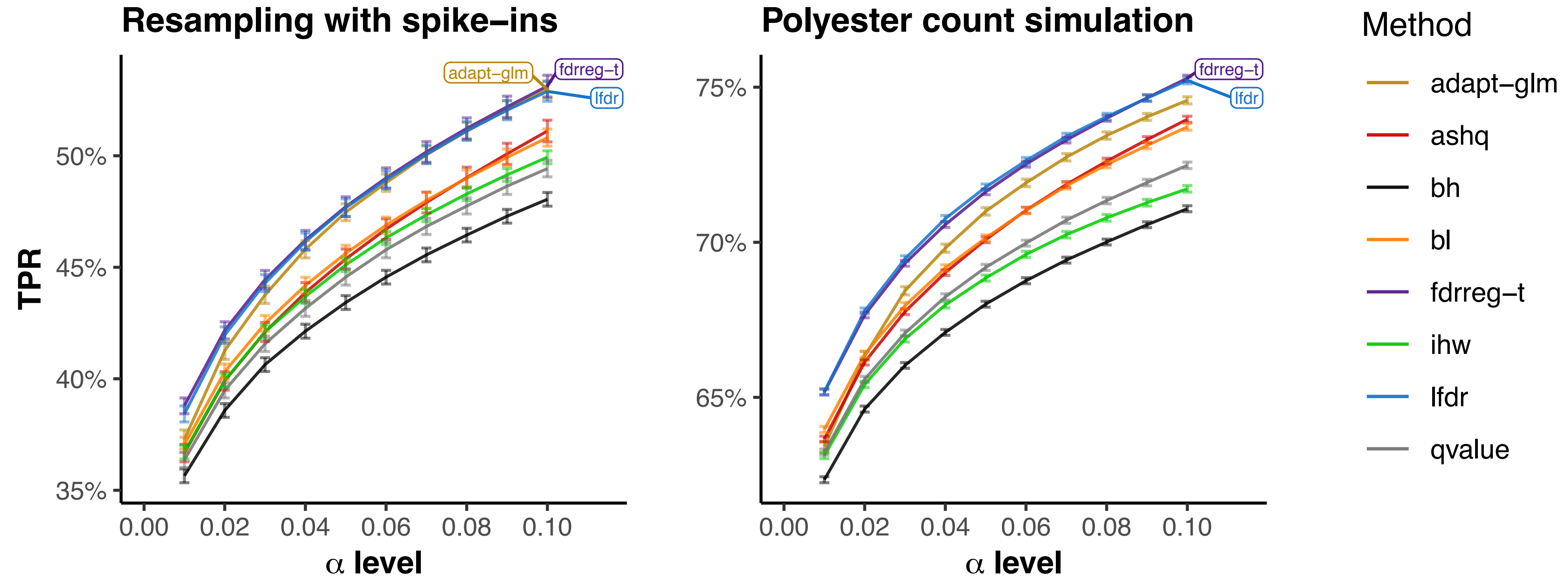
# Some methods were sensitive to number of tests, null proportion

## FDR across simulation settings ( $\alpha = 0.05$ )



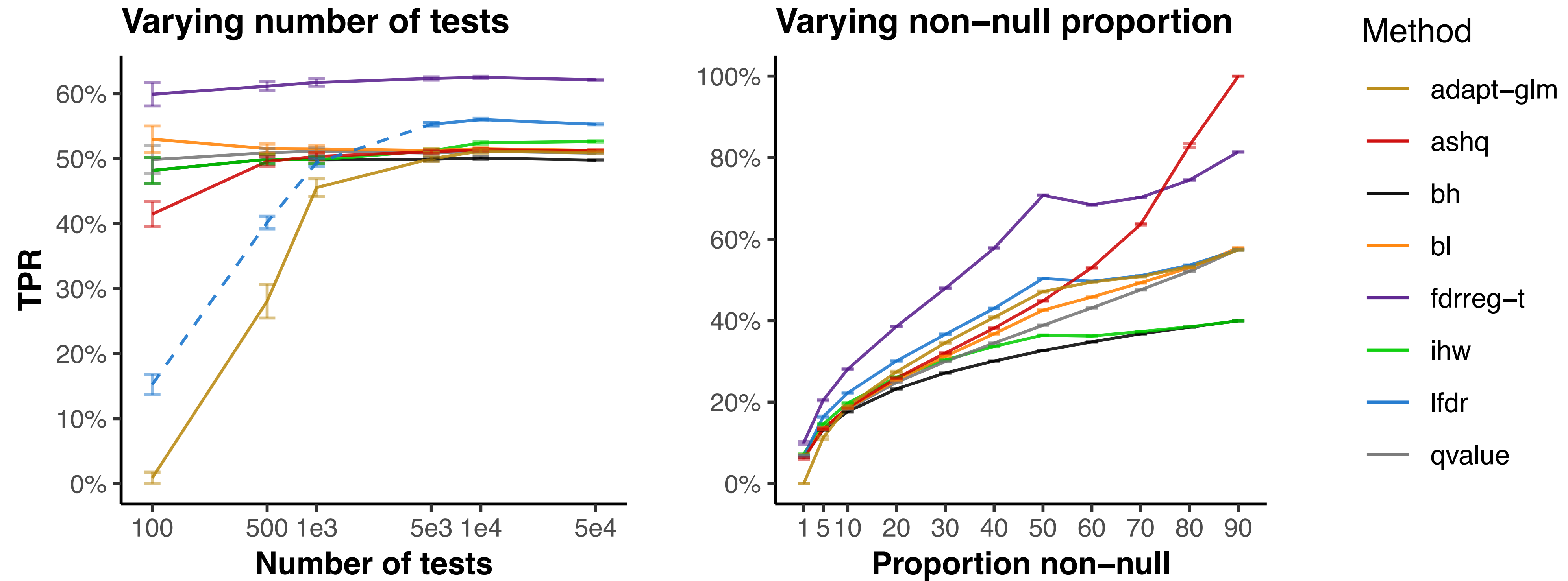
# Covariate-aware methods were modestly more powerful

## TPR in RNA-seq *in silico* experiments

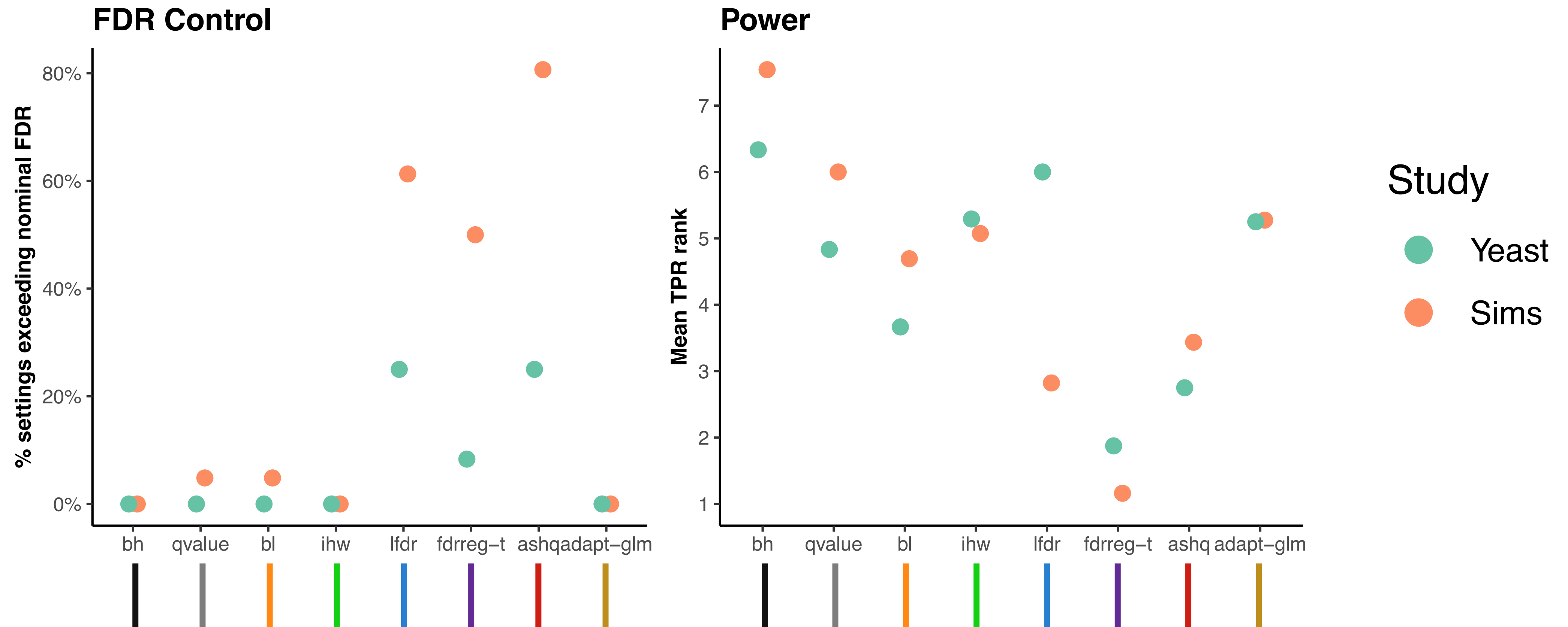


# Some methods were sensitive to number of tests, null proportion

## TPR across simulation settings ( $\alpha = 0.05$ )

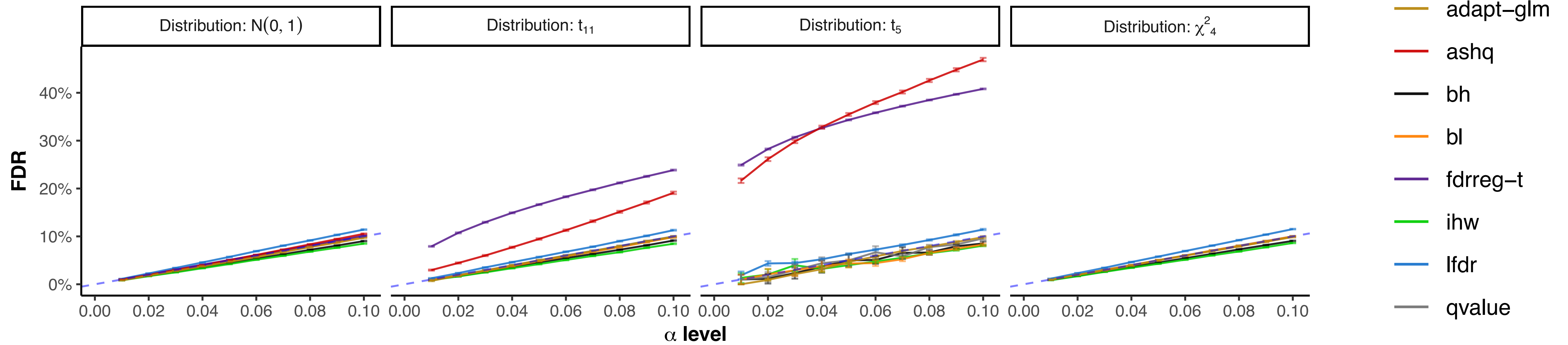


# Summarizing FDR control and power across simulations



# Some methods were sensitive to the test statistic

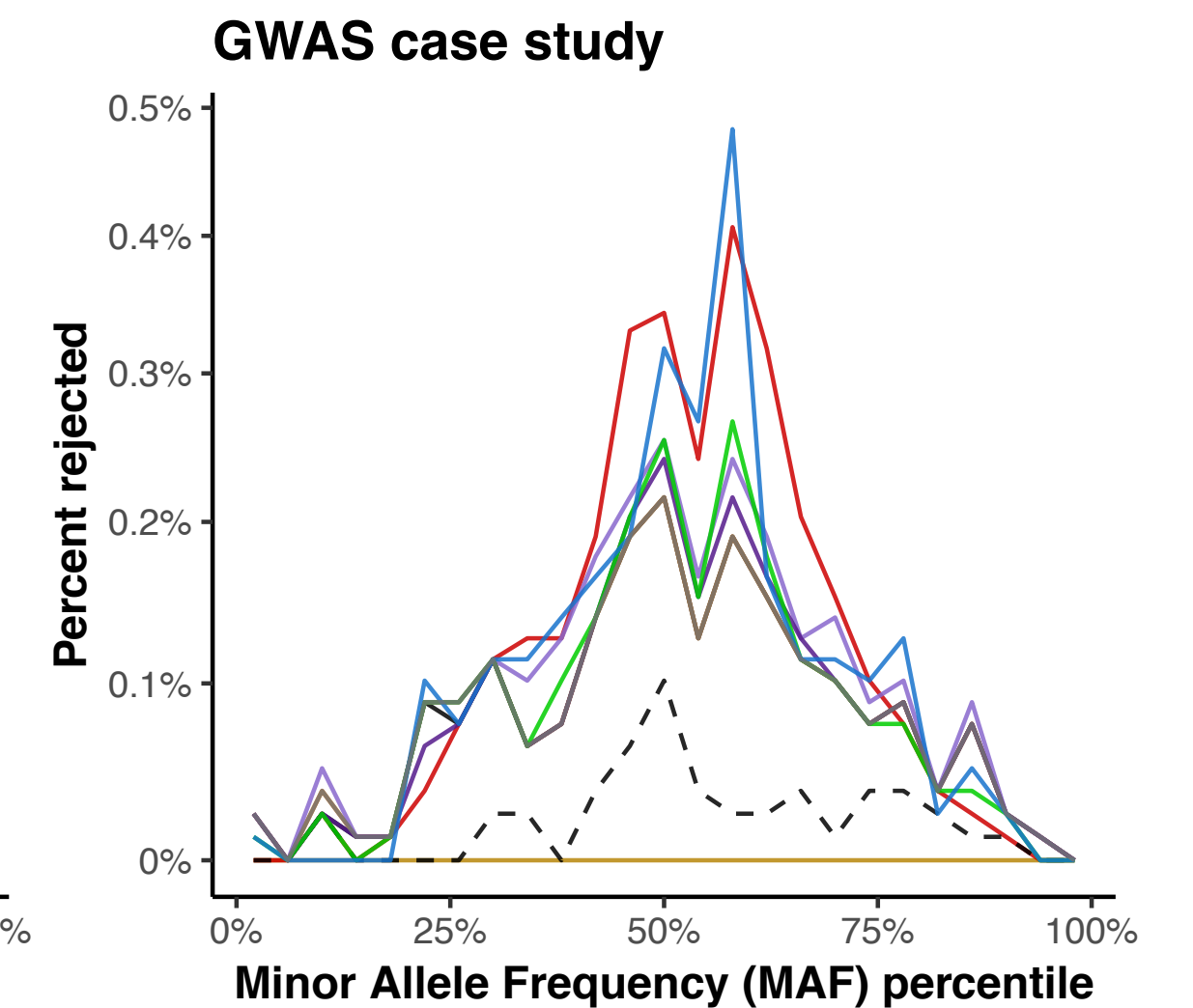
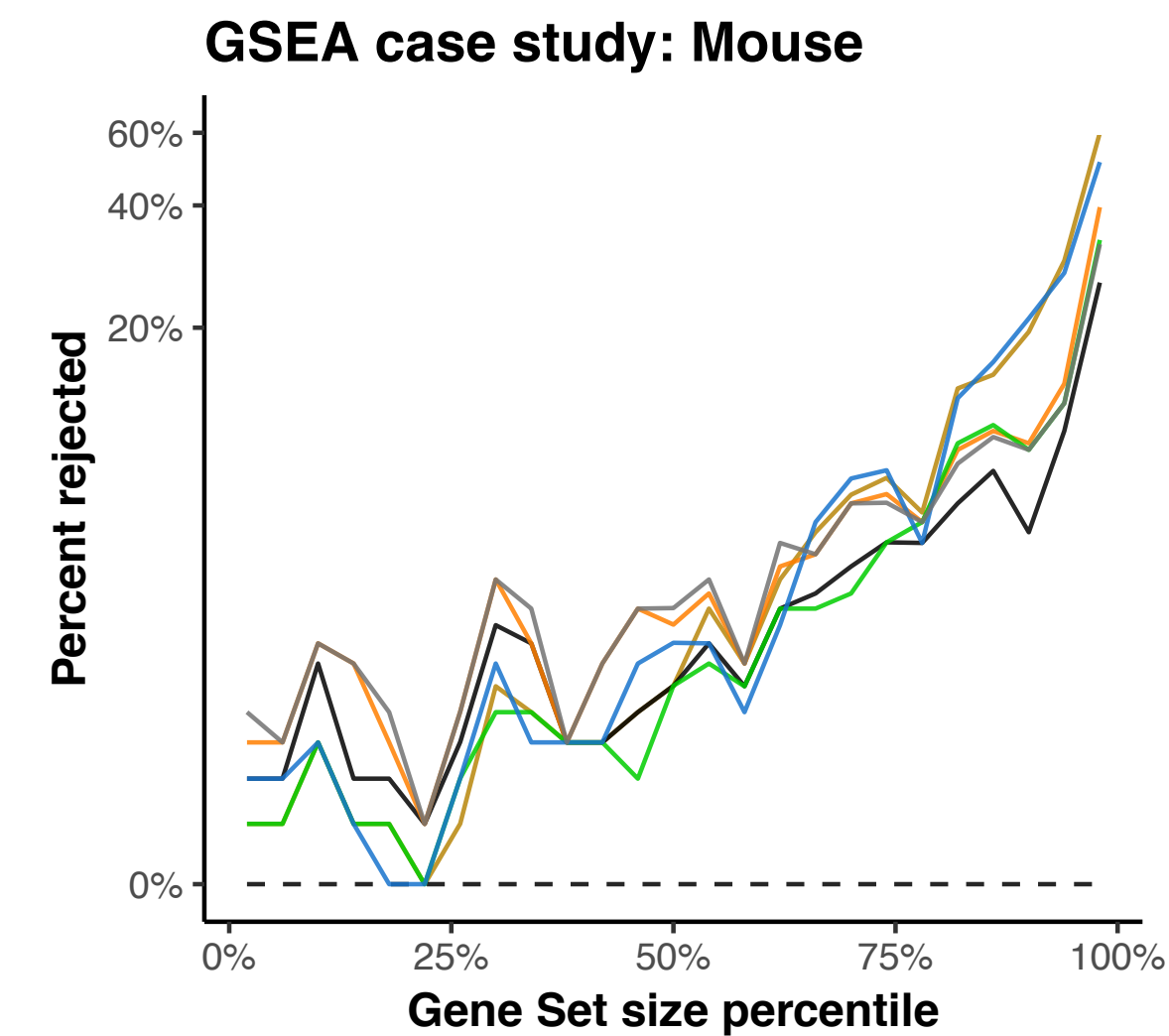
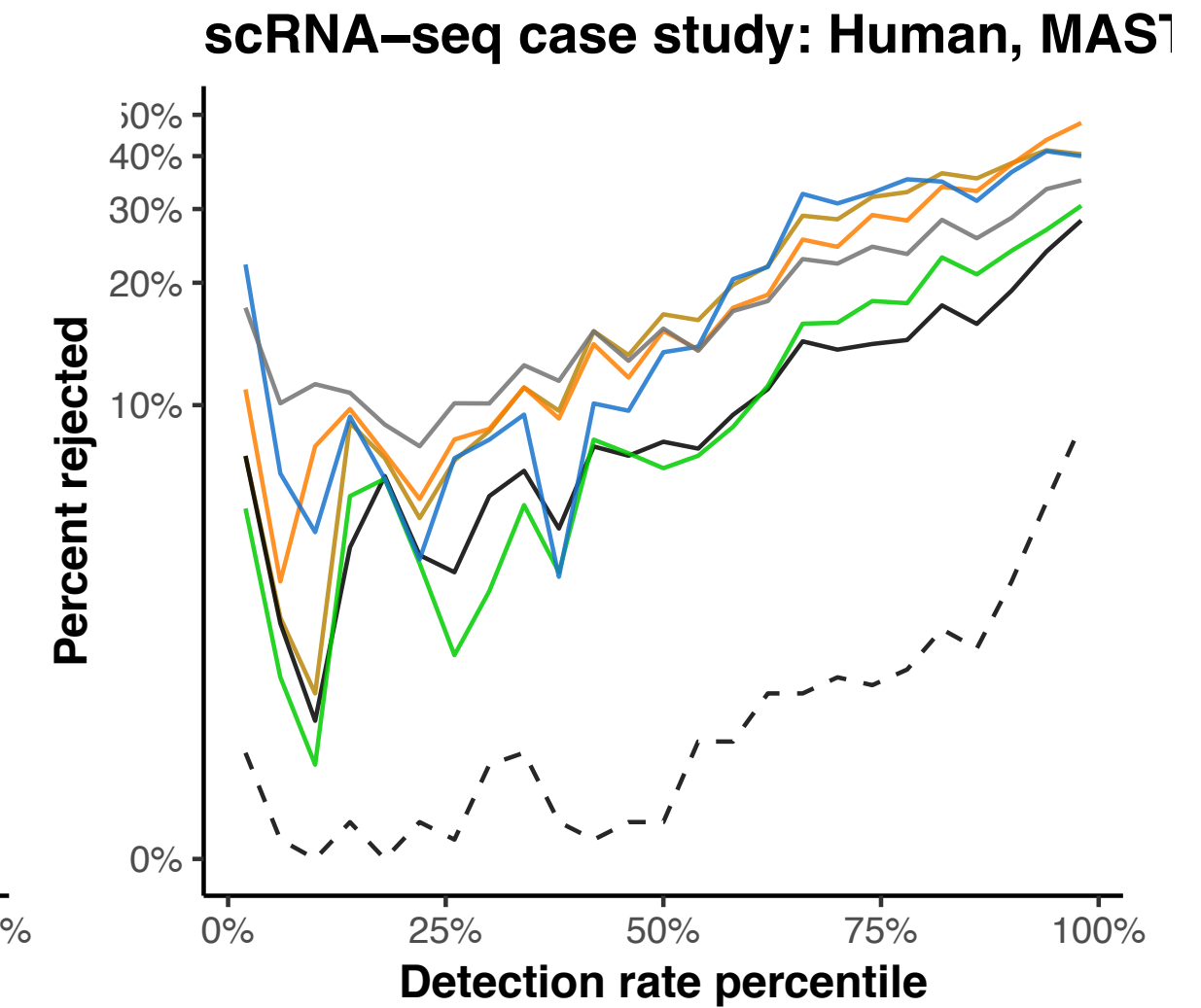
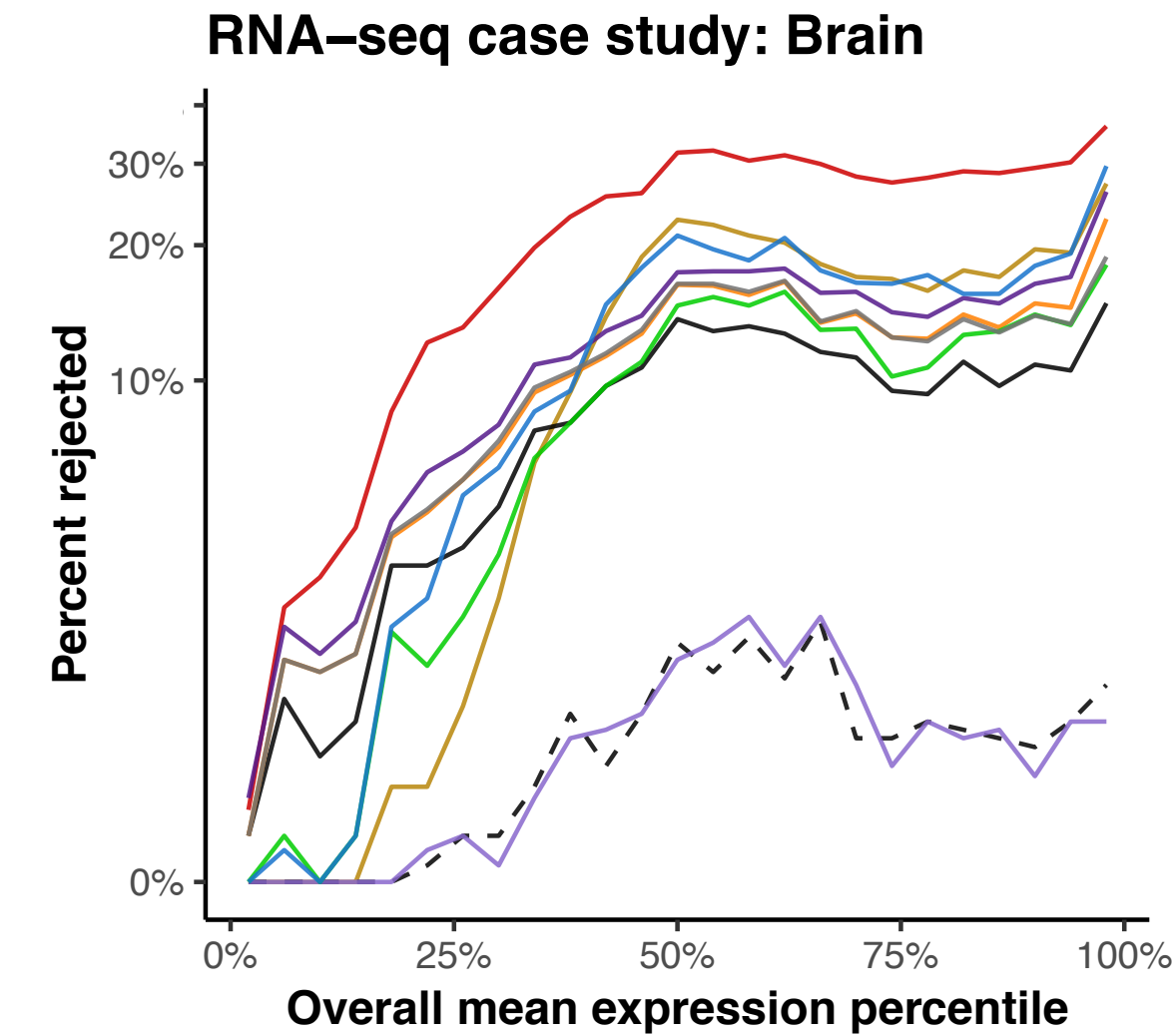
## FDR across test statistic distributions in simulation



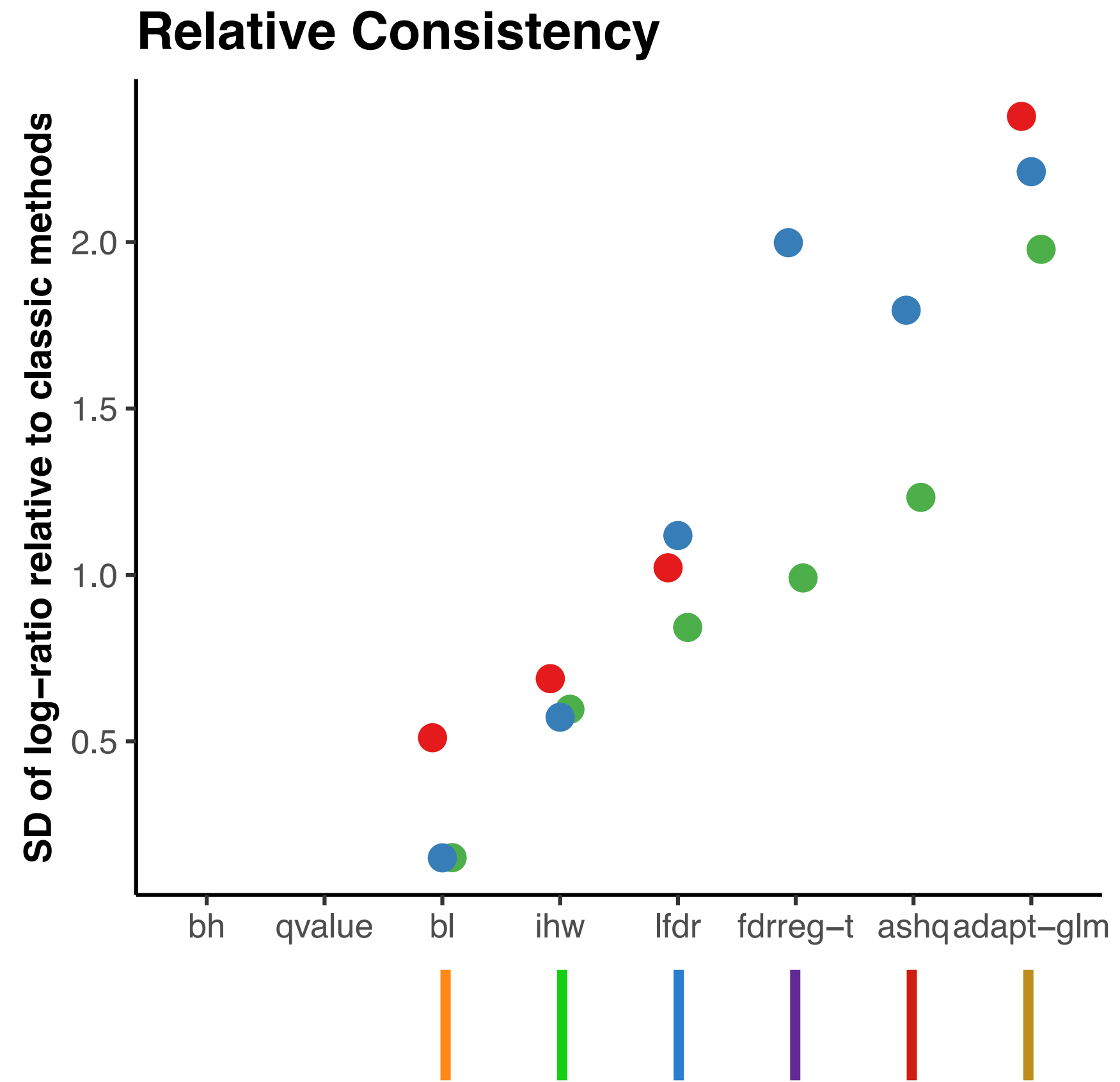
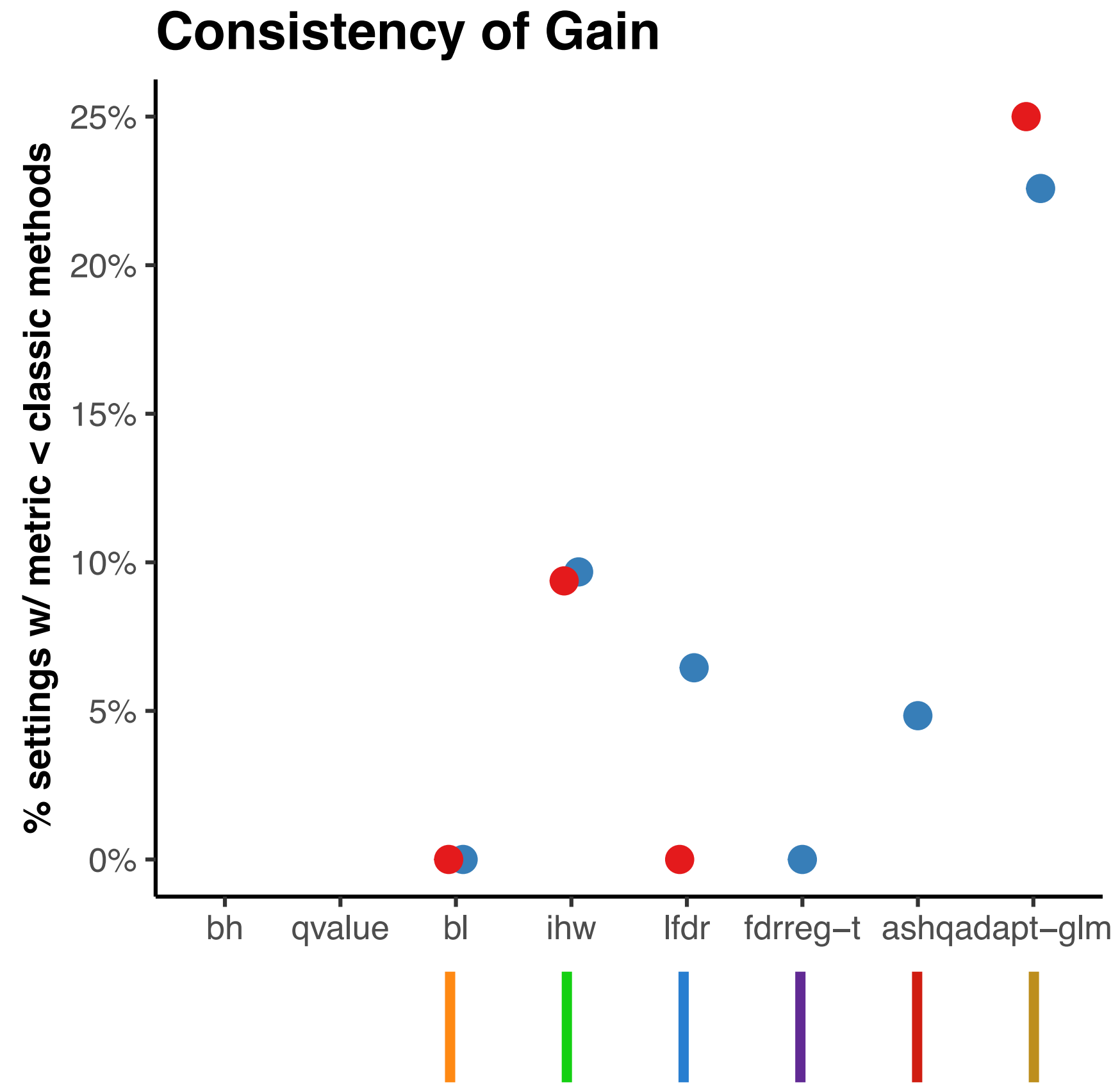


# Informative covariates in the case studies

Case Study	Covariate
Bulk RNA-seq	<b>mean gene expression</b>
Single Cell RNA-seq	mean non-zero gene expression, <b>detection rate</b>
Microbiome	mean non-zero abundance, ubiquity
ChIP-seq	mean read depth, window size
GWAS	<b>minor allele frequency</b> , sample size
Gene Set Analysis	<b>gene set size</b>



# Gains relative to classic methods varied across methods



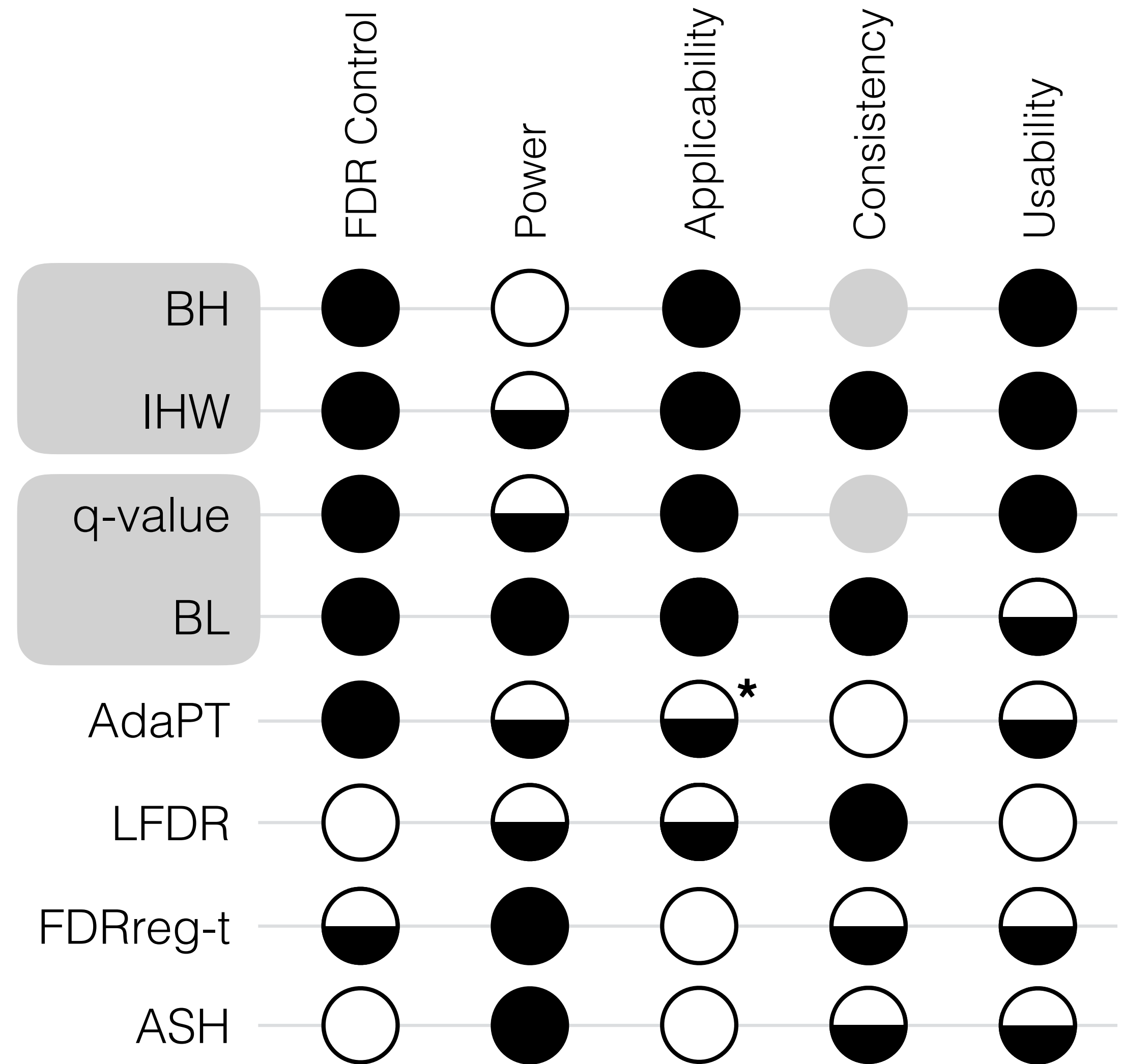
## Metric

- CS (%reject)
- Sims (TPR)
- Sims (FDR)

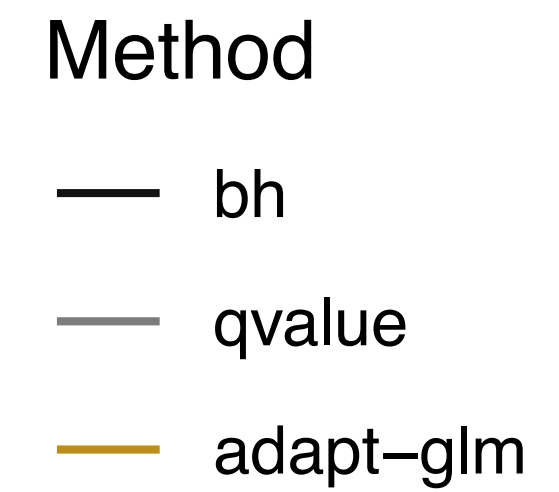
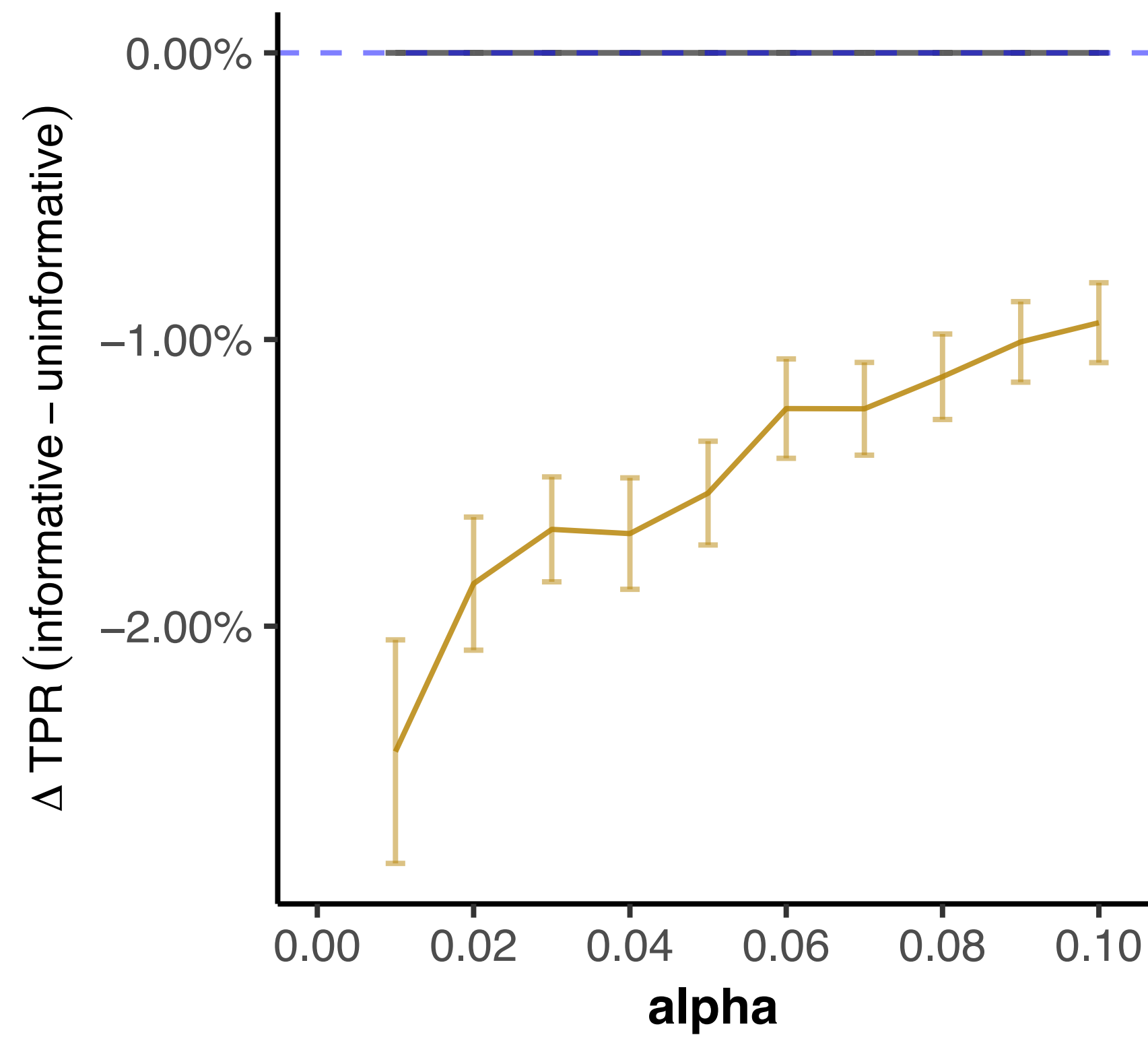
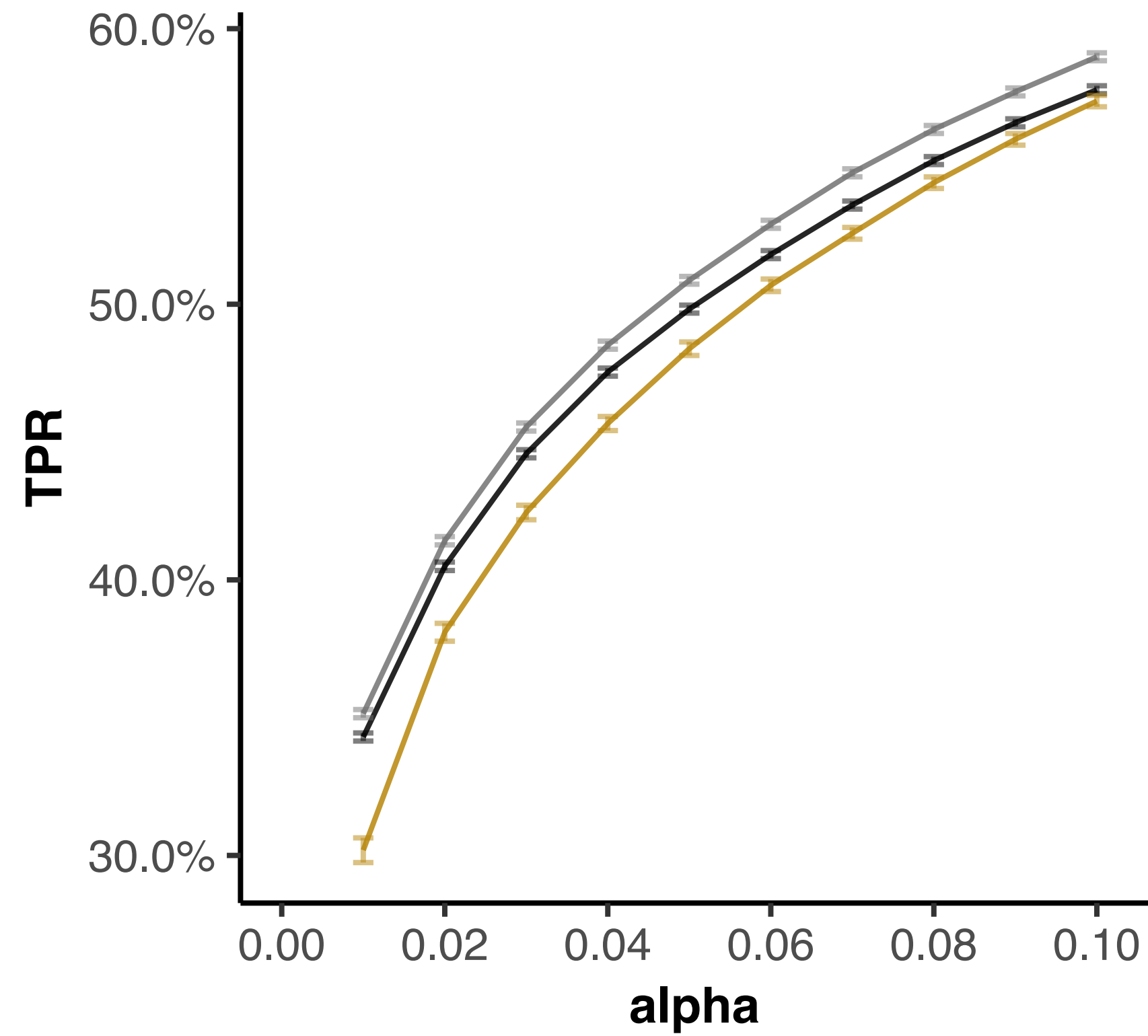


# Takeaways

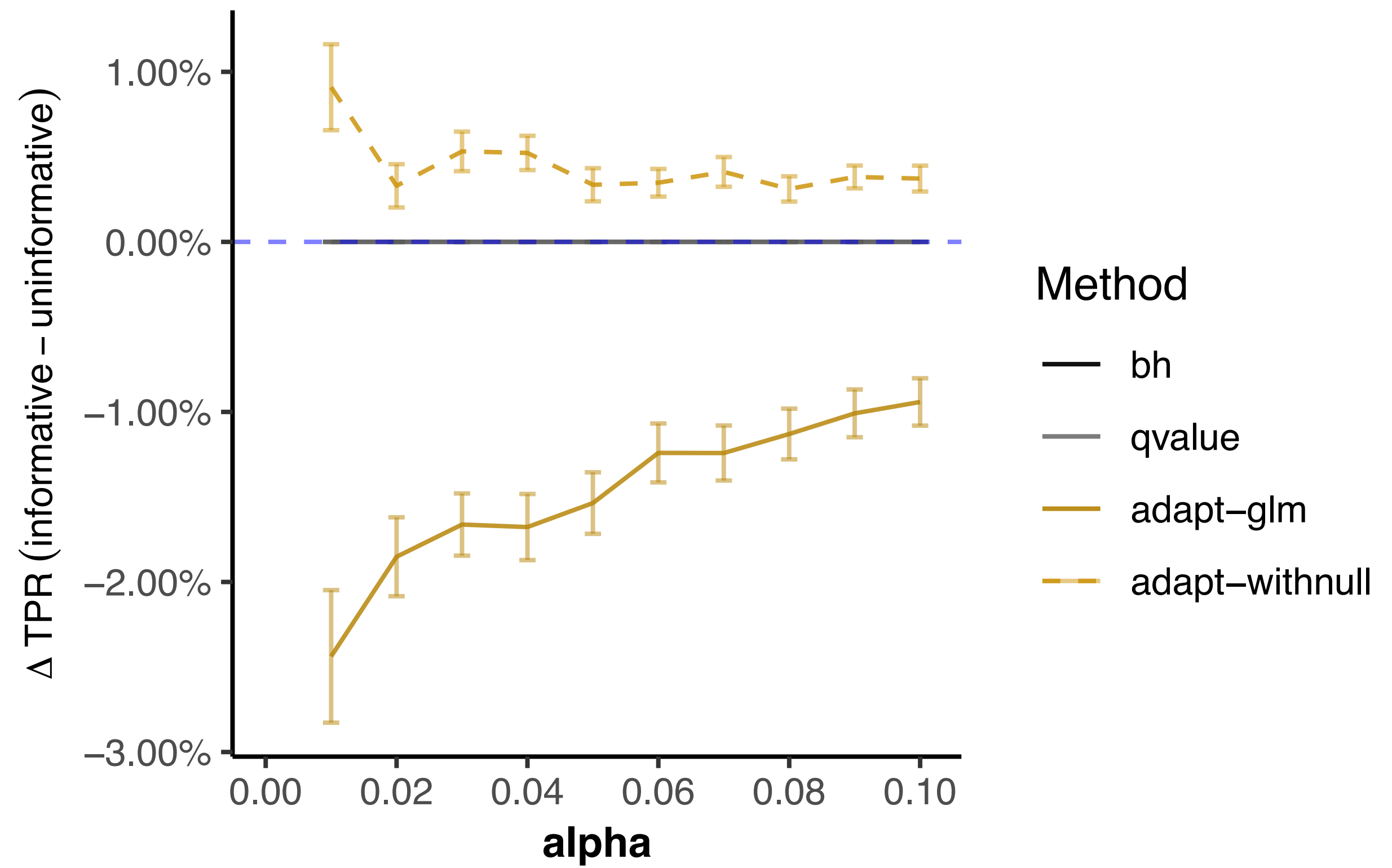
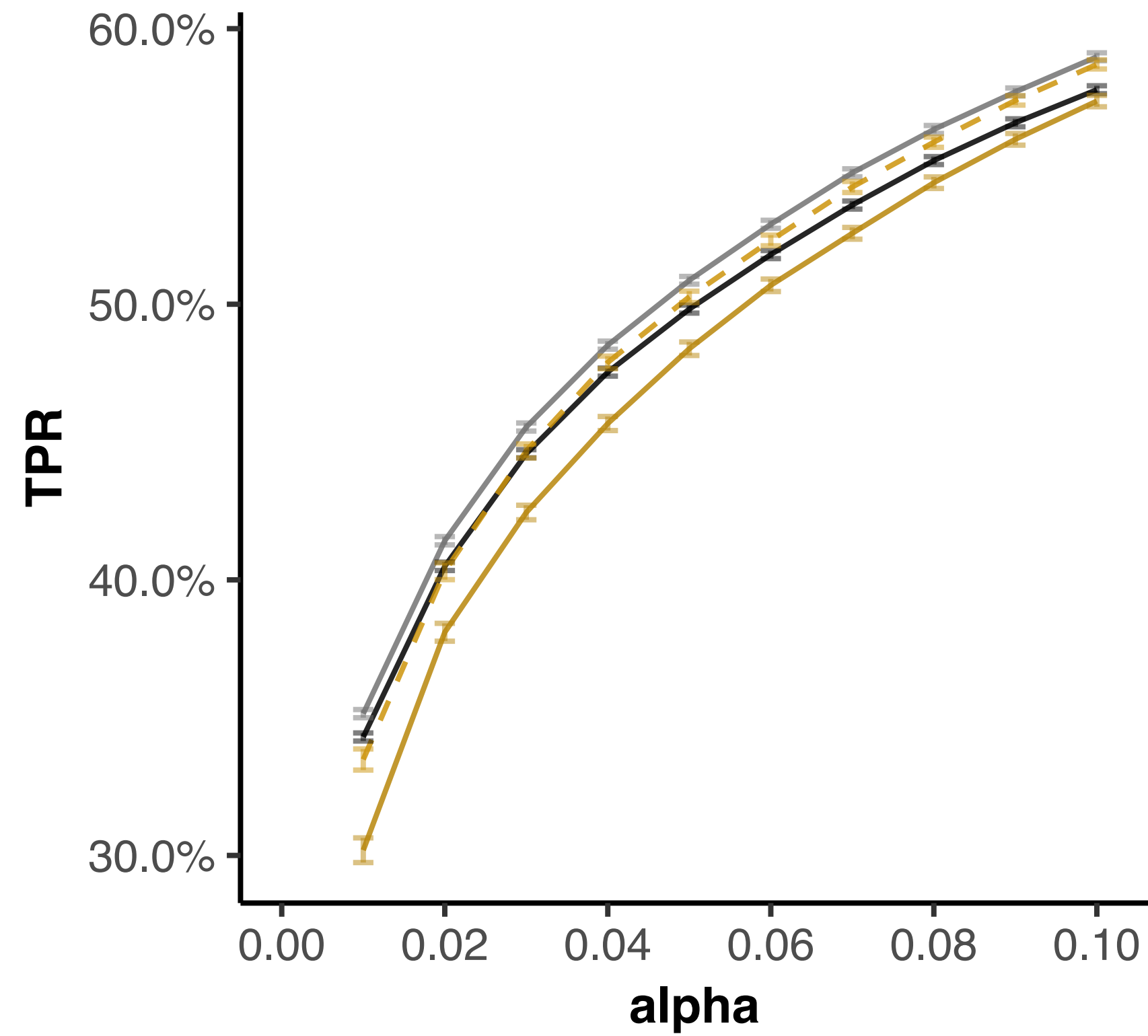
- Many covariate-aware methods provide consistent FDR control ([IHW](#), [BL](#), [AdaPT](#))
- These covariate-aware methods typically provide modest gains in power
- Not all methods could be applied to all simulations and case studies ([FDRreg](#), [ASH](#))
- Some methods showed highly variable performance across simulations and case studies ([AdaPT](#))
- **Not all R packages are created equal**



# Benchmarking as a social exercise



# Benchmarking as a social exercise



Reproducible and replicable comparisons of  
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# Recall the FDR benchmark setup

- BH procedure
- Storey's  $q$ -value

- IHW
- BL
- AdaPT
- LFDR
- FDRreg
- ASH

## Simulated Data

- *in silico* experiments
- pure simulations

## Case Studies

- RNA-seq DE
- scRNA-seq DE
- 16S microbiome DA
- ChIP-seq DB
- GWAS
- Gene Set Analysis

## FDR control

**Power**

**Applicability**

**Consistency**

**Usability**

# How the FDR benchmarking project started

```
fdr_methods <- function(dat) {  
  ## keep adjusted p-values  
  adj_pset <- list()  
  
  ## Bonferroni  
  adj_p <- p.adjust(dat$pval, "bonferroni")  
  adj_pset$bonf <- adj_p  
  
  ## BH  
  adj_p <- p.adjust(dat$pval, "BH")  
  adj_pset$bh <- adj_p  
  
  ## qvalue (Storey)  
  adj_p <- qvalue::qvalue(p=dat$pval)$qvalues  
  adj_pset$qvalue <- adj_p  
  
  . . .  
  return(adj_pset)  
}
```

```
head(tdat, n = 3)  
  H test_statistic effect_size      pval      SE  
1  1      -3.247964    -1.708222 4.465398e-03 0.5259363  
2  1      -2.453800    -1.039939 2.454995e-02 0.4238076  
3  1      -4.684693    -1.895645 1.845383e-04 0.4046467  
  
p_table <- fdr_methods(tdat)  
p_table  
$bonf  
[1] 0.19489 1.00000 0.00103 1.00000 1.00000  
[6] 1.00000 0.05170 0.11135 1.00000 0.68348  
. . .  
saveRDS(p_table, file = "my_p_table.rds")
```

## typical questions

how do we organize **data + results**?

what **parameters** did we use?

which **package version** did you use?

**dat** → **fdr\_methods()** → **adj\_pset**

...

# Problems with benchmarking computational methods

- simulation results are unstructured
  - *SummarizedBenchmark* class
- simulation code is unstructured
  - *BenchDesign* class
- code and results are disconnected
  - *SummarizedBenchmark*

```
head(tdat, n = 3)
  H test_statistic effect_size      pval      SE
1  1    -3.247964    -1.708222 4.465398e-03 0.5259363
2  1    -2.453800    -1.039939 2.454995e-02 0.4238076
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## typical questions

how do we organize **data + results**?

what **parameters** did we use?

which **package version** did you use?

...

# SummarizedBenchmark framework

## Methods



BenchDesign

## BenchDesign class

- collection of methods
  - function
- map: data → function parameters

```
## regular function call
p.adjust(p = data$pval, method = "BH")

## BenchDesign format
BDMethod(
  x = p.adjust,
  params = quos(p = pval, method = "BH")
)
```



# SummarizedBenchmark framework

## Methods

BenchDesign

## BenchDesign class

- collection of methods
  - function
  - map: data → function parameters

```
> bd
```

```
BenchDesign
```

```
-----  
benchmark data:
```

```
NULL
```

```
benchmark methods:
```

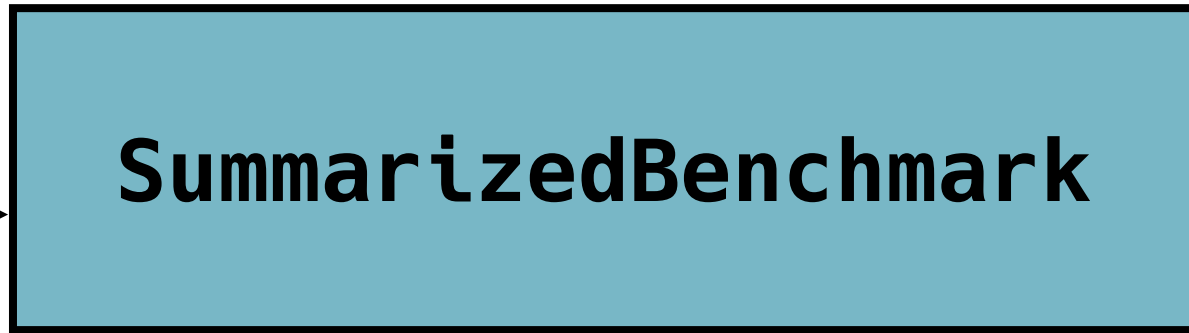
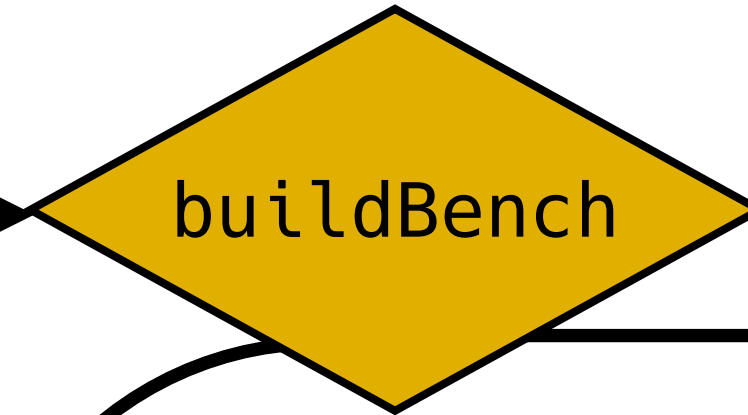
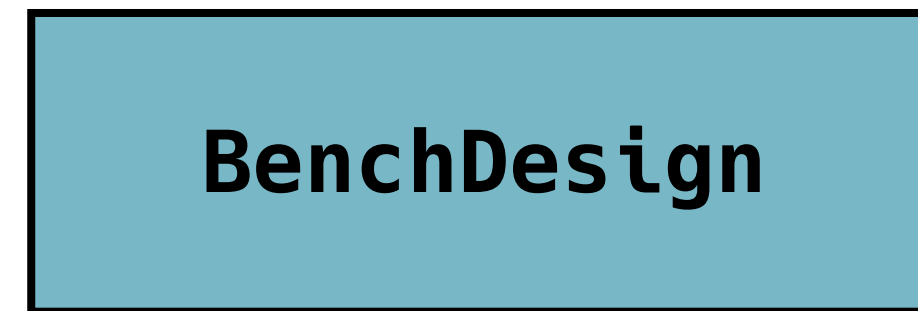
```
method: bonf; func: p.adjust
```

```
method: BH; func: p.adjust
```

```
method: qv; func: qvalue::qvalue
```

# SummarizedBenchmark framework

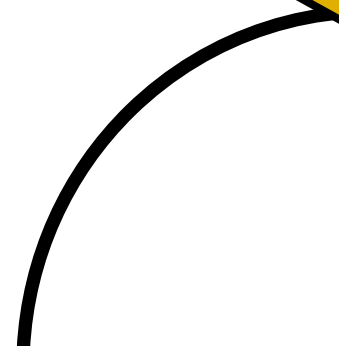
## Methods



## Results



## Dataset

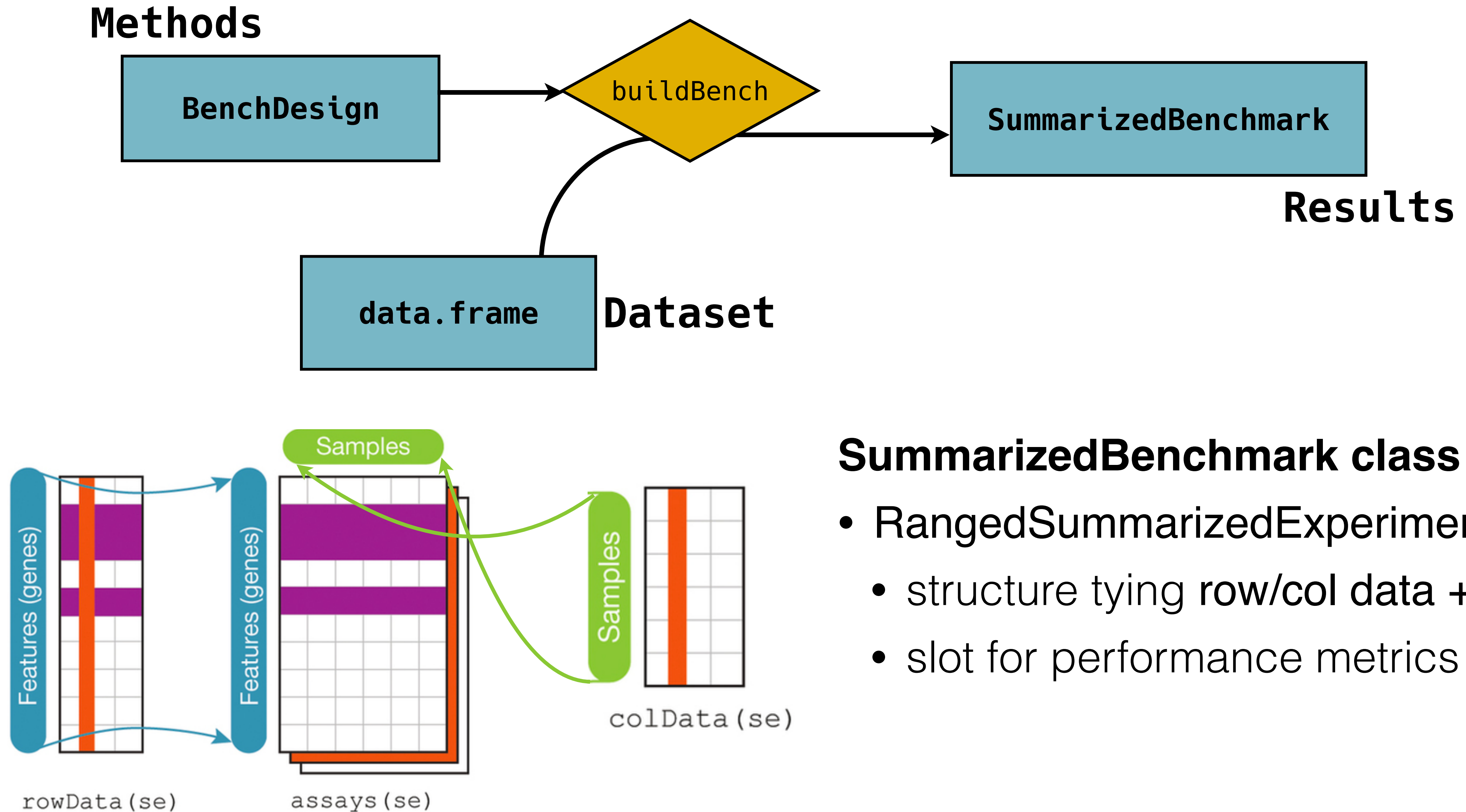


## BenchDesign class

- collection of methods
  - function
  - map: data → function parameters

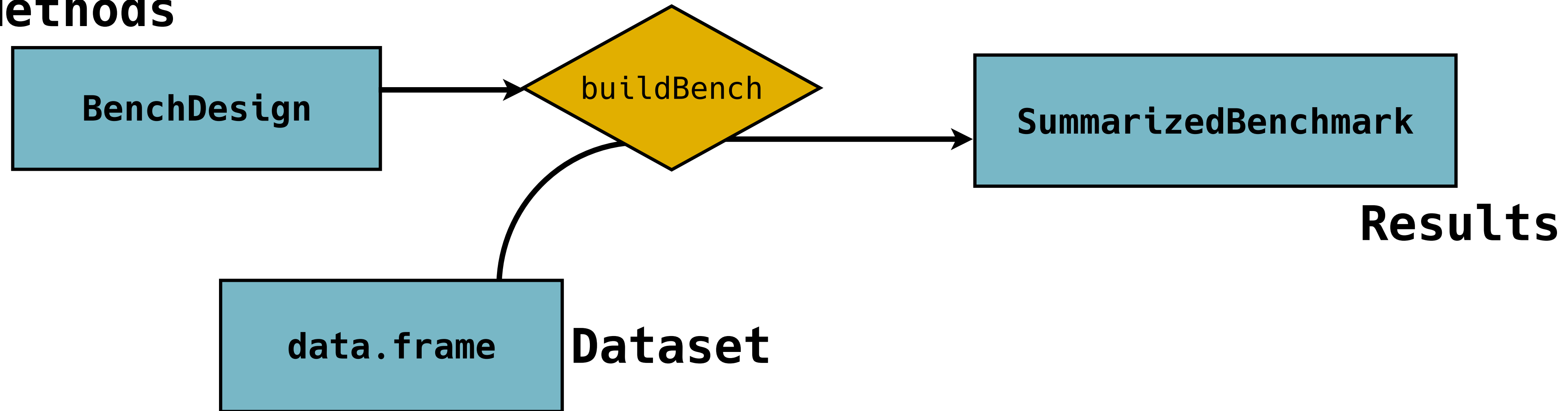
```
> bd
BenchDesign
-----
benchmark data:
  NULL
benchmark methods:
  method: bonf; func: p.adjust
  method:  BH; func: p.adjust
  method:  qv; func: qvalue::qvalue
```

# SummarizedBenchmark framework



# SummarizedBenchmark framework

## Methods



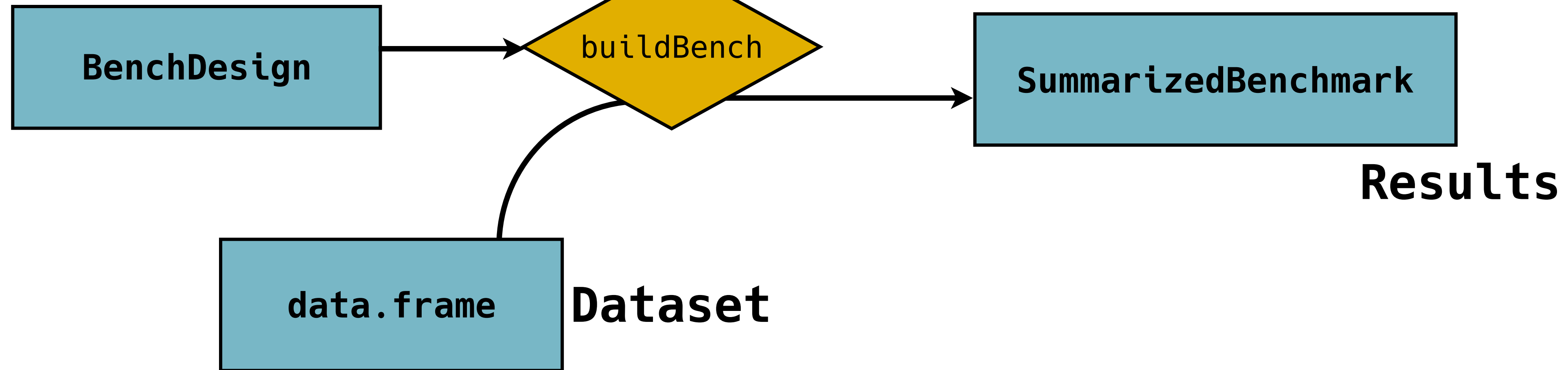
```
> sb
class: SummarizedBenchmark
dim: 50 3
metadata(1): sessions
assays(1): H
rownames: NULL
rowData names(1): H
colnames(3): bonf BH qv
colData names(6): func.pkg func.pkg.vers ...
param.method session.idx
```

## SummarizedBenchmark class

- RangedSummarizedExperiment class
  - structure tying row/col data + results
  - slot for performance metrics

# SummarizedBenchmark framework

## Methods

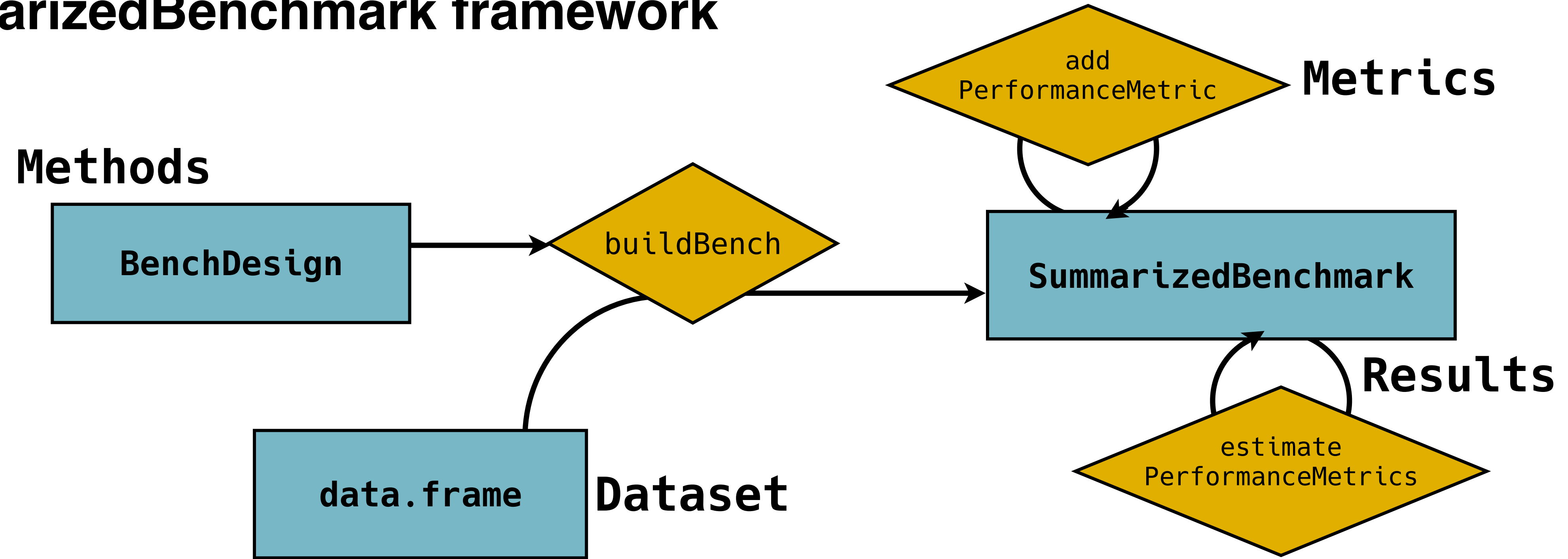


```
> colData(sb)
```

```
DataFrame with 3 rows and 5 columns
```

	<b>func.pkg</b>	<b>func.pkg.vers</b>	<b>func.pkg.manual</b>	<b>param.p</b>	<b>param.method</b>
	<character>	<character>	<logical>	<character>	<character>
<b>bonf</b>	stats	3.5.0	FALSE	pval	"bonferroni"
<b>BH</b>	stats	3.5.0	FALSE	pval	"BH"
<b>qv</b>	qvalue	2.12.0	FALSE	pval	NA

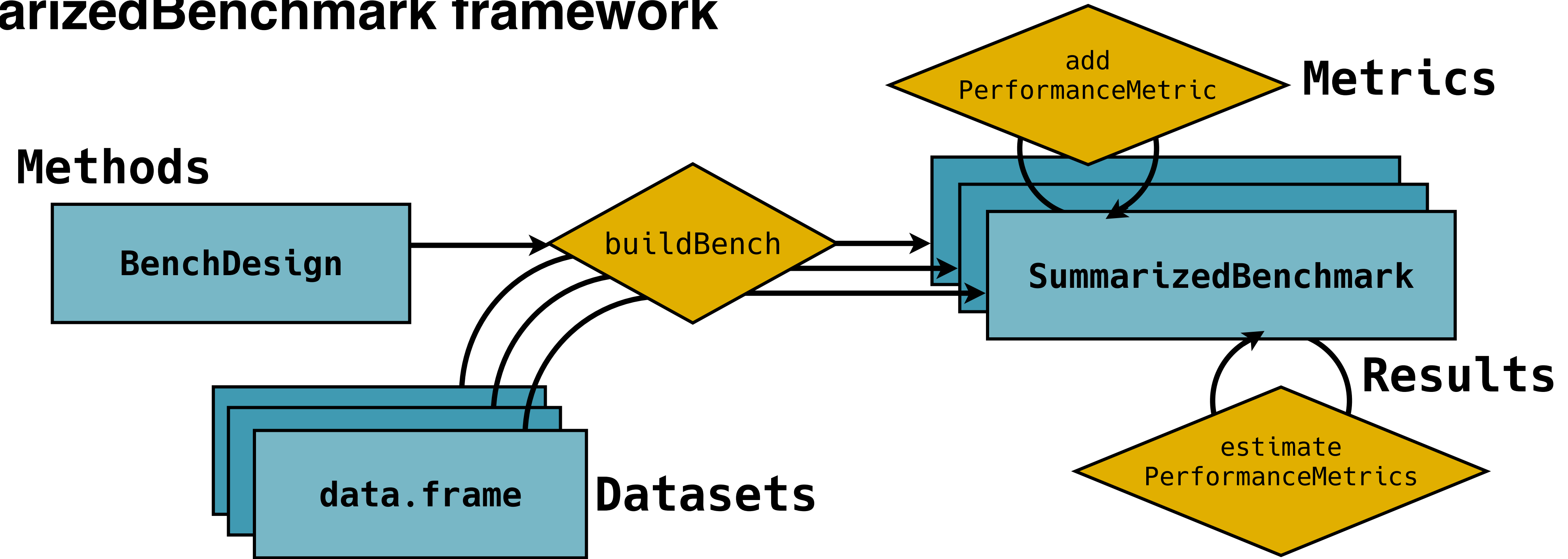
# SummarizedBenchmark framework



## performanceMetrics

- map: results (+ metadata) → metrics
- e.g. FDR, TPR, #rejections

# SummarizedBenchmark framework



## Additional Features

- iterative benchmarking
- error handling
- parallelization

## Ongoing Work

- handling larger pipelines
- additional default metrics

# SummarizedBenchmark

## Proposed framework

- methods
- data
- results
- summaries

The image shows two overlapping browser windows. The top window is the Bioconductor website for the SummarizedBenchmark package. The bottom window is the documentation website for SummarizedBenchmark, hosted on www.pkimes.com.

**Bioconductor Page:**

- URL: <https://bioconductor.org/packages/devel/bioc/html/SummarizedBenchmark>
- Navigation: Home, Install, Help, Developers, About
- Breadcrumb: Home » Bioconductor 3.9 » Software Packages » SummarizedBenchmark (development version)
- Section: SummarizedBenchmark
- Documentation link: Documentation » Bioconductor

**Documentation Page:**

- URL: [www.pkimes.com/SummarizedBenchmark/](http://www.pkimes.com/SummarizedBenchmark/)
- Version: SummarizedBenchmark 1.99.3
- Navigation: Quick Start, Reference, Articles
- Section: SummarizedBenchmark
- Text: SummarizedBenchmark defines a flexible framework for benchmarking computational methods in R. Classes and functions are provided for defining, executing and evaluating benchmark experiments. The package builds on the SummarizedExperiment class to keep results organized, with outputs tied directly with important method metadata. This site is for the development version of the package. Documentation and examples for the current Bioconductor release version of the package can be found at the official [release page](#).
- Text: If you have any suggestions on how we can improve the package, [let us know!](#)
- Section: Installation
- Code Block:

```
# Install development version from Bioconductor
BiocManager::install("SummarizedBenchmark", version = "devel")

# Install release version from Bioconductor
BiocManager::install("SummarizedBenchmark")
```
- Section: Usage
- Links:
  - Download from BIOC at <https://www.bioconductor.org/packages/SummarizedBenchmark>
  - Browse source code at <https://github.com/areyesq89/SummarizedBenchmark>
  - Report a bug at <https://github.com/areyesq89/SummarizedBenchmark/issues>
- License: GPL (>= 3)
- Citation: Citing SummarizedBenchmark
- Developers:
  - Alejandro Reyes: Author, maintainer
  - Patrick Kimes: Author
- Dev status

Kimes PK\* and Reyes A\*. (2018). Reproducible and replicable comparisons using *SummarizedBenchmark*. Bioinformatics.



## Acknowledgements

### FDR Benchmarking

- Keegan Korthauer\*
- Stephanie Hicks
- Claire Duvallet
- Ayshwarya Subramanian
- Alejandro Reyes
- Chinmay Shukla
- Mingxiang Teng

### SummarizedBenchmark

- Alejandro Reyes\*

**Rafael Irizarry**

