

# Models and Ecological Data

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# Mt Rundle Hike





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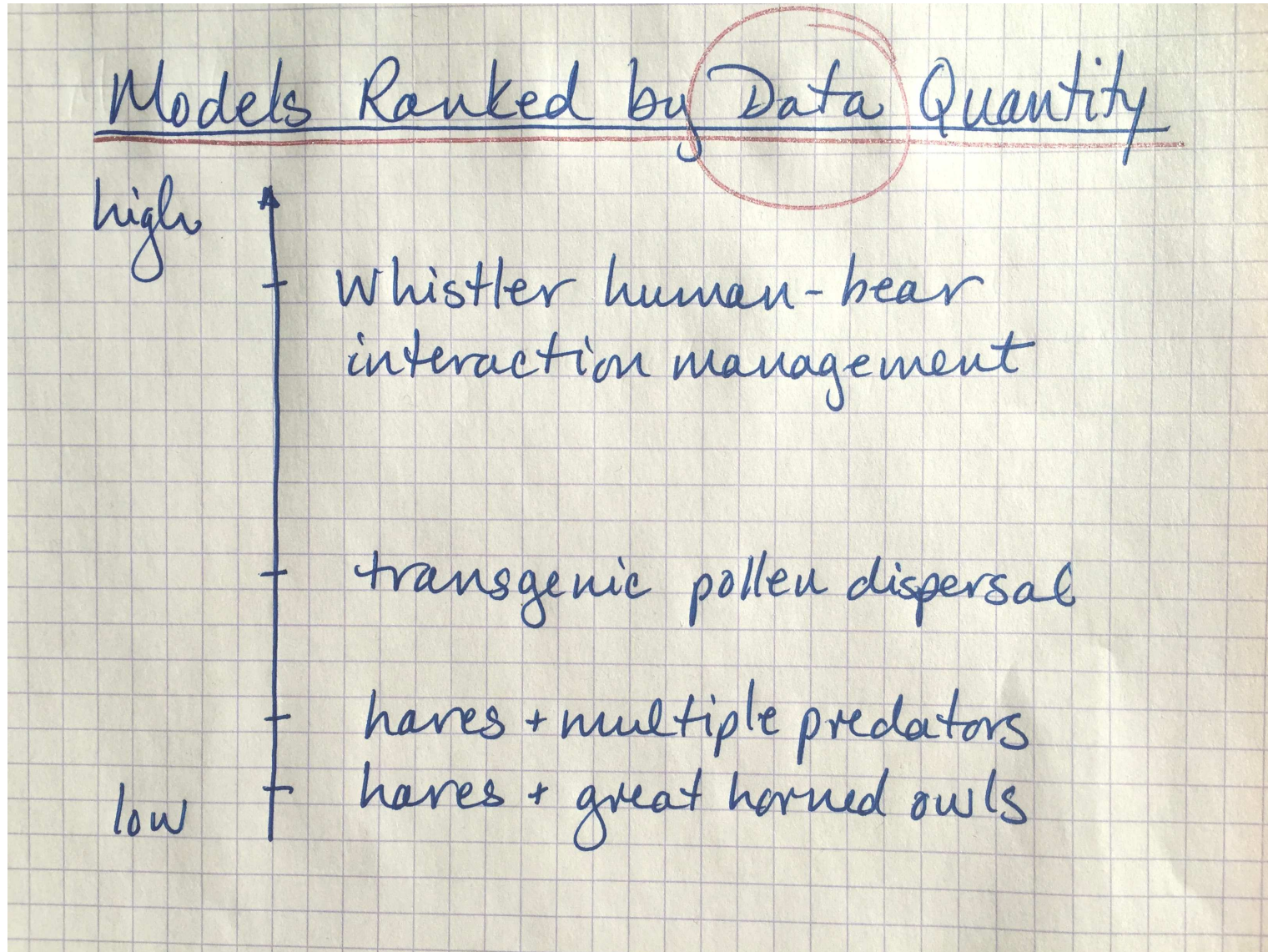


# Mt Rundle Hike





# Models Ranked by Data



# 1. Whistler HBI Management

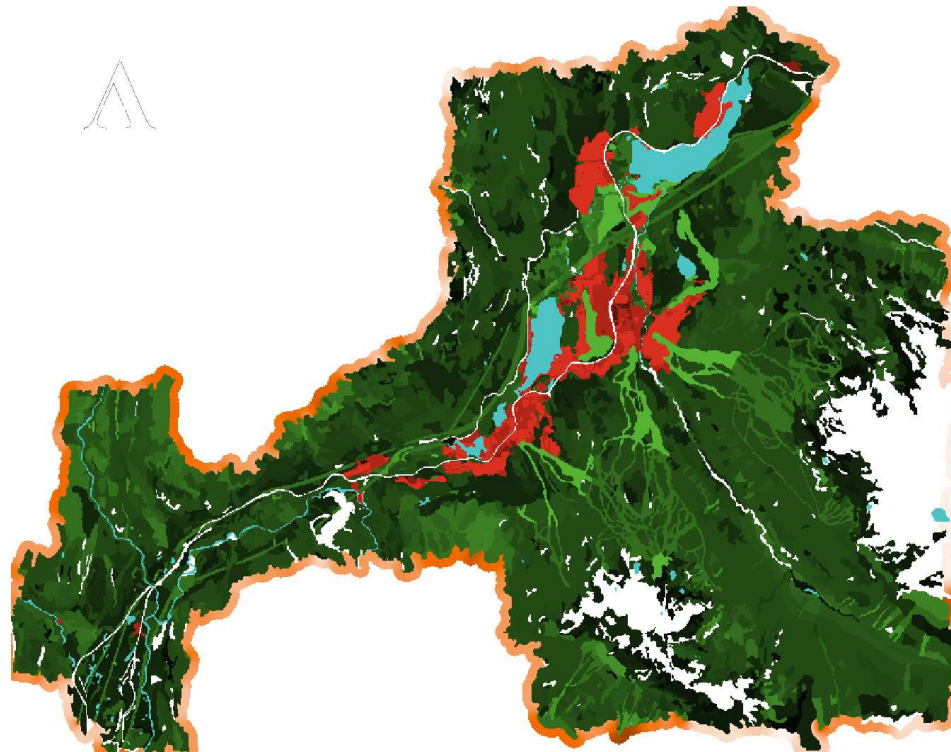
**Research Question:** Which management options will have the greatest effect at reducing HBI in Whistler?

**Data:**

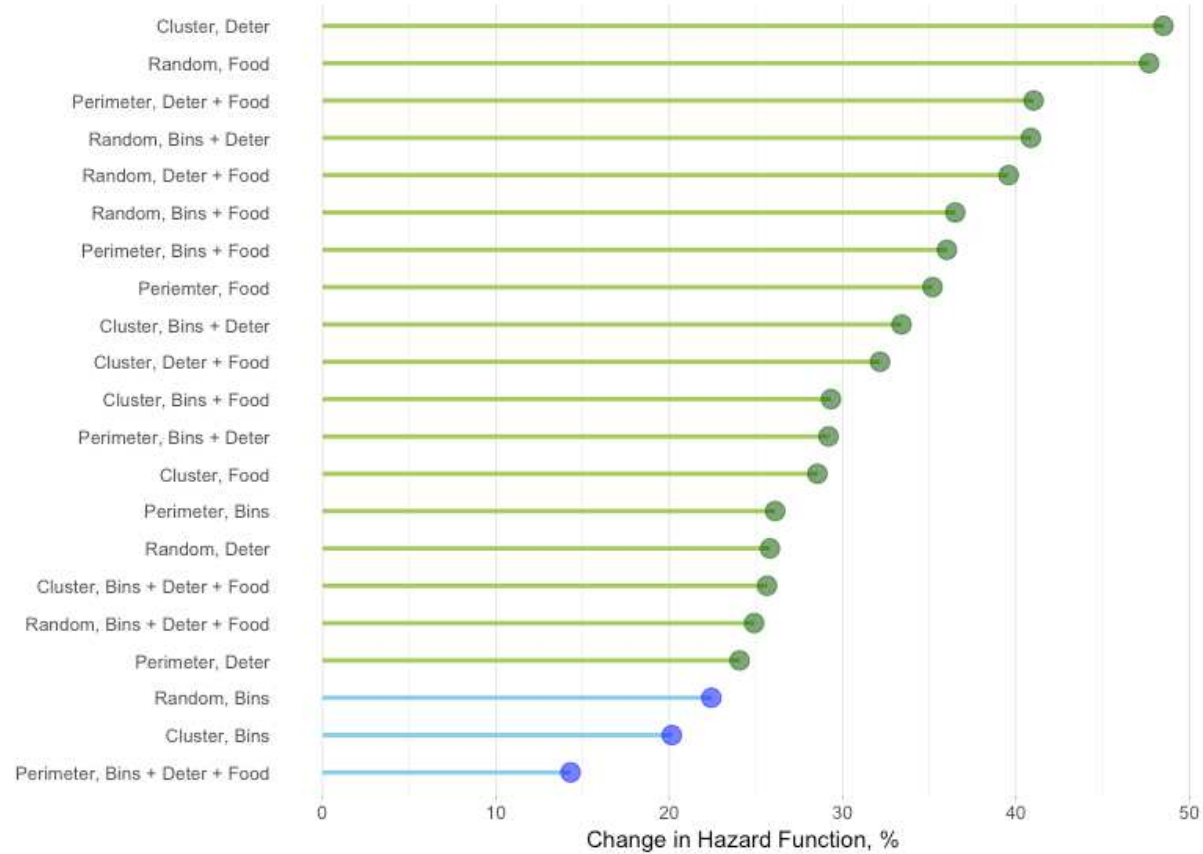
- GPS data from 9 collared bears
- vegetation maps
- urban zoning maps

**Model:**

- ABM



# Results



**Impact:** new approach → proof of concept

Marley et al (2019) Ecological Modelling

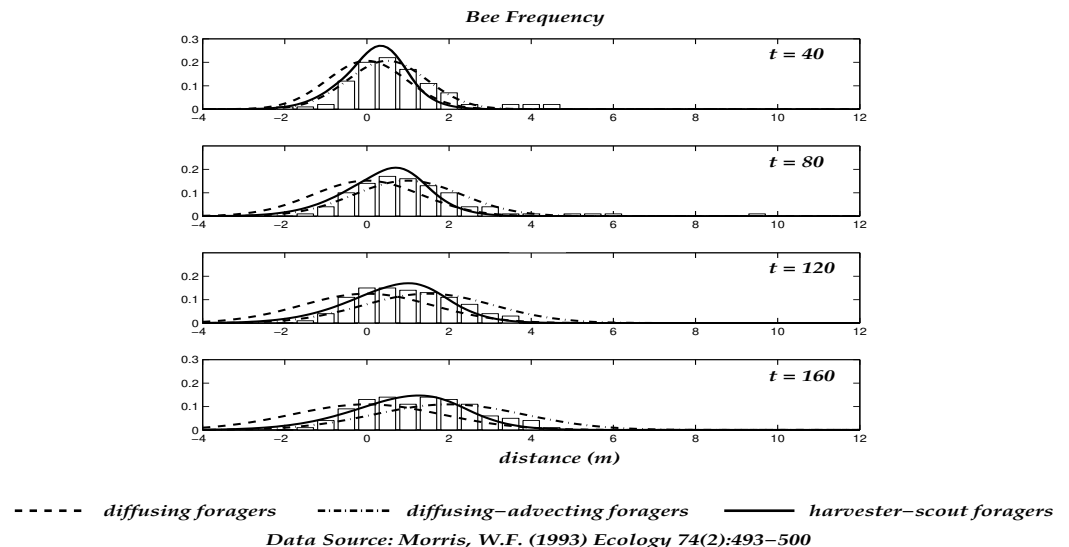
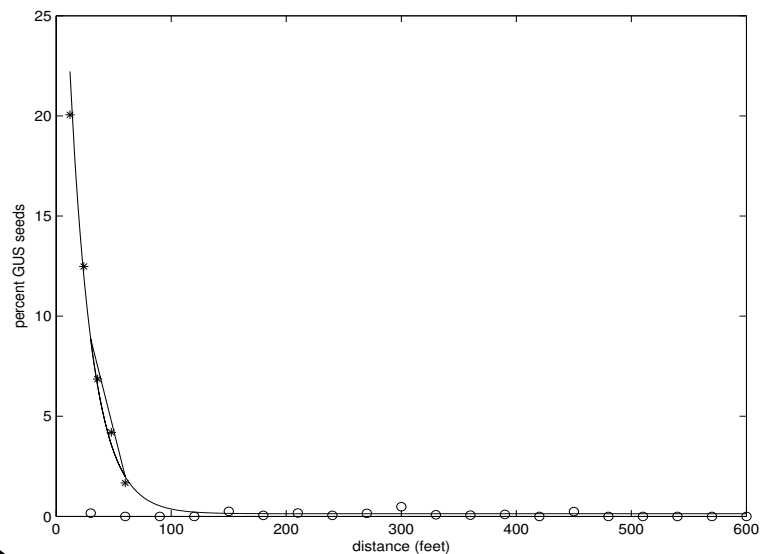
# 2. Transgenic Pollen Dispersal

**Research Question:** How far will bee-transported transgenic pollen disperse?

- I) honey bee dispersal
- II) pollen dispersal

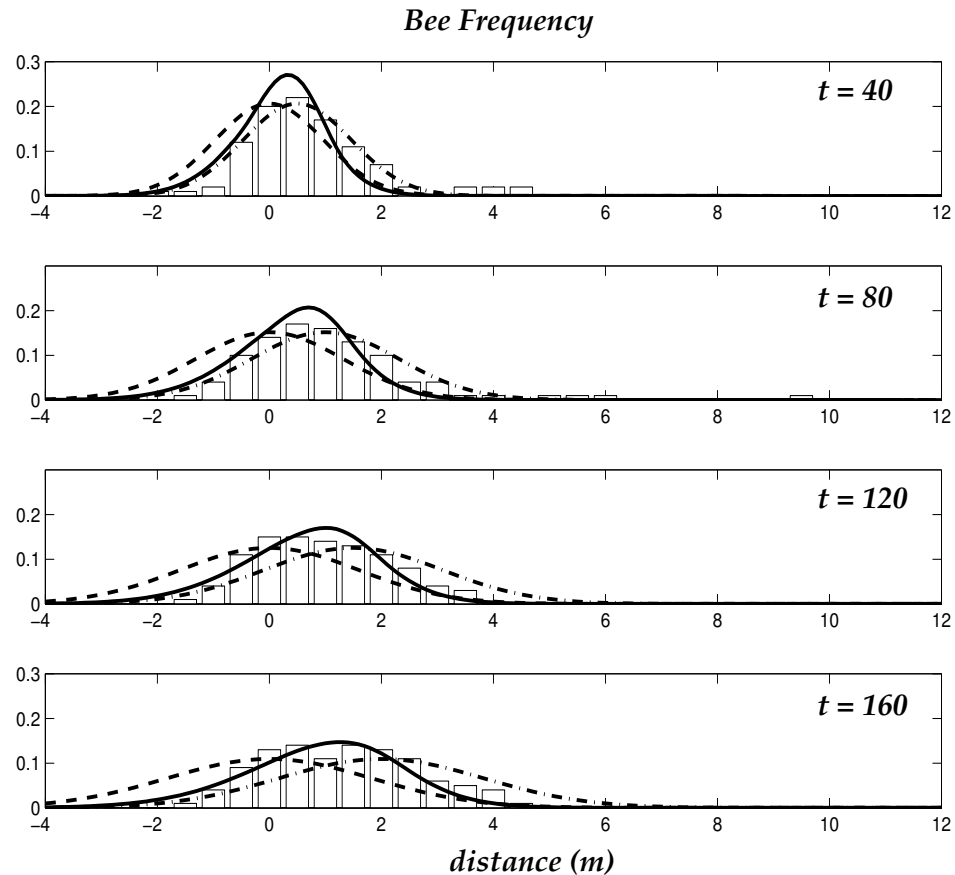
**Data:**

- percent transgenic seed as a function of distance
- honey bee dispersal over time
- flight speed





# Validation



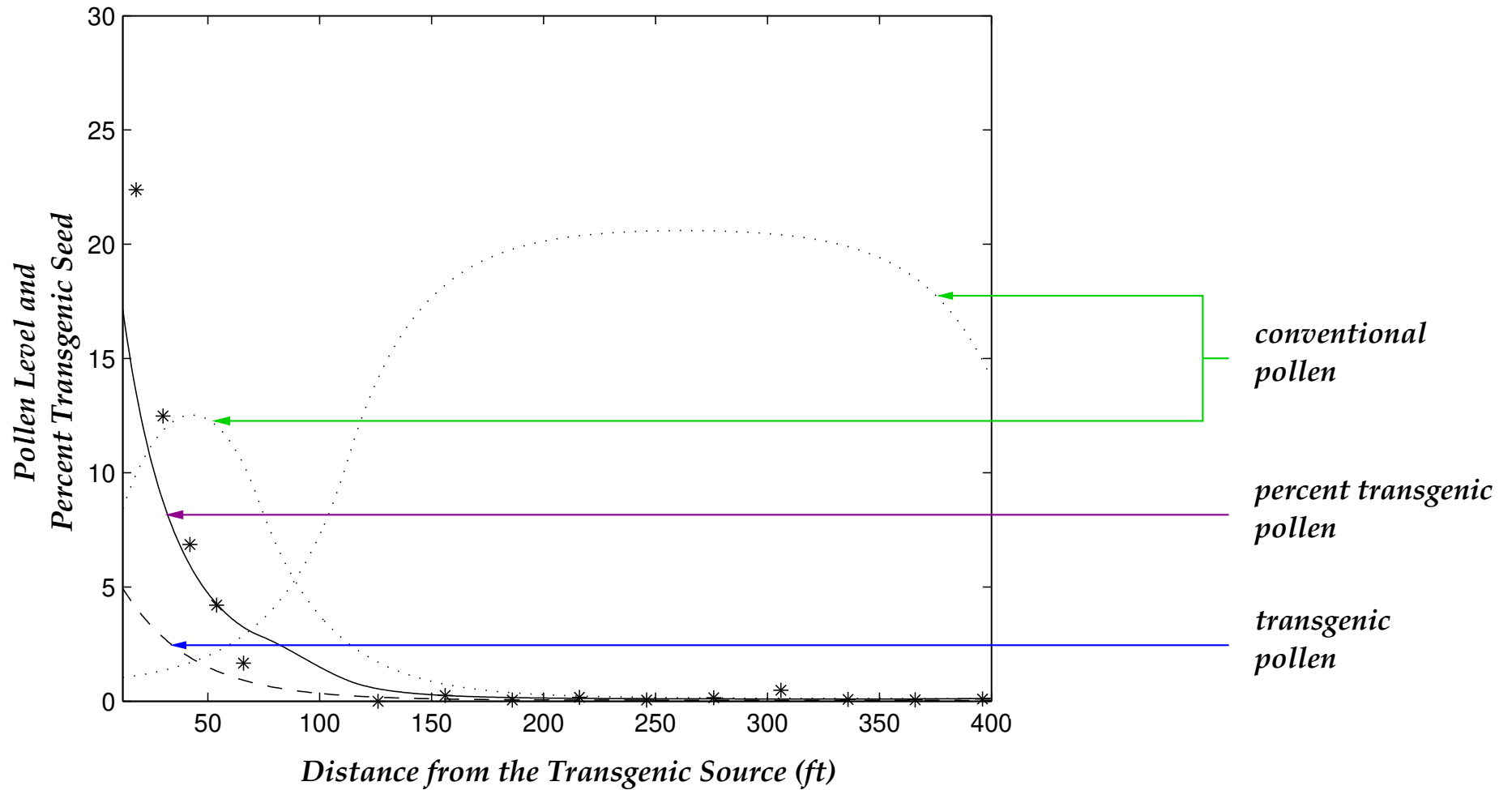
----- *diffusing foragers*    - · - · - · *diffusing-advecting foragers*    — *harvester-scout foragers*

*Data Source: Morris, W.F. (1993) Ecology 74(2):493-500*

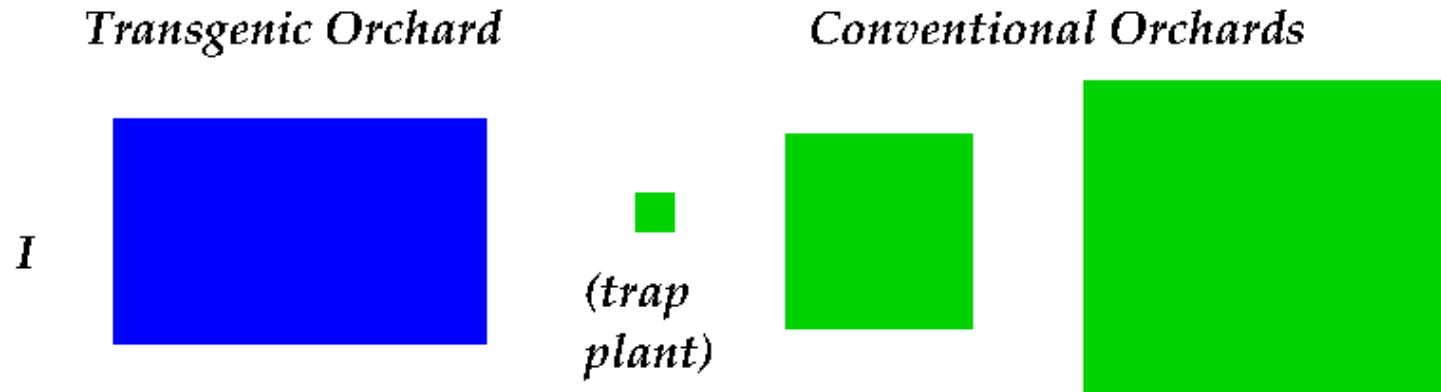
AIC used for formal validation

Tyson, Wilson & Lane, (2011) Theoretical Population Biology

# Validation



# Results



Relative Size of Conventional Orchard	Isolation Distance Required (ft)	
	0.9% outcrossing	0.1% outcrossing
Trap	1829	3679
0.5	60	1510
1.0	50	1410
2.0	30	1320

**Impact:** GMO apple approved for planting in Canada



# 3. Hares + Multiple Specialists

**Research Question:** What drives the hare minima to the very low levels observed in the boreal forest? *Hypothesis: Multiple specialist predators.*

## Data:

- Kluane study: 1 full cycle (1 data point per year)
  - ◆ parameter values
  - ◆ functional responses: lynx, coyote, great horned owl
- parameter values
- cycle properties (period, lag, max, min)

## Model:

$$\text{hare (prey):} \quad \frac{dN}{dt} = rN \left( 1 - \frac{N}{k} \right) - \sum_{i=1}^n \frac{\alpha_i N P_i}{N + \mu_i}$$

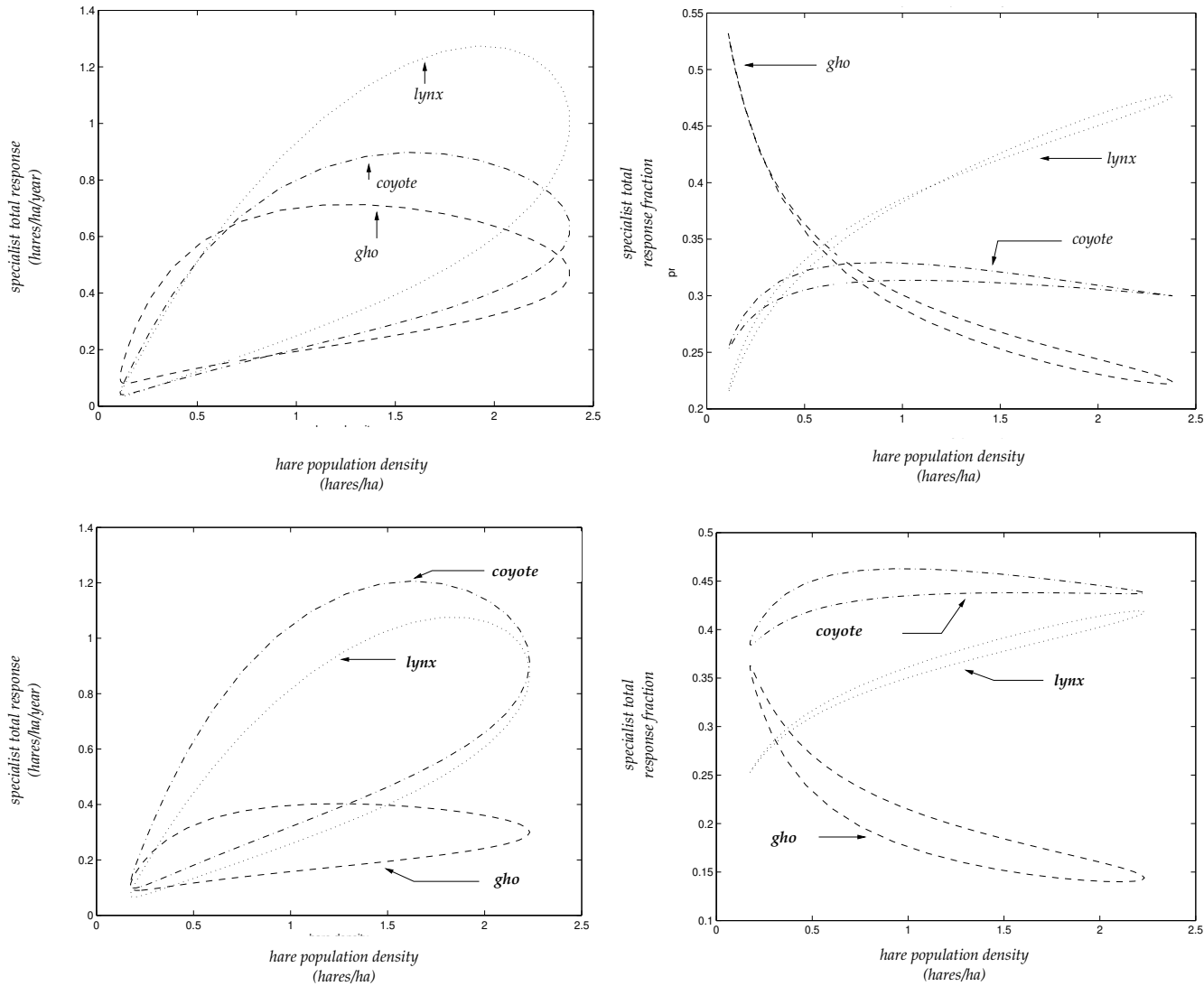
$$\text{specialist predator:} \quad \frac{dP_i}{dt} = s P_i \left( 1 - \frac{q_i}{N} P_i \right)$$

Tyson, Haines, & Hodges (2010) Theoretical Ecology

# Fit to the Data

Probe		<i>Basic Model</i>				<i>LC &amp; LG Models</i>		<i>LCG Model</i>
		l	l:c	l:g	l:c:g	l&c	l&g	l,c&g
hare density (/ha)	max	✓	✓	×	✓	✓	✓	✓
	min	×	×	×	×	×	×	✓
pred. complex density (/100 km <sup>2</sup> )	max	–	×	×	✓	–	–	–
	min	–	×	×	✓	–	–	–
lynx density (/100 km <sup>2</sup> )	max	×	–	–	–	×	×	✓
	min	×	–	–	–	×	×	✓
coyote density (/100 km <sup>2</sup> )	max	–	–	–	–	×	–	✓
	min	–	–	–	–	×	–	✓
owl density (/100 km <sup>2</sup> )	max	–	–	–	–	–	✓	✓
	min	–	–	–	–	–	✓	✓
predator lag (years)	l	✓	✓	✓	✓	✓	✓	✓
	c	–	–	–	–	✓	–	✓
	g	–	–	–	–	–	✓	✓
period (years)		✓	✓	✓	✓	✓	✓	✓

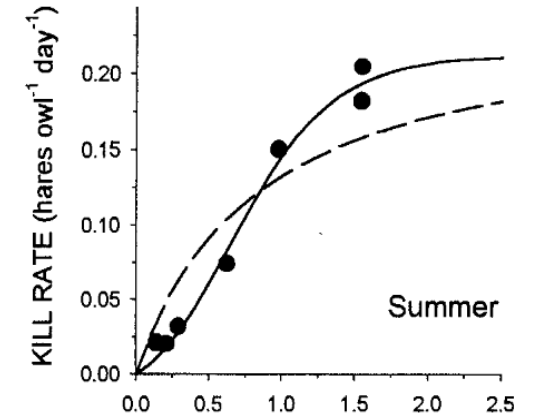
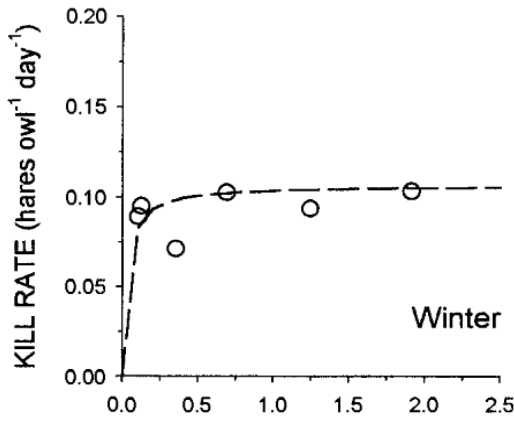
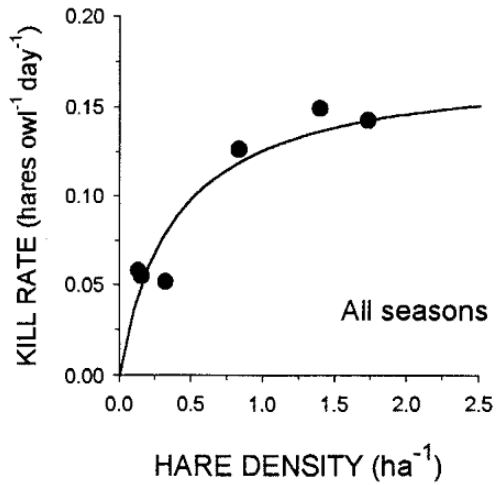
# Results: Predator Comparison



**Impact:** Understanding the role of avian predators



# 4. Seasonal Specialist



Krebs, et al. *Ecosystem Dynamics of the Boreal Forest: The Kluane Project*. 2001



photo credit: R. Lalonde

# Hare and Great Horned Owl

**Research Question:** If the predator functional response is generalist in one season and specialist in the other, what behaviours do we find in the predator-prey system?

## Data:

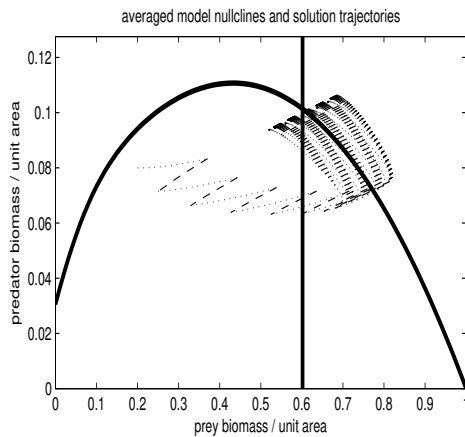
- Kluane study: 1 full cycle (2 data points per year)
  - ◆ parameter values
  - ◆ great horned owl summer and winter functional responses
- parameter values

**Model:** The averaged model worked well:

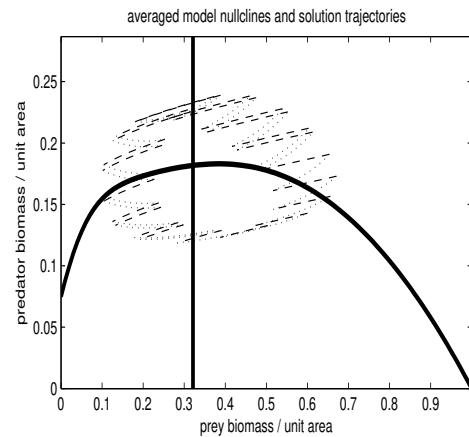
$$\begin{aligned}\frac{dn}{d\tau} &= T_s \left[ n(1-n) - \frac{n^2 p}{b^2 + n^2} \right] + (1 - T_s) \left[ -\frac{\alpha n p}{\beta + n} \right] \\ \frac{dp}{d\tau} &= T_s \left[ \gamma \frac{n^2 p}{b^2 + n^2} + s \frac{p}{1 + \nu p} - m p \right] + (1 - T_s) \left[ \gamma \frac{\alpha n p}{\beta + n} - \mu p \right].\end{aligned}$$

Tyson & Lutscher (2016) American Naturalist

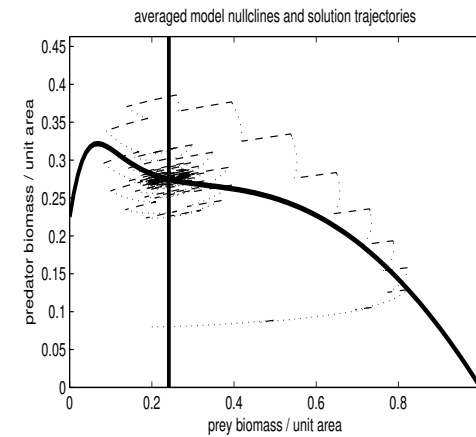
# Results



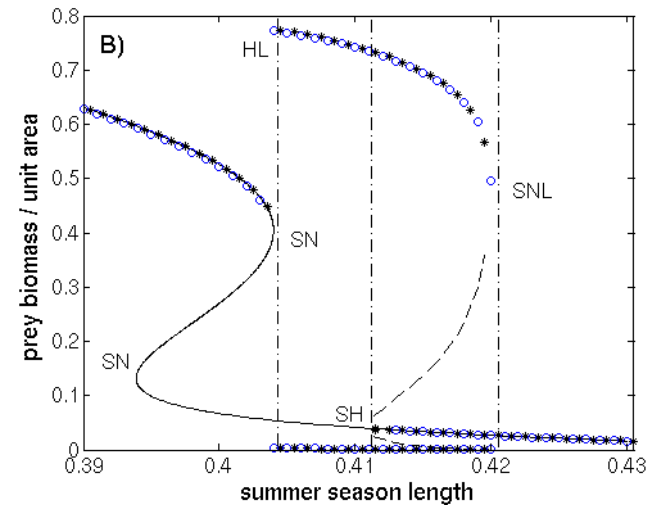
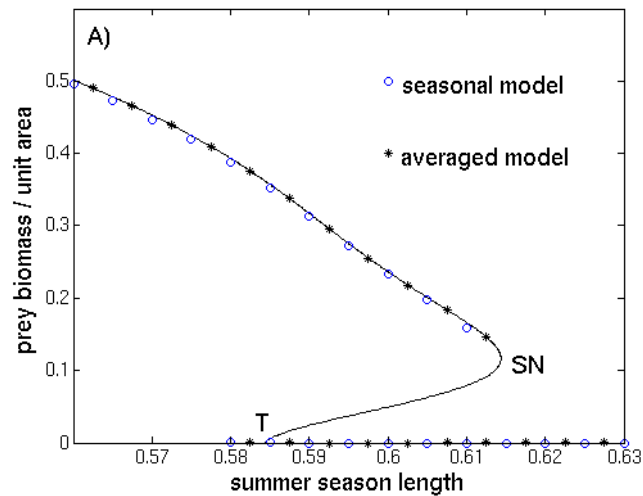
(a)  $T_s = 0.55$



(a)  $T_s = 0.75$



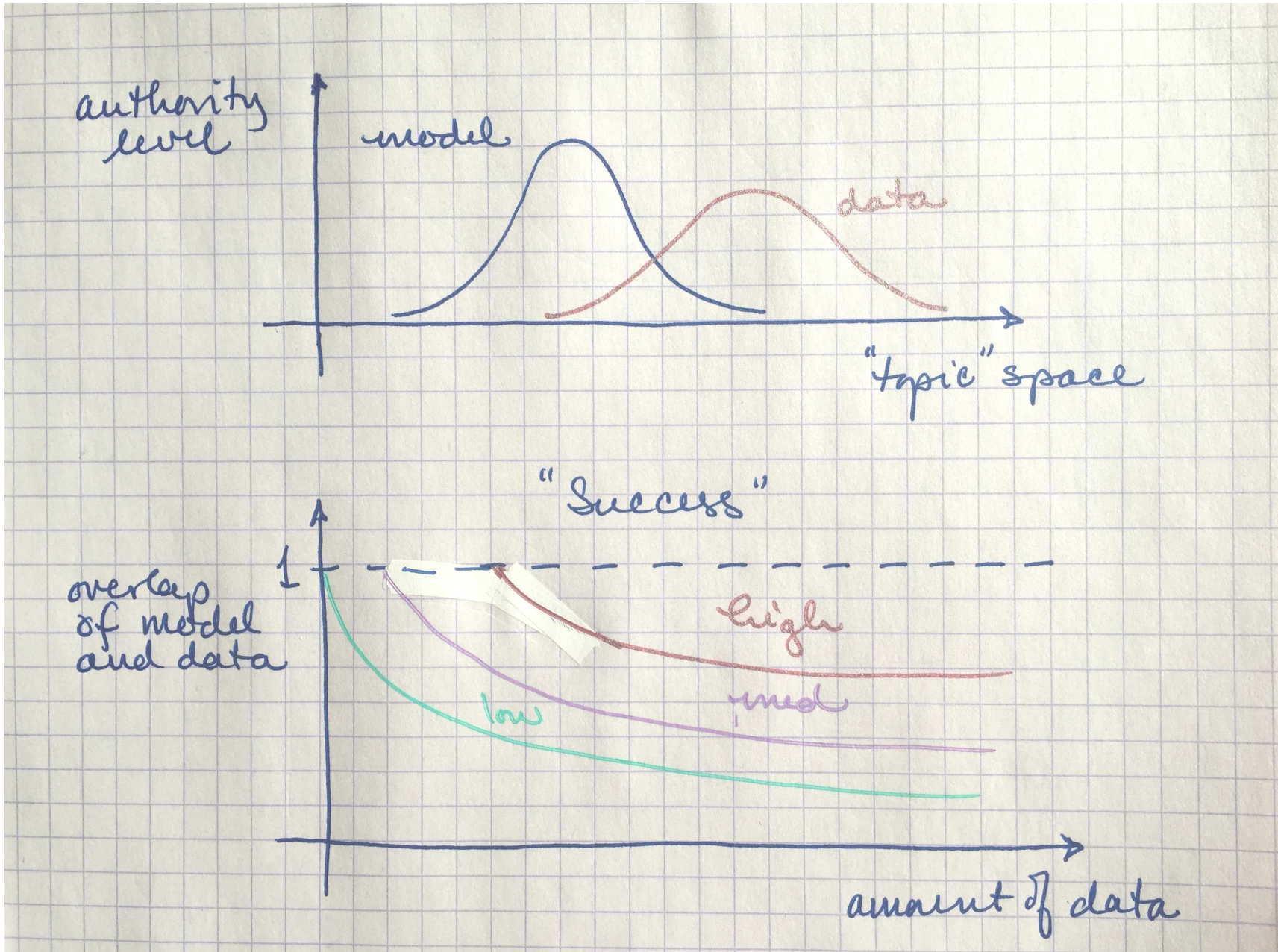
(a)  $T_s = 0.9$



**Impact:** Theory - successful use of averaging, need for seasonal data for functional responses



# Overlap of Models and Data





# Many Thanks

## ■ Researchers

- ◆ Tony Hamilton
- ◆ Susan E. Senger
- ◆ Lael Parrott
- ◆ W. David Lane
- ◆ Eric Deleersnider
- ◆ Emmanuel Hanert
- ◆ Karen Hodges
- ◆ Frithjof Lutscher



## ■ Students

- ◆ Jessa Marley
- ◆ Joseph Salkeld
- ◆ J. Ben Wilson
- ◆ Valentin Vallaeys
- ◆ Sheena Haines



# Movement Model

$$\begin{array}{l}
 \text{harvesters} \\
 \underbrace{\frac{\partial H}{\partial t}} \\
 = \underbrace{D \frac{\partial^2 H}{\partial x^2}}_{\text{diffusion}} - \underbrace{\gamma_1 H}_{\text{switch to scouting}} + \underbrace{\gamma_2 (S_l + S_r)}_{\text{switch from scouting}}
 \end{array} \quad (1a)$$

$$\begin{array}{l}
 \text{right-moving scouts} \\
 \underbrace{\frac{\partial S_r}{\partial t}} \\
 = \underbrace{-v \frac{\partial S_r}{\partial x}}_{\text{advection}} + \underbrace{\gamma_1 \left( \frac{H}{2} \right)}_{\text{switch from harvesting}} - \underbrace{\gamma_2 S_r}_{\text{switch to harvesting}}
 \end{array} \quad (1b)$$

$$\begin{array}{l}
 \text{left-moving scouts} \\
 \underbrace{\frac{\partial S_l}{\partial t}} \\
 = \underbrace{v \frac{\partial S_l}{\partial x}}_{\text{advection}} + \underbrace{\gamma_1 \left( \frac{H}{2} \right)}_{\text{switch from harvesting}} - \underbrace{\gamma_2 S_l}_{\text{switch to harvesting}}
 \end{array} \quad (1c)$$

Tyson, Wilson & Lane, (2011) Theoretical Population Biology

# Pollen Dispersal Model

diffusing pollen

$$\frac{\partial P_d}{\partial t} = \overbrace{D \frac{\partial^2 P_d}{\partial x^2}}^{\text{diffusion}} + \boxed{\overbrace{\alpha F(x) - \beta P_d}^{\text{production \& decay}}} - \overbrace{\gamma(P_d - P_r - P_l)}^{\text{movement mode switching}} \quad (2a)$$

right-moving pollen

$$\frac{\partial P_r}{\partial t} = \overbrace{-v \frac{\partial P_r}{\partial x}}^{\text{rightward advection}} + \overbrace{\gamma \left( \frac{P_d}{2} - P_r \right)}^{\text{movement mode switching}} \quad (2b)$$

left-moving pollen

$$\frac{\partial P_l}{\partial t} = \overbrace{v \frac{\partial P_l}{\partial x}}^{\text{leftward advection}} + \overbrace{\gamma \left( \frac{P_d}{2} - P_l \right)}^{\text{movement mode switching}} \quad (2c)$$

stationary pollen

$$\frac{\partial P_s}{\partial t} = \boxed{\overbrace{\beta P_d}^{\text{deposition}}} \quad (2d)$$

Tyson, Wilson & Lane, (2011) Ecological Modelling



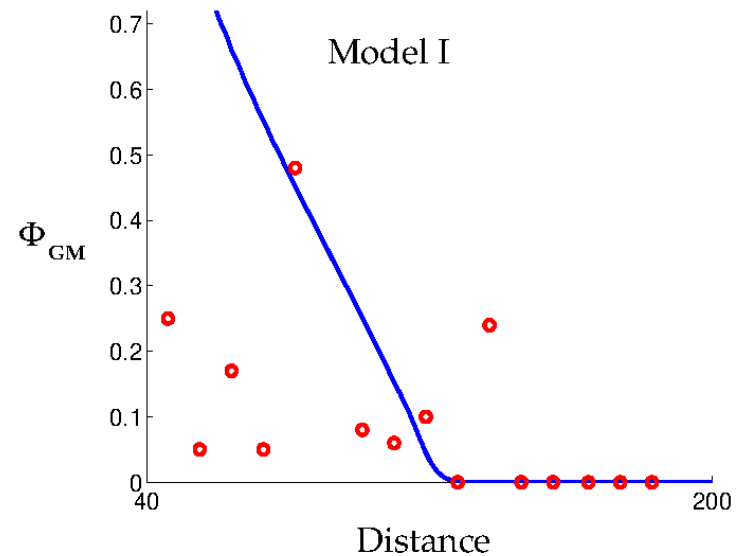
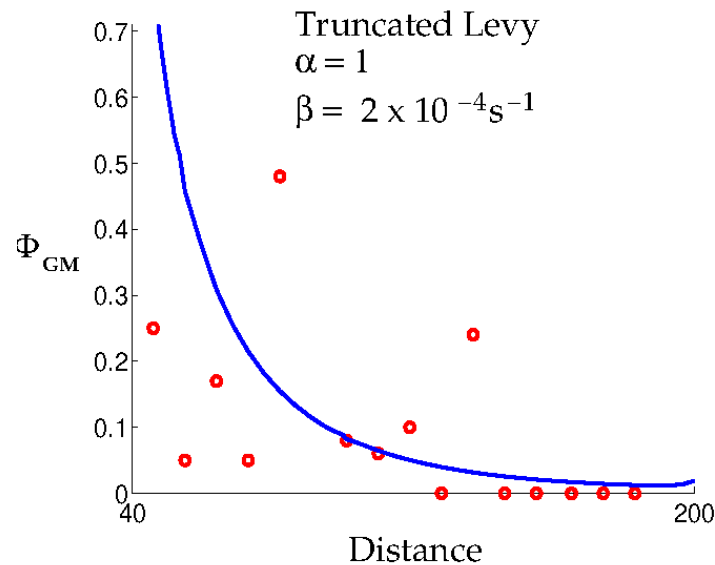
# Another Approach

## Truncated Levy vs Harvester-Scout (Model I)

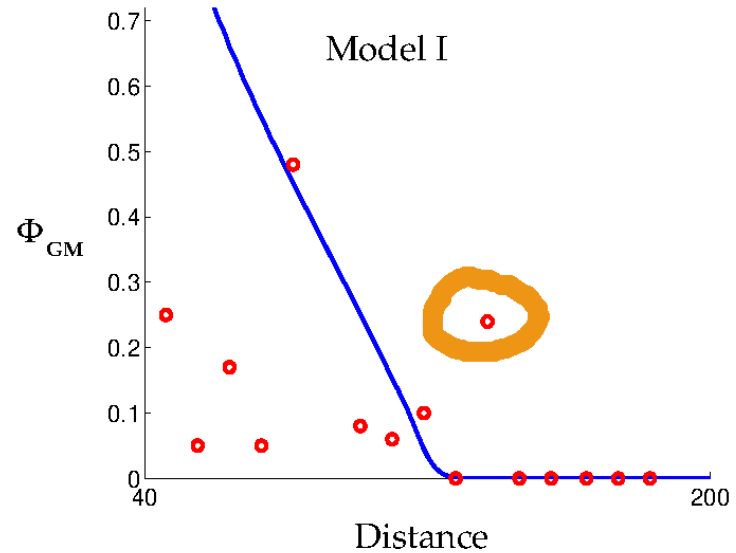
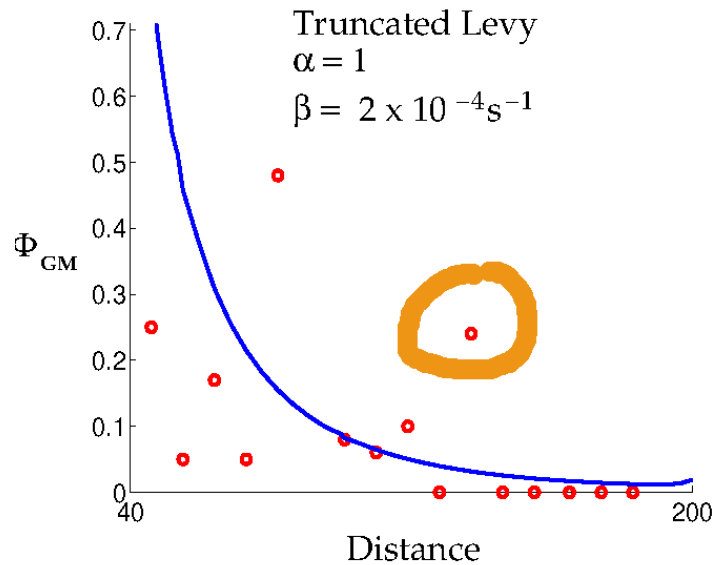
motile pollen: 
$$\frac{\partial P_m}{\partial t}(x, t) = K_\alpha \partial_x^{\alpha, \lambda} P_m(x, t) + F(x, t) - \beta P_m(x, t)$$

stationary pollen: 
$$\frac{\partial P_s}{\partial t}(x, t) = \beta P_m(x, t)$$

## Fit to the Tail



# Key Data in the Tail



Relative Size of Conventional Orchard	Isolation Distance Required (m)	
	Harvester-Scout	Truncated Levy
0.5	18	88
1.0	15	72
2.0	9	51

# Results: Predator Comparison

Define

$$\text{Total Response}_i = TR_i = \frac{\alpha_i N P_i}{N + \mu_i}$$

$$\text{Total Response Fraction}_i = \Phi_i = \frac{\text{Total Response}_i}{\sum_{j=1}^3 \text{Total Response}_j}$$

where

- Total Response<sub>*i*</sub> = density of hares killed per year by  $P_i$
- Total Response Fraction<sub>*i*</sub> = fraction due to  $P_i$  of total density of hares killed