Swampland conjectures from Black Holes and Finiteness



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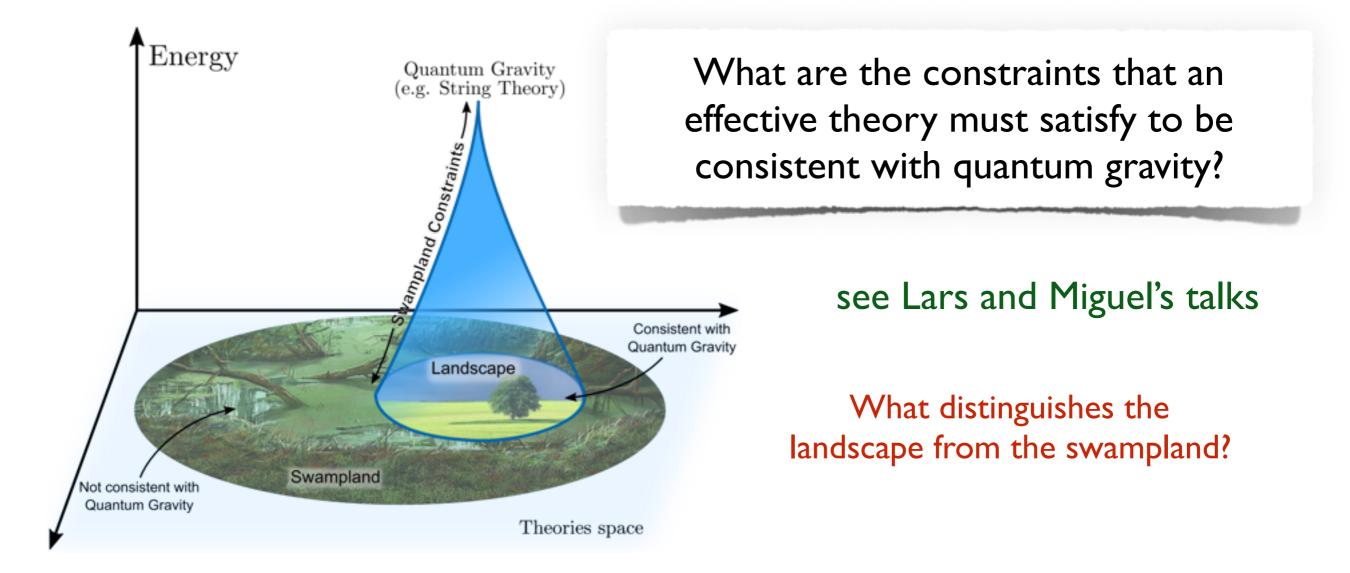
Harvard University + IFT Madrid



Based on 2111.00015 with Hamada, Montero and Vafa

Strings: Geometry and Symmetries for Phenomenology, Oaxaca, November 2021

Goal of the Swampland program:

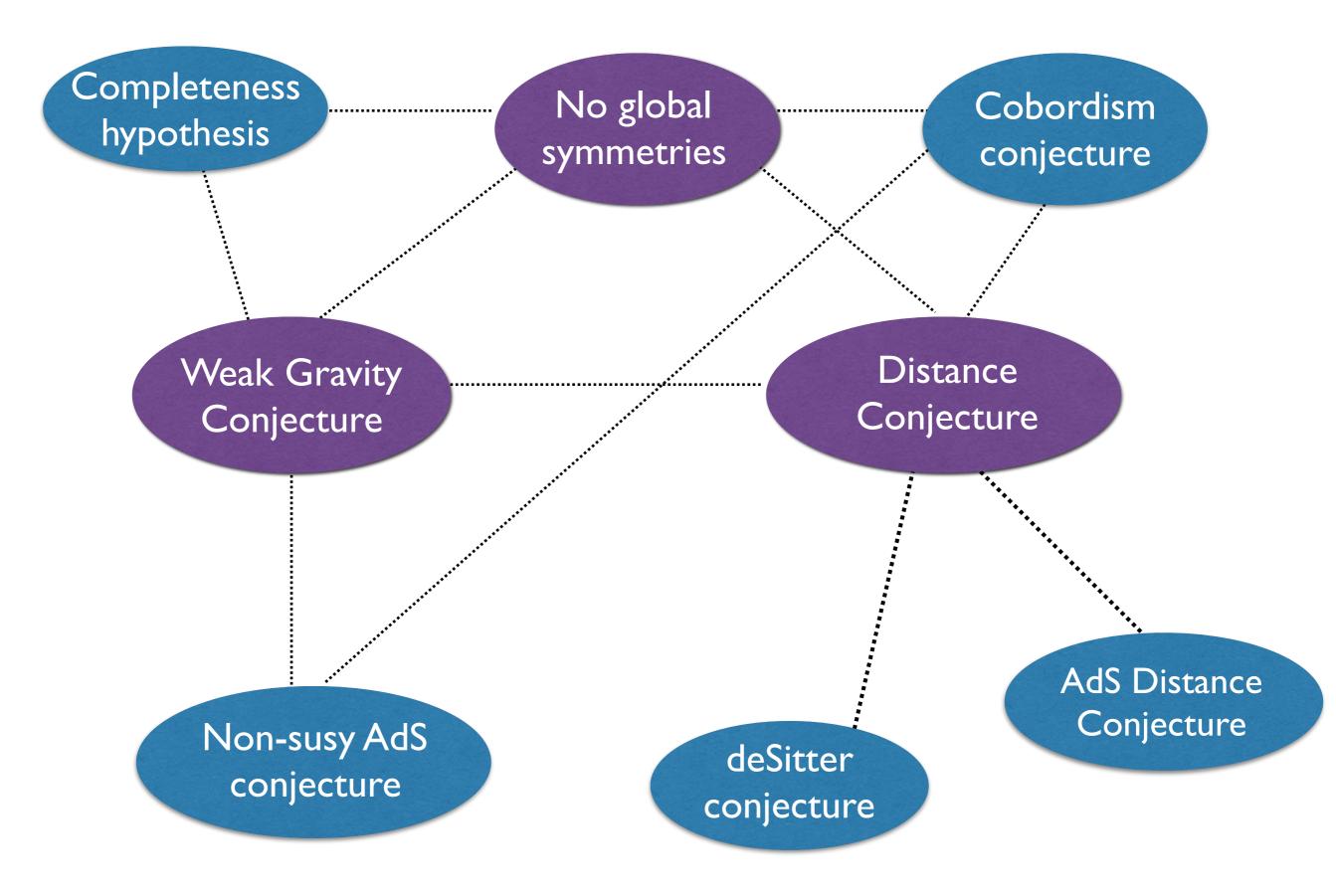


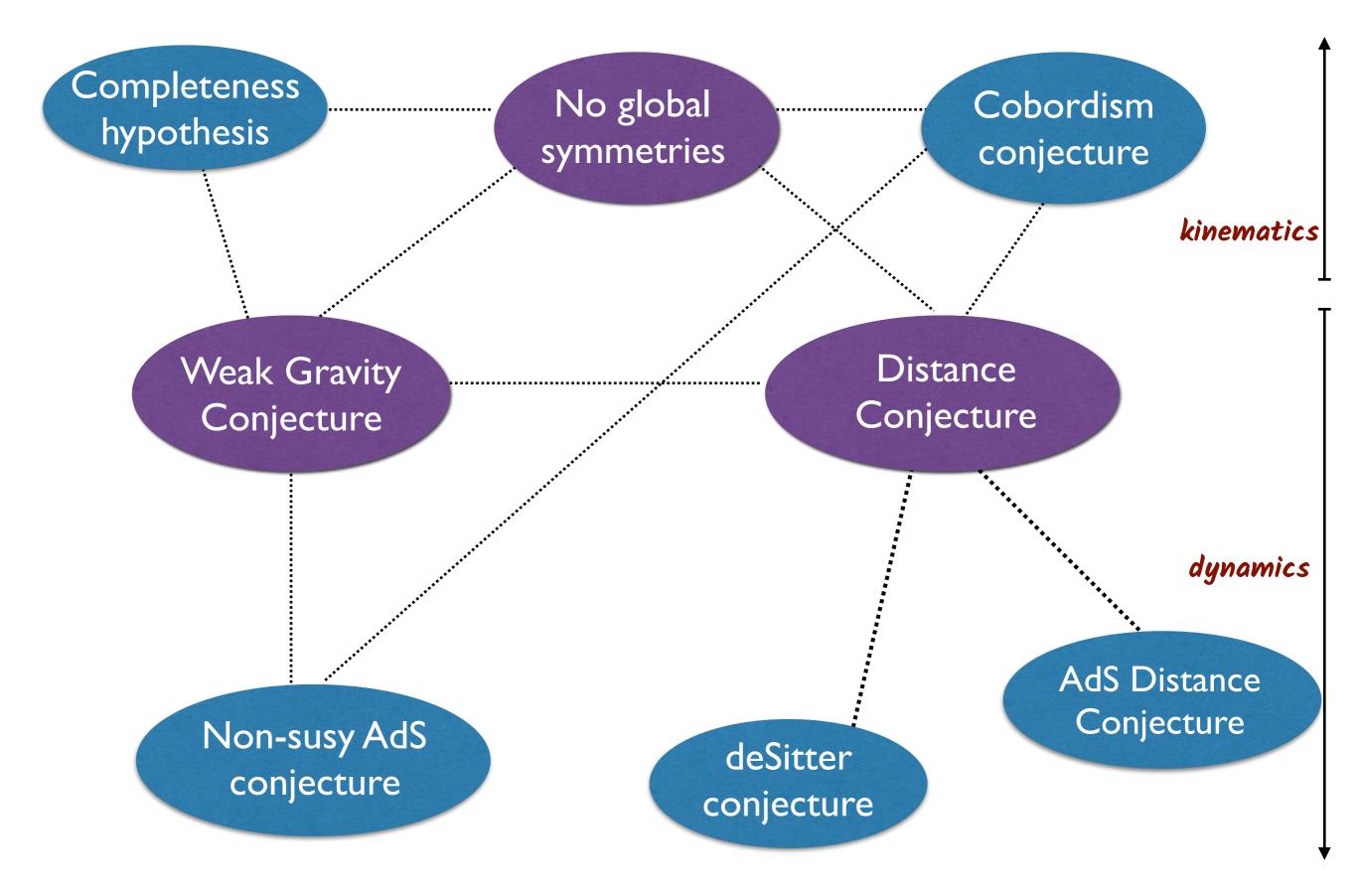


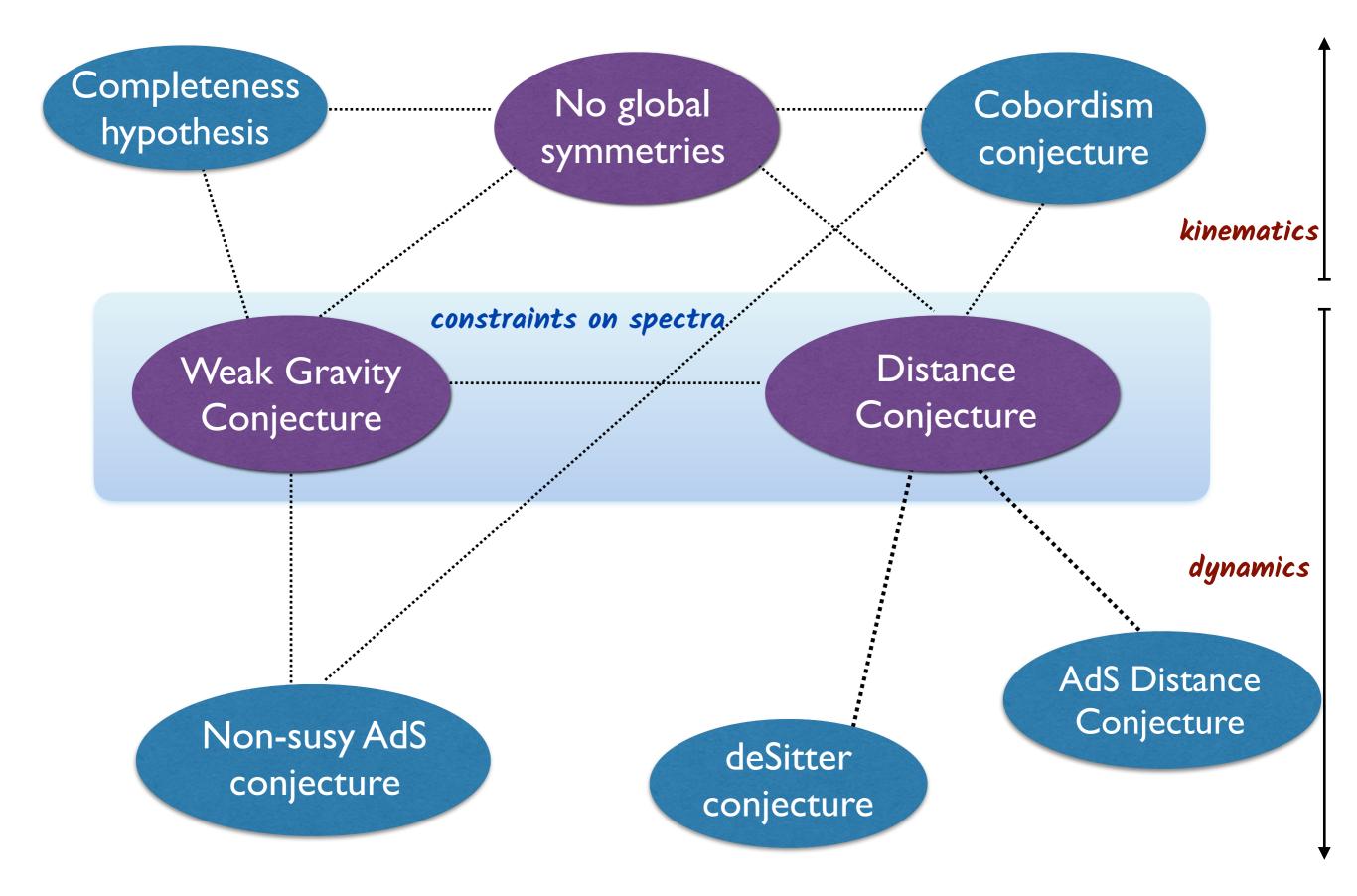
- Guiding principles to construct BSM models
- When the second second

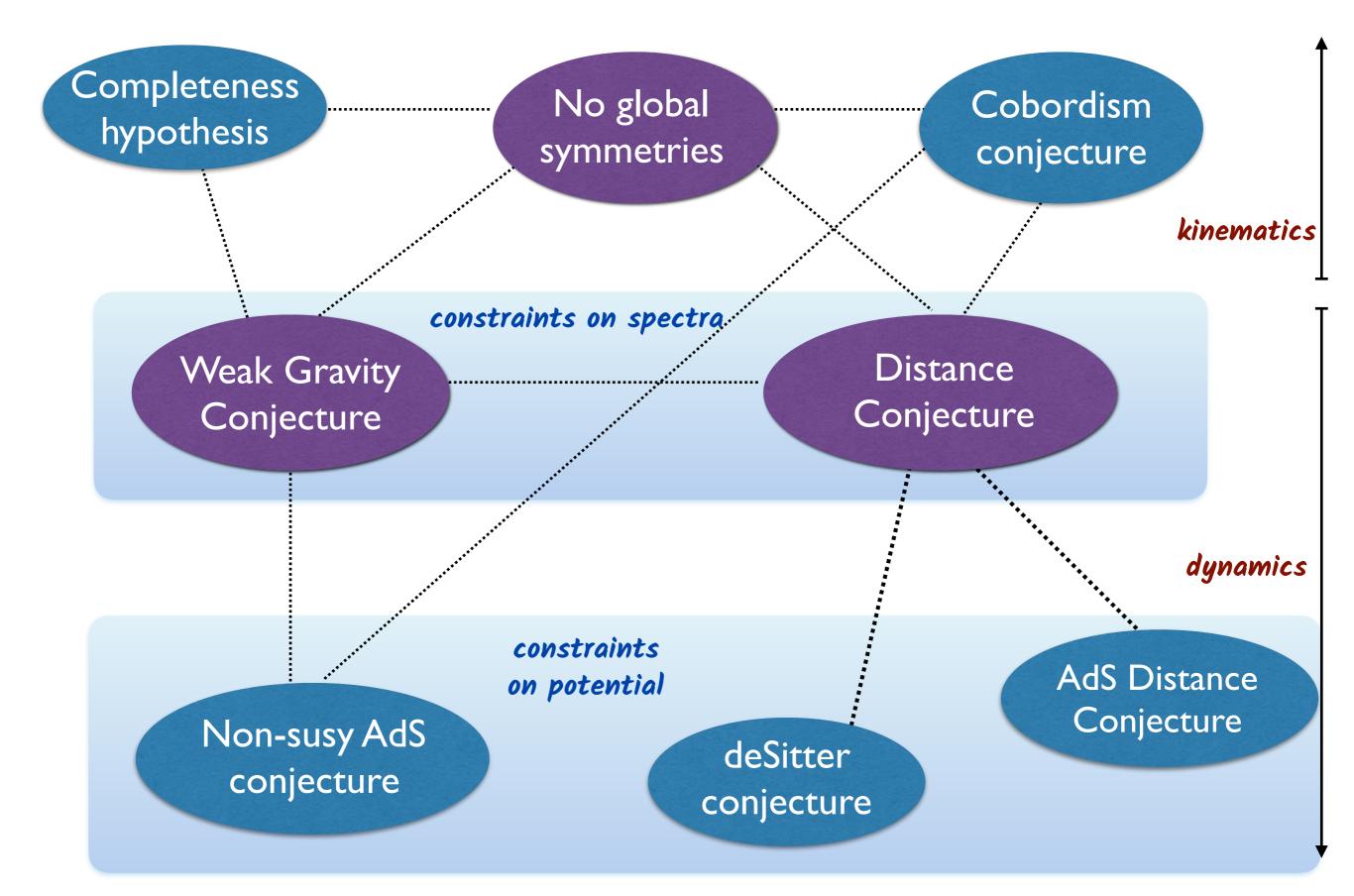
Outline

- Introduction
 - Swampland program
 - Asymptotic towers of states (WGC and SDC)
 - Review of state-of-the-art
- Swampland conjectures from Finiteness and Black Holes
 - Asymptotic towers of states from black hole entropy bounds
 - UV compactness and Emergence
 - Finiteness of quantum gravity amplitudes (and vacua)









Swampland Program

Step 0: Identify universal patterns (swampland conjectures)

Quantitative tests in string theory

Explain underlying QG principle

Phenomenological implications

Swampland Program

Recall: EFT expectations can fail in the presence of gravity

For instance, EFT breaks down at a scale much below Mp if we have:

- Small gauge couplings
- Large field ranges

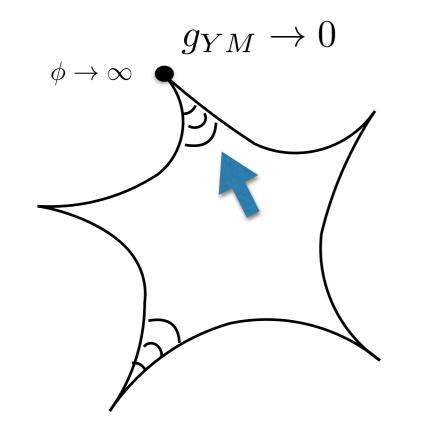
. . .

Approximate global symmetries

because of the presence of an infinite tower of states becoming light

Asymptotic Towers of States

Surprising from EFT point of view, but very natural from string theory perspective:



The tower hints a new weakly coupled description of the theory



Linked to string dualities

Typically, they signal decompactification or string perturbative limit

Emergent String Conjecture [Lee,Lerche,Weigand'19]

Approximate global symmetries, Weakly coupled gauge theories, Large field ranges...

...come at a price.

Weak Gravity Conjecture (WGC):

Given a gauge theory, there must exist an electrically charged state with

 $\frac{Q}{M} \ge \left(\frac{Q}{M}\right)_{\text{extremal}} = \mathcal{O}(1) \quad \begin{array}{l} \mathbf{Q} = \mathbf{q} \ \mathbf{g} : \text{charge} \\ \mathbf{m} : \text{mass in} \\ \mathbf{P} \text{lanck units} \end{array}$

Strong version: there is a sublattice/tower of superextremal states

[Montero et al.'16][Heidenreich et al.'15-16][Andriolo et al'18]

(Swampland) Distance Conjecture (SDC):

There is an infinite tower of states becoming exponentially light at every infinite field distance limit of the moduli space

> $m(P) \sim m(Q)e^{-\alpha\Delta\phi}$ when $\Delta \phi \to \infty$

(geodesic distance)

[Ooguri-Vafa'06]

UV cut-off goes to zero due to new light states

 $\Lambda \sim g M_p$ $\Lambda \sim M_p \exp(-\alpha \Delta \phi)$

Phenomenological implications

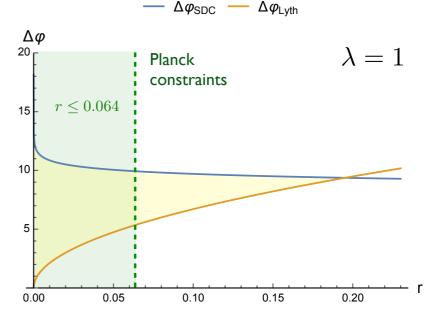
WGC: constrains theories with tiny gauge couplings and large axionic decay constants

• SDC: constrains theories with large field ranges $\Delta \phi \lesssim \frac{1}{\lambda} \log \left(\frac{M_p}{\Lambda} \right)$

Example: Constraints on large field inflation:

$$\begin{array}{ll} \mbox{If } H \leq \Lambda \\ \Delta \phi \leq \frac{1}{\lambda} \log \frac{M_p}{H} \end{array} \end{array} = \frac{1}{\lambda} \log \sqrt{\frac{2}{\pi^2 A_s r}} \end{array}$$

Opposite scaling than Lyth bound!



[Scalisi,IV'18]

Asymptotic Towers of States

String Theory Evidence:

- More than 8 supercharges: $\mathcal{M} = G/H$ [Cecotti'15]
- Theories with 8 supercharges:
 - 5d/6d N=1 theories: F-theory CY compactifications
 - 4d N=2 theories: Calabi-Yau compactifications of Type II

Systematic classification of limits \checkmark

[Lee,Lerche,Weigand'18-19] [Grimm, Palti, IV'18]Gendler,IV'20] [Grimm,Palti,Li'18] [Baume,Marchesano,Wiesner'19] [Corvilain, Grimm, IV'18]

AdS/CFT [Perlmutter,Rastelli,Vafa,IV'20]

[Luest, Palti, Vafa' 19] [Baume, Calderon-Infante'20]

Theories with 4 supercharges

[Lanza, Marchesano, Martucci, IV'20] [Klaewer, Lee, Weigand, Wiesner'20]

What is the value of the exponential rate?

 AdS_{d+1}/CFT_d with d>2 [Perlmutter,Rastelli,Vafa,IV'20]

$$\alpha = \sqrt{\frac{2c}{\dim G}} \geq \frac{1}{\sqrt{3}} \quad \text{for 4d N=2}$$
$$\geq \frac{1}{2} \quad \text{for 4d N=1}$$

[Grimm, Palti, IV'18] [Gendler, IV'20]

Lower bound for BPS states in CY compactifications: α

$$x \ge \frac{1}{\sqrt{2n}}$$
 for CY_n

$$\label{eq:constraint} \bigstar \mathsf{TCC} \qquad \alpha \geq \frac{1}{\sqrt{(d-2)(d-3)}} \qquad \text{[Bedroya,Vafa'I9] [Andriot et al'20]}$$

Asymptotic Towers of States

A bottom-up explanation independent of string theory is missing

Promising avenue: think about black hole physics

Distance Conjecture ??

Weak Gravity Conjecture: to allow extremal black holes to decay It only supports a mild version of WGC

(a single particle is needed, not a tower)

In this talk:

I will provide new arguments in support of these conjectured asymptotic towers of states based on finiteness of black hole entropy

... or more generally, finiteness of quantum gravity amplitudes

Very nice connection with **Emergence Proposal**

Finiteness

Many Swampland conditions somehow emerge from a suitable replacement of infinity by a finite number, achieved when Mp is finite

✤ Finite number of degrees of freedom below a cut-off $N \leq \left(\frac{M_p}{\Lambda}\right)^{d-2}$

Finite number of quantum gravity vacua

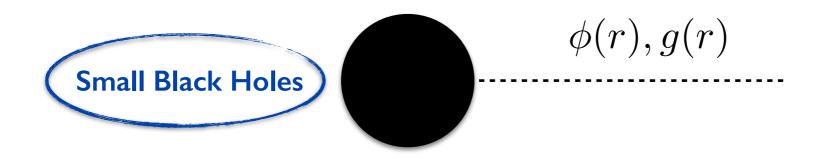
[Arkani-Hamed'05][Dvali'07]...

We want to initiate a program to view all the Swampland criteria from the prism of finiteness, thus taking a step in unifying the conjectures.

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Let us engineer some large field range and weak coupling limit induced by the backreaction of a solitonic object in a given EFT



What goes wrong then?

Very useful avenue in [Klaewer, Palti'16] charged dilatonic black holes

[Draper, Farkas'19] bubble of nothing, dilatonic BHs...

[Bonnefoy et al'19] large black holes

[Lanza, Marchesano, Martucci, IV'20-21] low codimension objects

Take Einstein-Maxwell-Dilaton theory:

$$\begin{split} S &= \int d^4x \sqrt{-g} \left[R + 2 |d\phi|^2 + \frac{1}{2g(\phi)^2} |F|^2 \right] \\ & \text{ such that } \quad g(\phi) \to 0 \quad \text{ as } \quad \phi \to \infty \end{split}$$

Look for electrically charged extremal black hole solutions

$$ds^{2} = -e^{2U}dt^{2} + e^{-2U}\left(\frac{d\tau^{2}}{\tau^{4}} + \frac{1}{\tau^{2}}d\Omega_{2}^{2}\right)$$
$$F = \frac{g^{2}}{4\pi}Qe^{2U}\tau^{2}$$

Due to the attractor mechanism, the dynamics is captured by the eom of:

subject to

$$\mathcal{L}_{1d} = \frac{1}{2} \left(\dot{U}^2 + \dot{\phi}^2 \right) + g^2 Q^2 e^{2U} \xrightarrow{\text{extremal BHs}}$$
the constraint $\dot{U}^2 + \dot{\phi}^2 - g^2 Q^2 e^{2U} = 0$

BH induces a running of the scalar field and gauge coupling as approaching the horizon

$$\phi(\tau)$$

$$\tau = -\infty$$

$$\tau = 0$$

Extremal black holes:

$$\dot{U}^2 \le g^2 Q^2 e^{2U} \longrightarrow A(\tau) = \frac{e^{-2U(\tau)}}{\tau^2} \le \frac{1}{\tau^2} \left(1 + Q \int_{\tau}^0 g(\tau) \, d\tau\right)^2$$

 If $g(\tau) = \text{constant}$ then $A(-\infty) > 0$: Reissner-Nordstrom BH

 $\label{eq:alpha} \mbox{ If } g(-\infty) \to 0 \quad \mbox{ then } A(-\infty) \to 0 \ : \ \ \mbox{ Small BH }$

example:
$$g = e^{-\phi}$$

 $\phi = \frac{1}{2} \log \frac{A}{r^2} = \log \left(1 - \frac{2M}{r}\right) \to \infty \text{ at } r = r_h = 2M$
 $\tau = -\frac{1}{r-2M}$

Large field variations associated with weak coupling limits are confined near small regions in space and associated to small BHs

infinitely many nearly point objects?? 💆

The area receives corrections in string theory embeddings

We will see that they can lead to a violation of the Bekenstein bound, unless the EFT cutoff decreases as dictated by the SDC and WGC.

Entropy Bound:

A region of size L cannot have more entropy than a Schwarzschild black hole of the same area ${\cal A}=L^2$

The number of distinct BH states that fit in the box should not grow larger than L^2

This is violated if they are point-like, since we can then fit infinitely many. If the EFT breaks down, they will have an effective area dictated by the cut-off, thus solving the problem.

Goal: determine how the cut-off must behave to avoid violation of entropy bounds

The gradient of the scalar field diverges at the core for small black holes:

$$|d\phi|^2 = \tau^4 e^{2U} \dot{\phi}^2 \ge \frac{\Delta g^2 Q^2}{A^2} \to \infty$$

EFT breaks down whenever: $|d\phi|^2 = \tau^4 e^{2U} \dot{\phi}^2 \sim \Lambda^2$

Using
$$\dot{\phi}^2 \leq g^2 Q^2 e^{2U}$$
 and $A(\tau) = \frac{e^{-2U(\tau)}}{\tau^2}$
we get $\Lambda \leq g \frac{Q}{A}$

How many BH states fit in a box of size L?

In the microcanonical ensemble at energy $E \sim L$

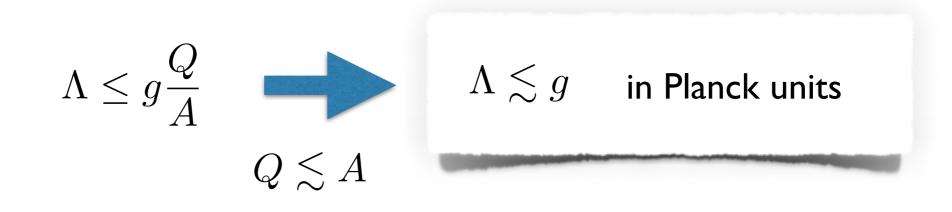
$$S = N_{\rm species}^{1/4} E^{3/4} L^{3/4} = N_{\rm species}^{1/4} L^{3/2}$$

At sufficiently weak coupling, any small black hole of charge Q effectively counts as an additional specie

(gravitational and gauge interactions become arbitrarily small)

$$N_{\rm species} = Q_{\rm max} \lesssim L^2 = A$$

To avoid violation with entropy bounds, EFT must break down at



This is precisely the cut-off dictated by the WGC!

- It supports a strong version of WGC since it requires the existence of infinitely many charged states becoming light (the local EFT description must break down)
- It makes quantitative the trouble with charged remnants for small gauge couplings (which didn't work for RN BHs)

It also provides a BH argument for the SDC:

EFT must break down by infinite many fields becoming massless at large field ranges associated to weak coupling points

If
$$g \sim e^{-a\phi}$$
 then $\Lambda \lesssim g \sim e^{-a\phi}$

This is the asymptotic behaviour for gauge couplings at infinite distance limits in string theory

Lamppost effect or fundamental reason?

Supported by Emergence Proposal (exponential behaviour emerges from integrating out tower of states)

[Heidenreich et al'17] [Palti,Grimm,IV'18]

Open question:

Any infinite distance limit corresponds to a weak coupling limit?

So far, in all string theory examples, there is a vanishing p-form gauge coupling asymptotically

• Proposed to be general in [Gendler,IV'20]

• Fits with Emergent String Conjecture [Lee,Lerche,Weigand'19] (either KK photon or B-field)

UV compactness and Emergence

Let us next argue that non-compact scalars are not allowed in QG regardless of having a gauge field theory.

Take a free scalar field theory and compactify to 1d:

$$\mathcal{L} = \frac{1}{2} \left(\partial_{\mu} \varphi \right)^2 \quad \Longrightarrow \quad H = \frac{1}{2} \hat{p}^2$$

Partition function diverges due to the continuum of eigenstates, unless the scalar field is compact (so the momenta spectrum is discrete)

$$Z = \sum_{n}^{E_n = \Lambda} e^{-\beta E_n} \simeq \frac{\phi_{\max}}{\sqrt{2\pi\beta}} \operatorname{erf}\left(\sqrt{\beta\Lambda}\right)$$

To keep partition function finite:

$$\Lambda\left(\phi_{\max}\right) \leq \frac{1}{\phi_{\max}^2} \quad \text{for} \quad \phi_{\max} \to \infty$$

UV compactness and Emergence

What about the exponential behaviour of the cut-off?

Emergence Proposal: the dynamics (all kinetic terms) emerge upon integrating out states up to QG cut-off

In particular, infinite distance emerges from integrating out an infinite tower of states up to species scale

$$N \sim \frac{1}{\Lambda^{d-2}} \qquad N = \frac{\Lambda}{\Delta m}$$

[Palti,Grimm,IV'18] [Heidenreich et al'18]

Quantum corrections
$$\delta g_{\phi\phi} \simeq \sum_{n=1}^{N} m_n^{d-4} (\partial_{\phi} m_n)^2 = \left(\frac{\partial_{\phi} \Delta m}{\Delta m}\right)^2$$
to field metric:

 $\Delta \phi \sim \int d(\log \Delta m) = \log \Delta m$ Masses behave exponentially!

UV compactness and Emergence

Emergence proposal assumes that the field space is compact in the UV, so the infinite distance is an IR artefact

Finiteness of partition function can be used to motivate this 'UV compactness'

Why this partition function should be finite?

- Associated to entropy of a black (d-1)-brane [Hamada, Vafa'20] [Bedroya et al'21] (generalization of finiteness of probe brane moduli space)
- Proposal: swampland conditions emerge from finiteness of quantum gravity amplitudes

Finiteness of Quantum Gravity Amplitudes

On the quest of a general underlying principle behind the swampland conjectures!

Finiteness of quantum gravity amplitudes (S-matrix elements, CFT correlators...)

EFT amplitudes can diverge, but not in the UV complete theory

Generalization of finiteness of probe brane moduli space [Hamada, Vafa'20] [Bedroya et al'21]

Finiteness of Quantum Gravity Vacua

Finiteness of QG amplitudes can be used to motivate finiteness of the string landscape:

- Compactify to 2d in arbitrary manifold. The wavefunction spreads over all topologies, so the partition function diverges if there are infinite many vacua.
- More concretely, the partition function of a scalar field probing all (infinitely many) vacua diverges.

Proposal:

The number of low energy EFTs (after quotienting by moduli spaces) consistent with quantum gravity that are valid (at least) up to a fixed finite energy cutoff is finite.

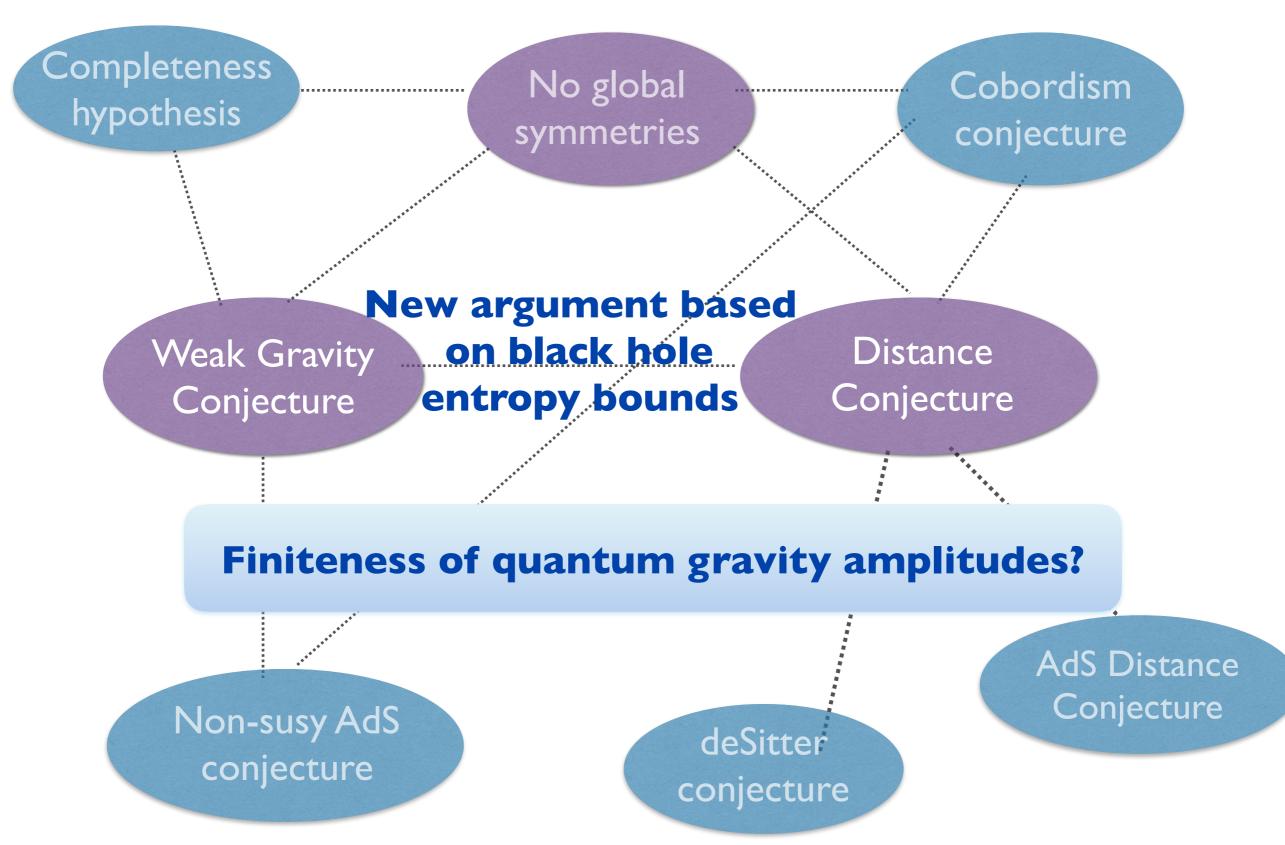
Finiteness of Quantum Gravity Vacua

The number of low energy EFTs (after quotienting by moduli spaces) consistent with quantum gravity that are valid (at least) up to a fixed finite energy cutoff is finite.

- It cuts-off the infinite distance tails of vacua asymptotically
- Infinite families of AdS vacua must come together with non-decoupled extra dimensions
- It fits with Cheeger's theorem: finite number of diffeomorphisms types of Riemenannian manifolds with bounded curvatures, volumes and diameters

see also [Archarya,Douglas'06] [Grimm'20]

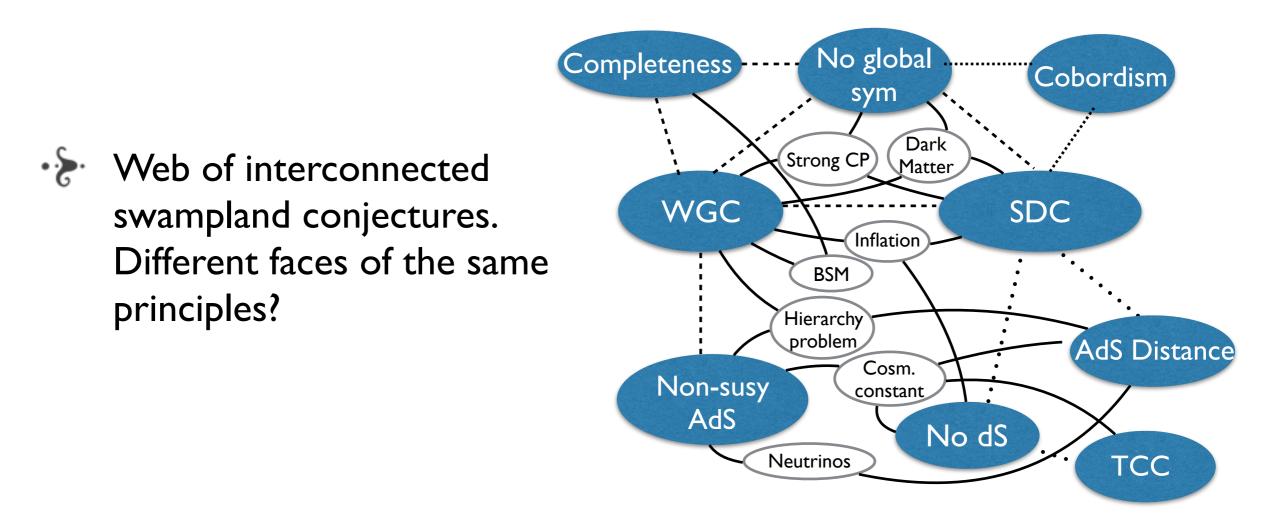
Conclusions



Thank you!

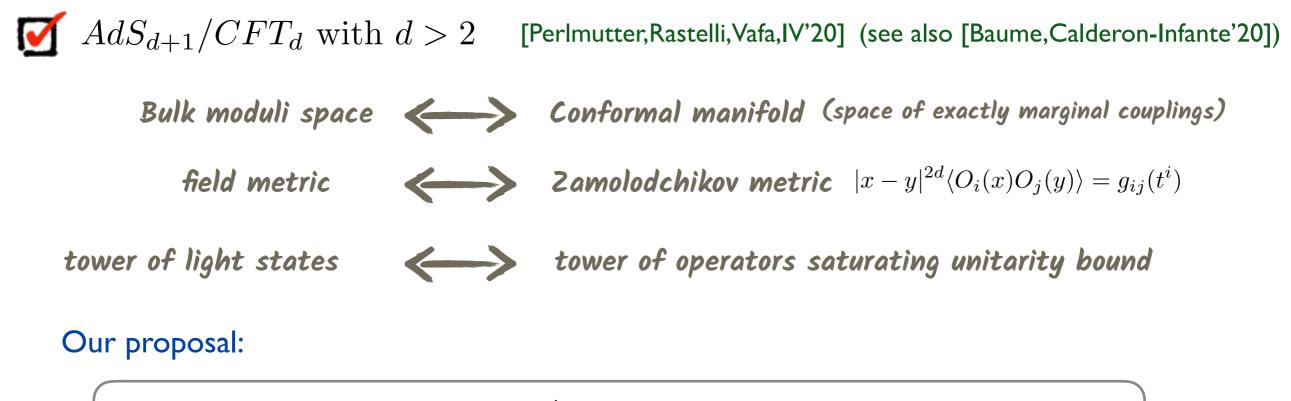
back-up slides

Consistency with quantum gravity can have important phenomenological implications. Not every EFT is allowed!

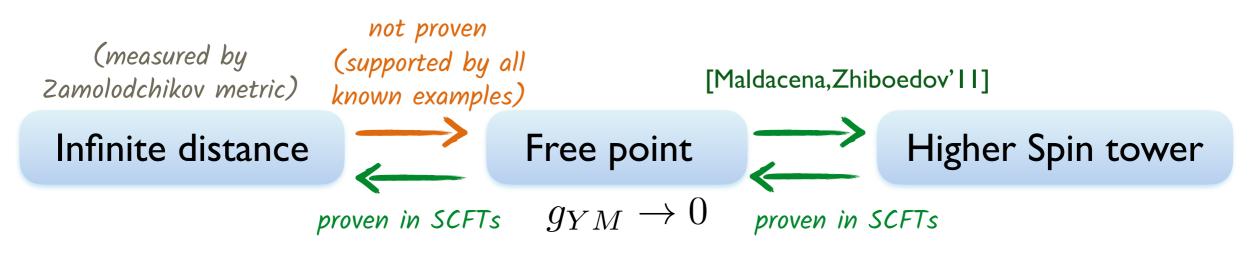


 Significant new evidence in favour of some conjectures in the past years from different research areas. Much more work to do!

CFT Distance Conjecture



 \exists tower of HS with $\gamma_J \sim e^{-\alpha d(\tau, \tau')}$ as $d(\tau, \tau') \to \infty$ in the conformal manifold



Consequence: 3d conformal manifolds are compact

CFT Distance Conjecture

 $\mathcal{O} AdS_{d+1}/CFT_d \text{ with } d > 2$ [Perlmutter,Rastelli,Vafa,IV'20] (see also [Baume,Calderon-Infante'20])

In the free limit $g_{YM} \to 0 \longrightarrow \mathcal{O}_{\tau} = \operatorname{Tr}(F^2 + \dots)$

By perturbation theory:

$$ds^2 = \beta^2 \frac{d\tau d\bar{\tau}}{(\mathrm{Im}\tau)^2} \quad \text{as} \quad \mathrm{Im}\tau \to \infty \qquad \qquad \beta^2 = 24 \, \dim G$$

If there is a weakly coupled AdS dual, it implies a stronger version of SDC:

Infinite distance limits at fixed AdS₅ radius Lower bound for α ! Tower of higher spin fields with an exponential rate: $\alpha = \sqrt{\frac{2c}{\dim G}} \stackrel{\geq}{=} \frac{1}{\sqrt{3}} \quad \text{for 4d N=2}$ $\geq \frac{1}{2} \quad \text{for 4d N=1}$

SDC in 4d N=I EFTs

 There could be other towers of states getting light, but the leading one scales like

$$m_*^2 \simeq M_{\rm P}^2 A \left(\frac{T}{M_{\rm P}^2}\right)^w$$

for some positive integer $w = 1, 2, \ldots$

T= string tension

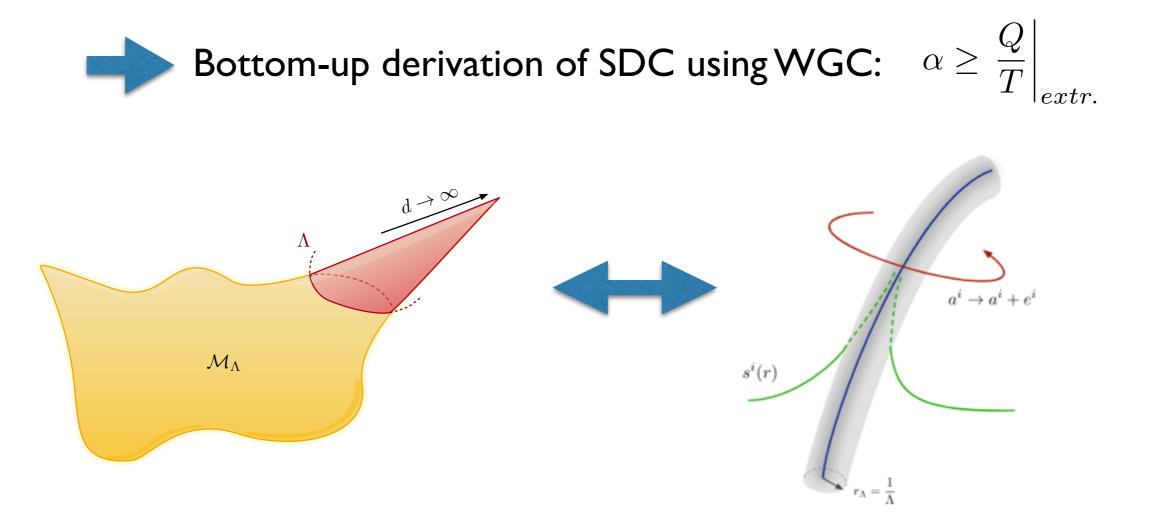
In all analysed string theory examples: w = 1, 2, 3 ??

dualities?

SDC in 4d N=I EFTs

2) Distant Axionic String Conjecture:

All infinite distance limits in 4d EFTs can be realised as RG flow endpoints of an axionic EFT string



Same philosophy than [Klaewer, Palti'16], [Draper, Farkas'19]

What happens in the presence of a potential?

Everything holds as long as the energy scale remains below the cut-off (so the infinite distance is not obstructed by the potential)

 $W = W_{\text{flux}}(\phi) + \mathcal{O}(e^{2\pi i m_i t^i})$

EFT strings still get tensionless inducing the EFT breakdown, but they get attached to membranes

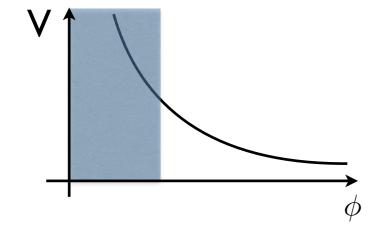
We can translate properties of the flux potential to the membranes:

$$T_{\rm mem} = 2M_p^3 e^{K/2} |W(q)|$$

$$Q^2 = 2V(q) \qquad \Longrightarrow \qquad \|\partial T_{\rm mem}\|^2 - \frac{3}{2}T_{\rm mem}^2 = M_{\rm P}^2 Q_{\bf q}^2$$

They induce a runaway for the scalar potential

[Lanza, Marchesano, Martucci, IV'20]



- It follows from a membrane saturating the WGC
- Asymptotic version of de Sitter conjecture [Obied et al'18]

[Ooguri et al'18]

 Tests in string theory (classical no-go's) [Hertzberg et al'07] [Wrase et al'10]... [Grimm,Li,IV'19]