

# *Helfrich-Hurault-like undulations in cholesteric liquid crystals induced by anchoring transitions*

*from M.O. Lavrentovich & L. Tran,  
Phys. Rev. Research  
(2020) 2:023128*

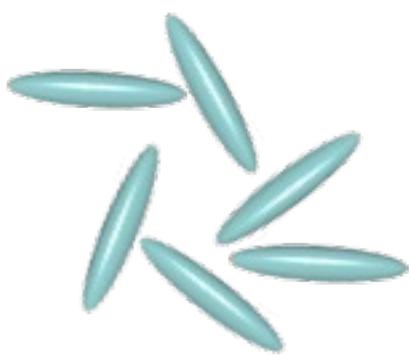
Lisa Tran – [l.tran@uu.nl](mailto:l.tran@uu.nl)  
*Utrecht University*



*BIRS*  
October 2022

# Liquid crystals - Basics

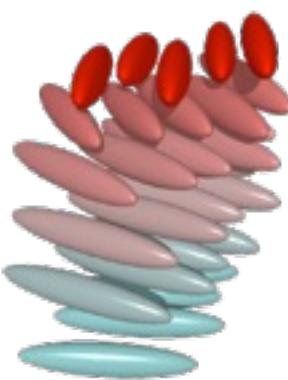
L. Tran



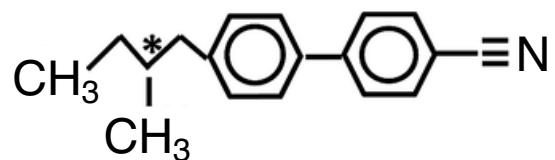
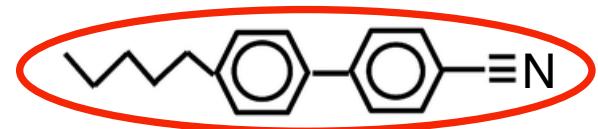
isotropic



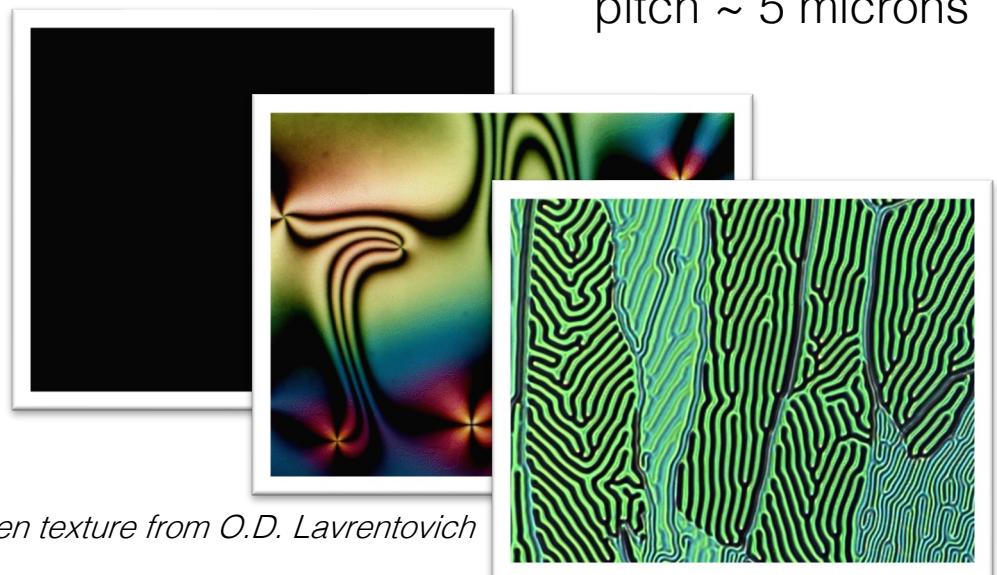
nematic



cholesteric



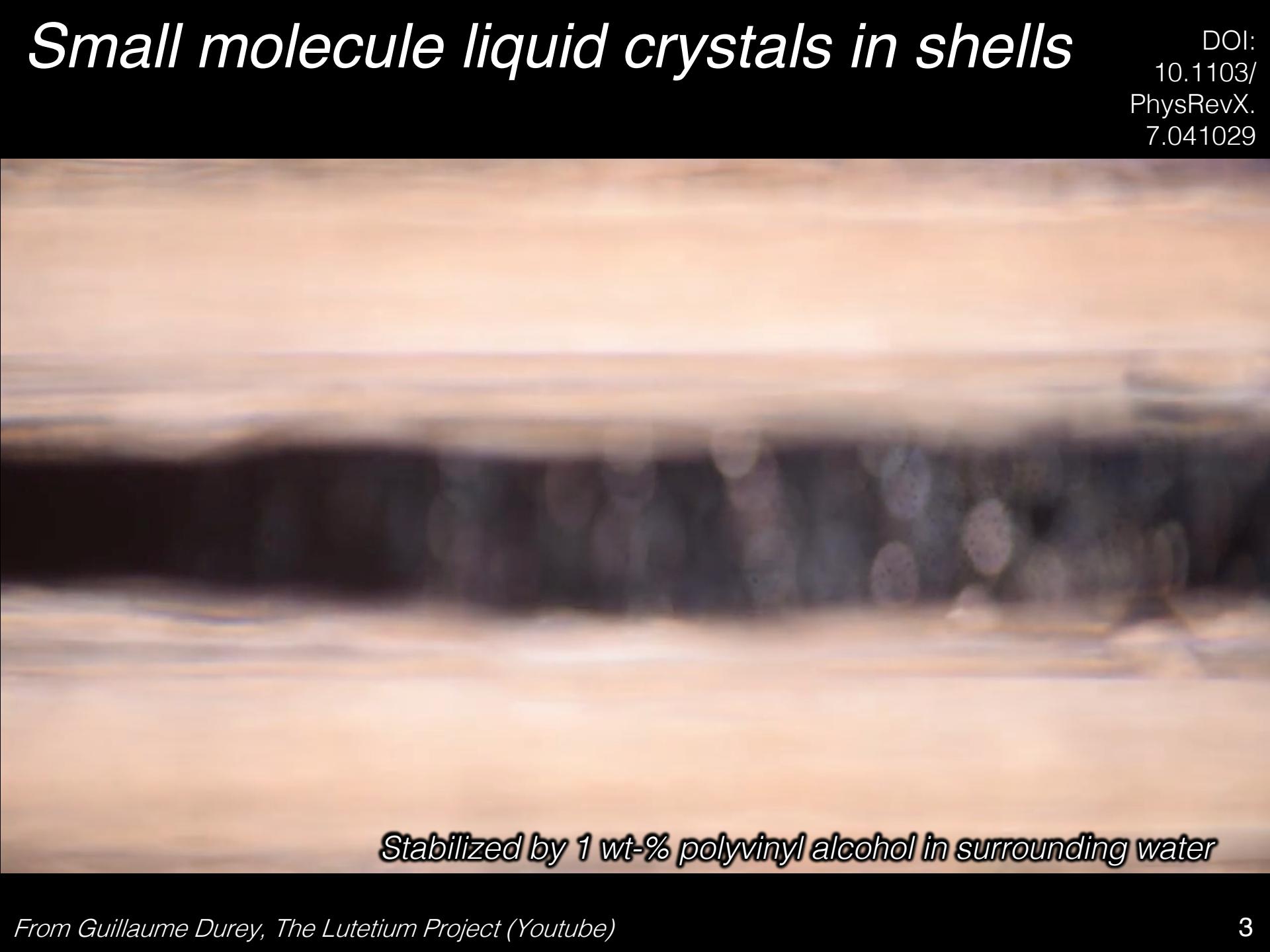
2.8 wt-% CB15  
pitch ~ 5 microns



Schlieren texture from O.D. Lavrentovich

# *Small molecule liquid crystals in shells*

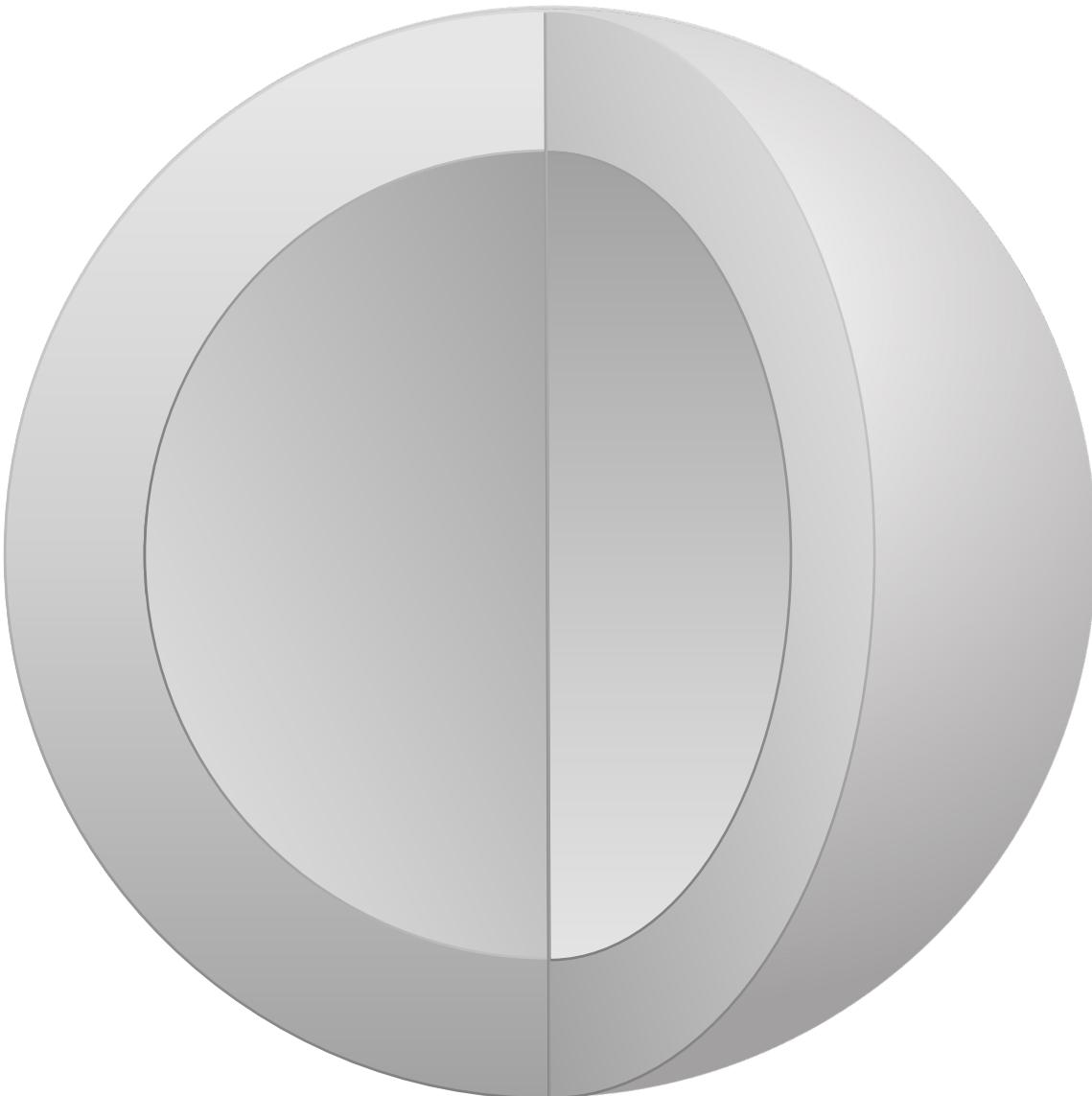
DOI:  
10.1103/  
PhysRevX.  
7.041029



*Stabilized by 1 wt-% polyvinyl alcohol in surrounding water*

# *Shells of cholesterics*

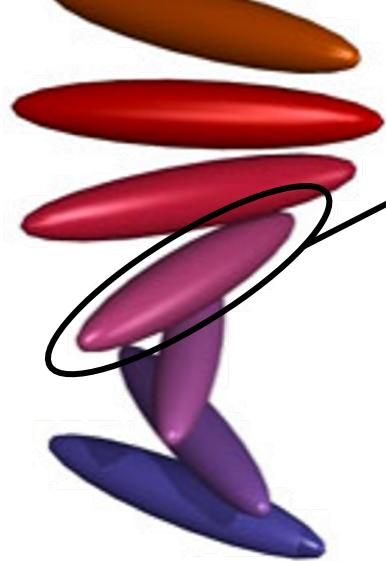
*L. Tran*



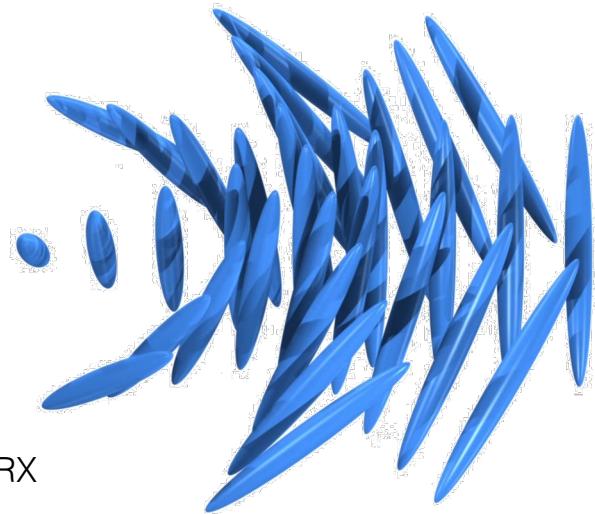
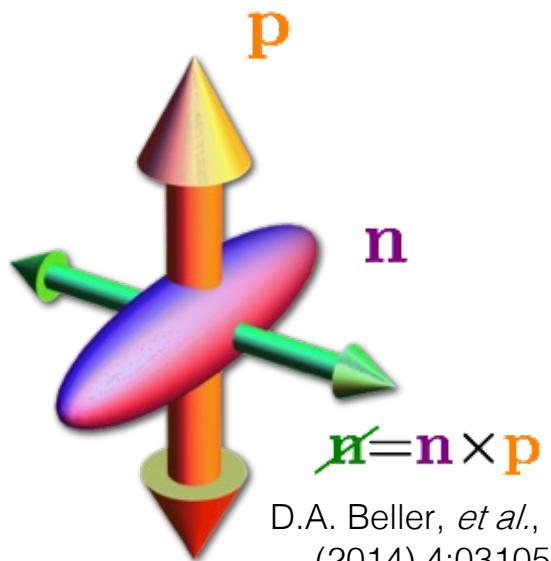
*Control  
bulk  
structure  
through  
surface  
geometry  
and  
anchoring*

# Cholesteric defects

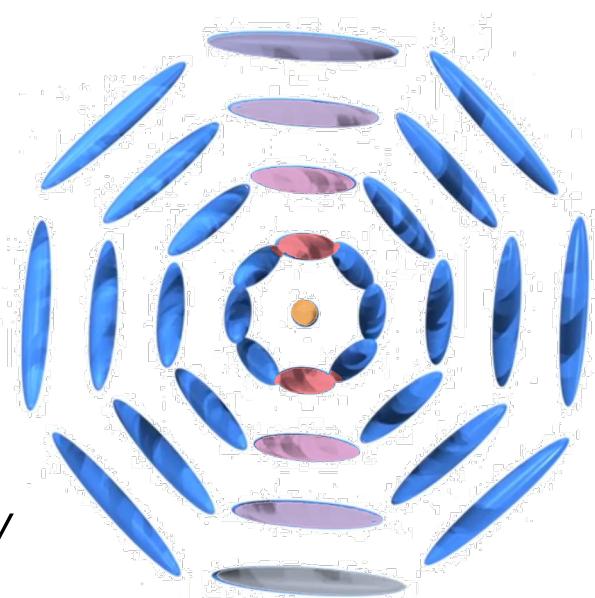
L. Tran



top view



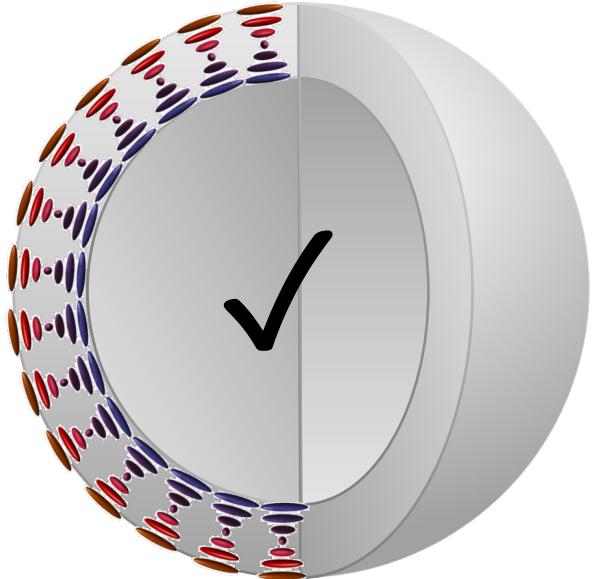
side view



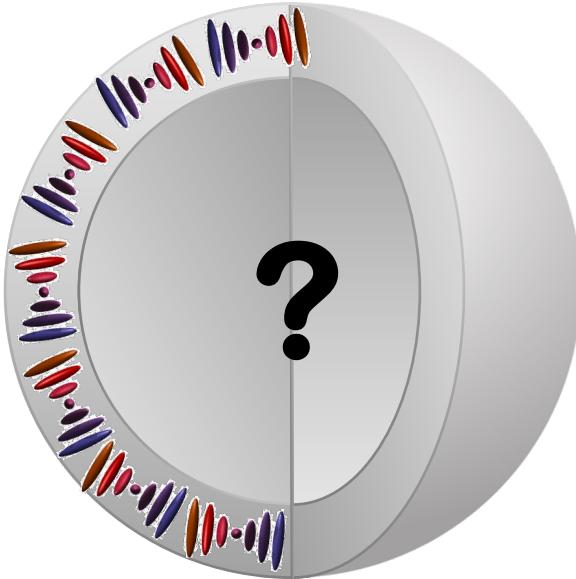
*no defect in  
director,  
but a defect  
in the pitch*

# *Surface anchoring and geometry*

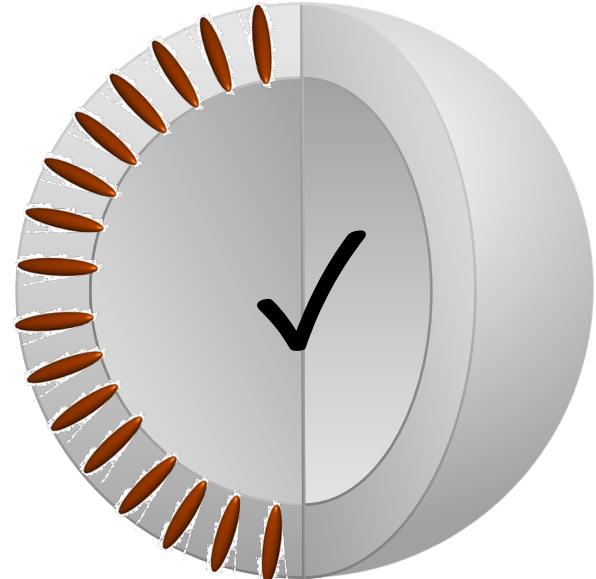
*L. Tran*



*planar  
anchoring*



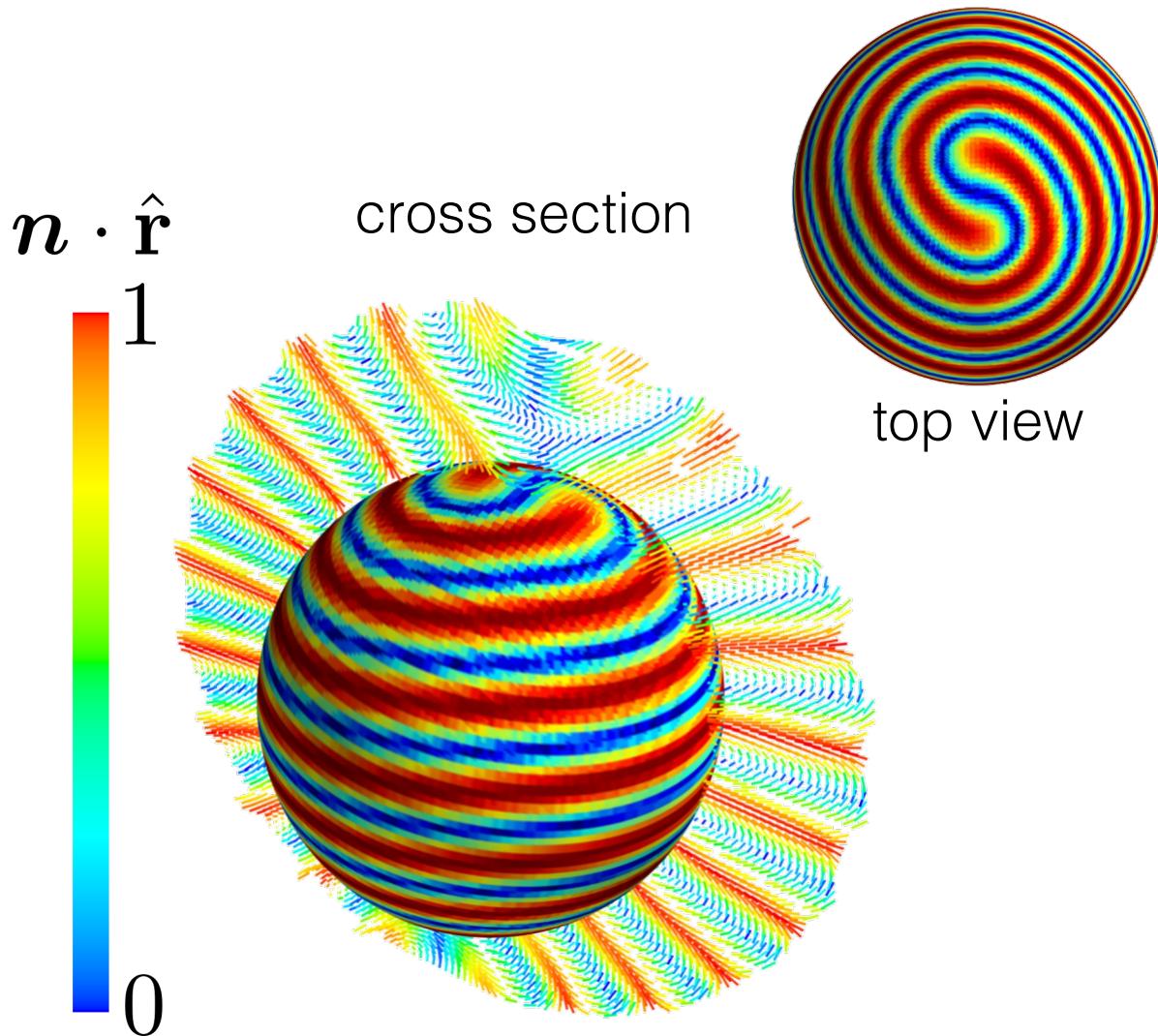
*weak  
perpendicular  
anchoring*



*strong  
perpendicular  
anchoring*

# *Ordering stripes in simulations*

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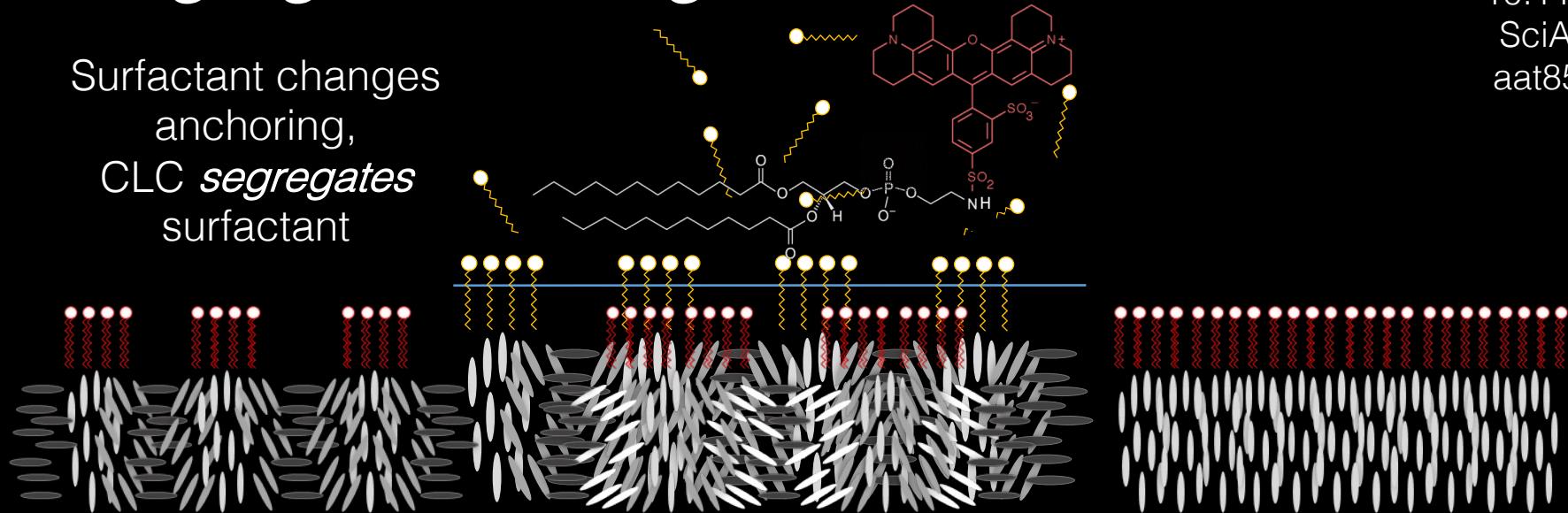


*published in PRX*  
DOI:  
[10.1103/PhysRevX.  
7.041029](https://doi.org/10.1103/PhysRevX.7.041029)

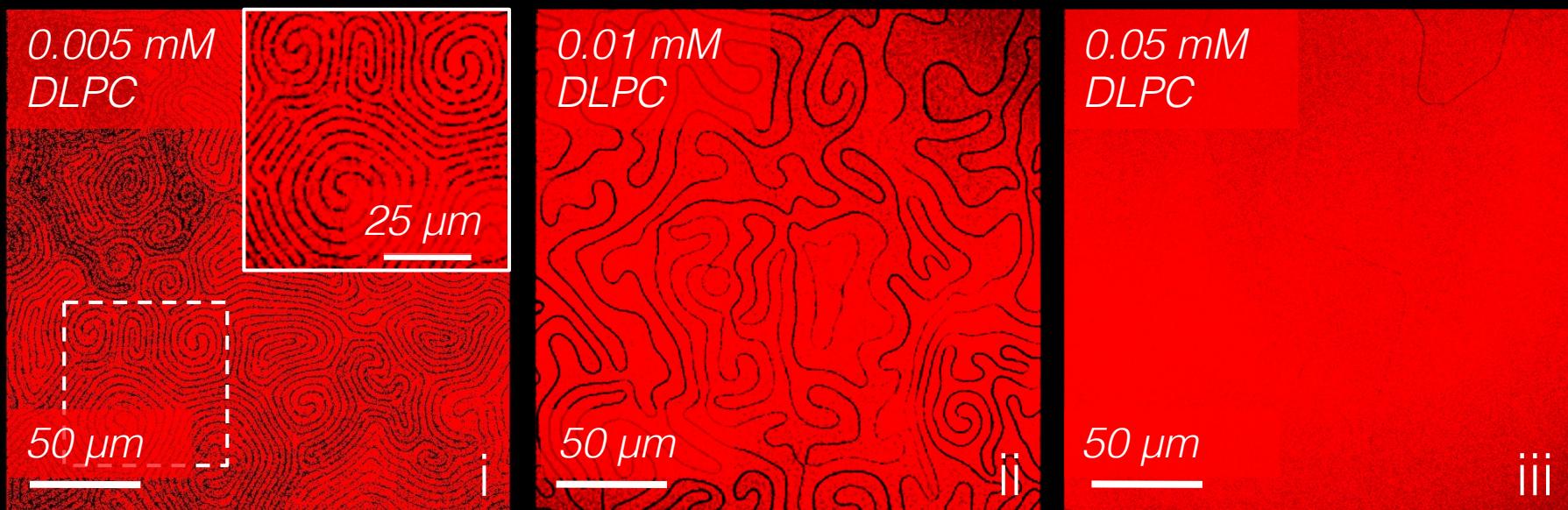
# Changing anchoring with surfactant

L. Tran DOI:  
10.1126/  
SciAdv.  
aat8597

Surfactant changes  
anchoring,  
CLC *segregates*  
surfactant

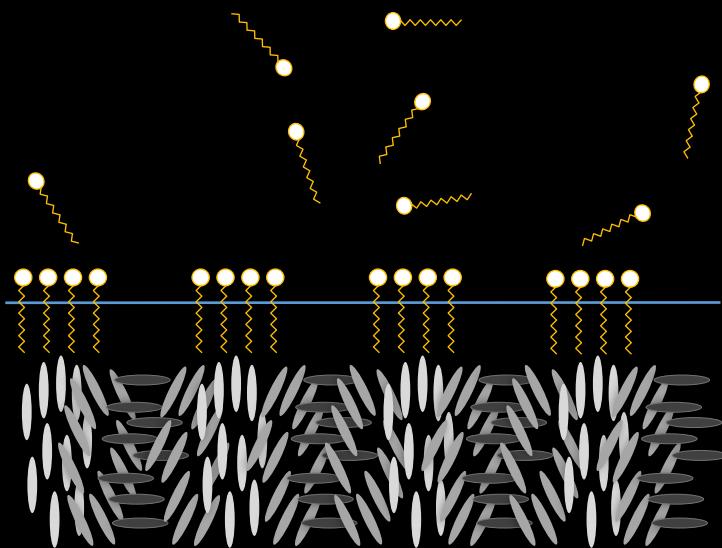


Flat cholesteric film: Fluorescently labeled lipid



# *Changing anchoring with surfactant*

L. Tran DOI:  
10.1103/  
PhysRevX.  
7.041029



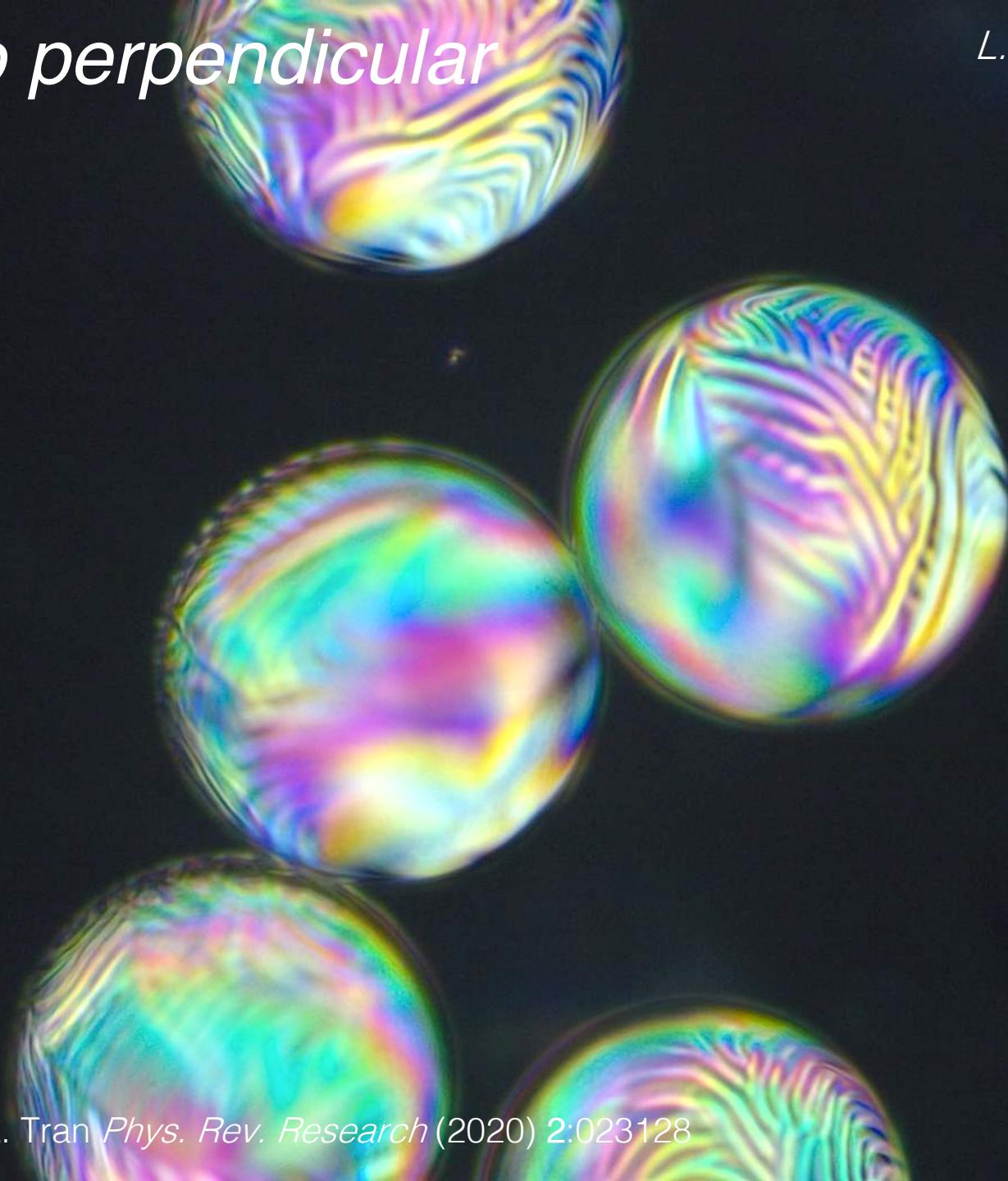
*Shell in 10 mM SDS, 0.1M NaCl*

*SDS is washed away*



# *Planar to perpendicular*

*L. Tran*



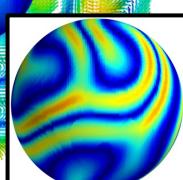
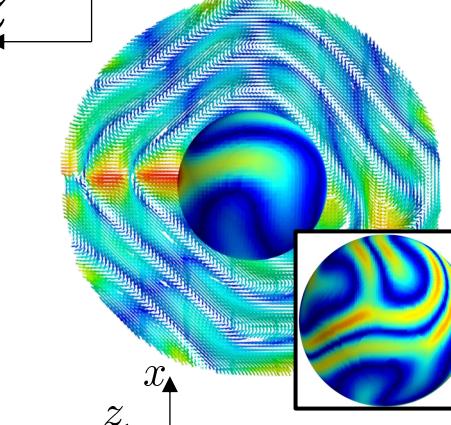
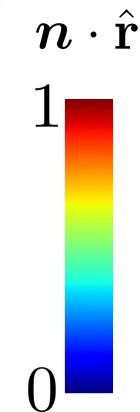
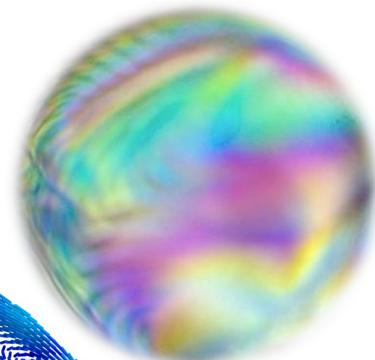
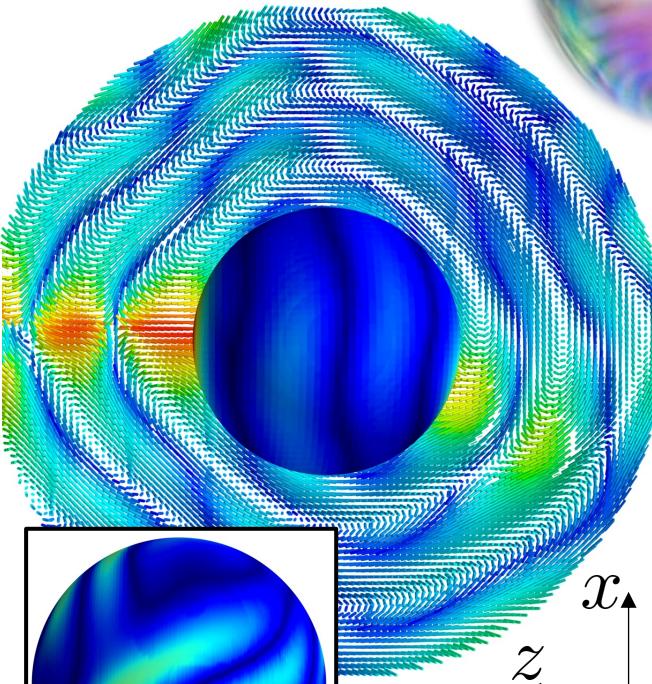
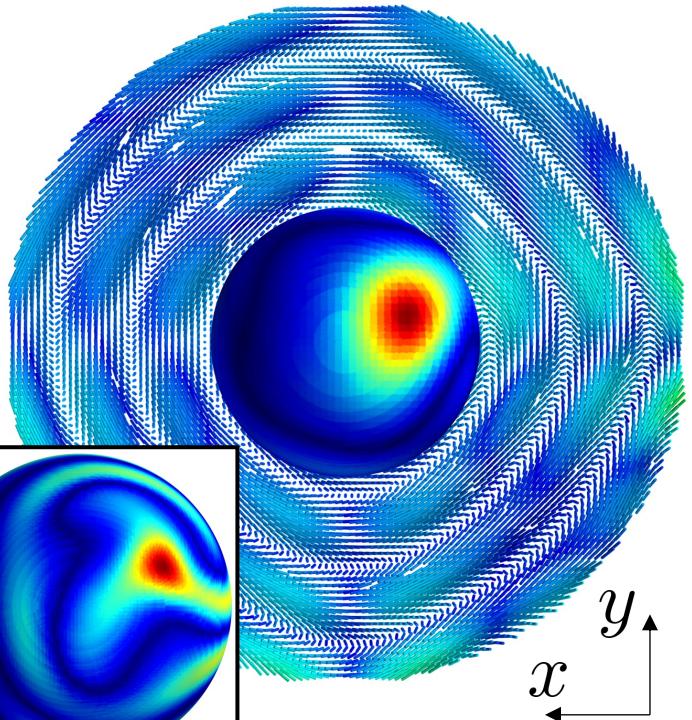
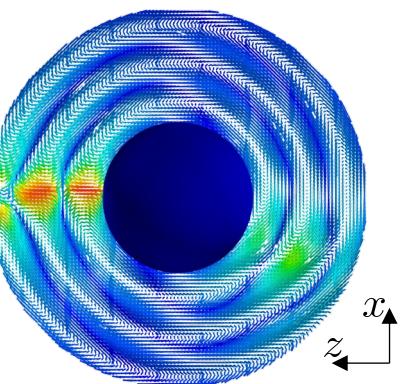
# Changing anchoring...

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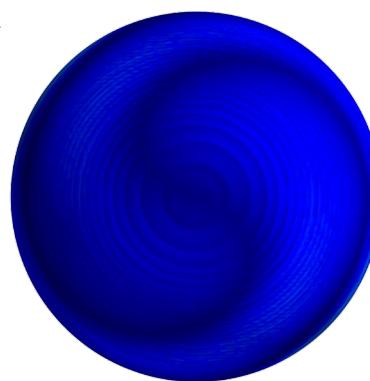
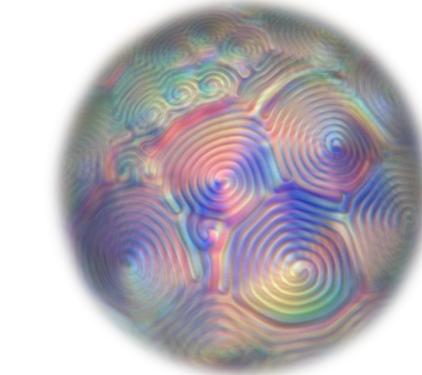
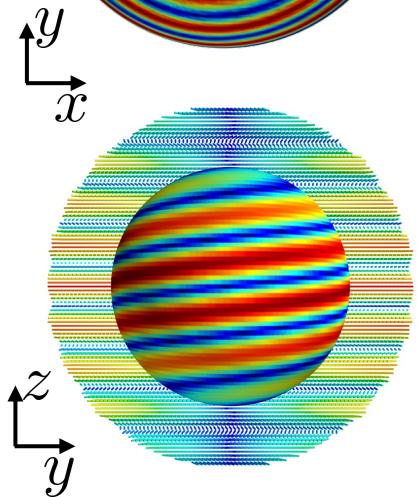
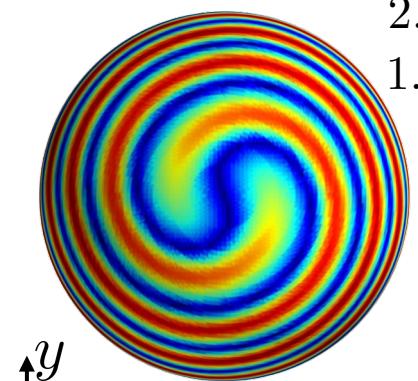


2.1  $\mu\text{m}$  thick  
1.2  $\mu\text{m}$  pitch

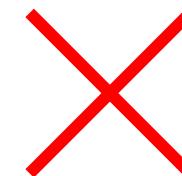
$2 \times 10^{-4} \text{ J/m}^2$   
perpendicular  
anchoring



# Changing anchoring...

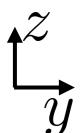
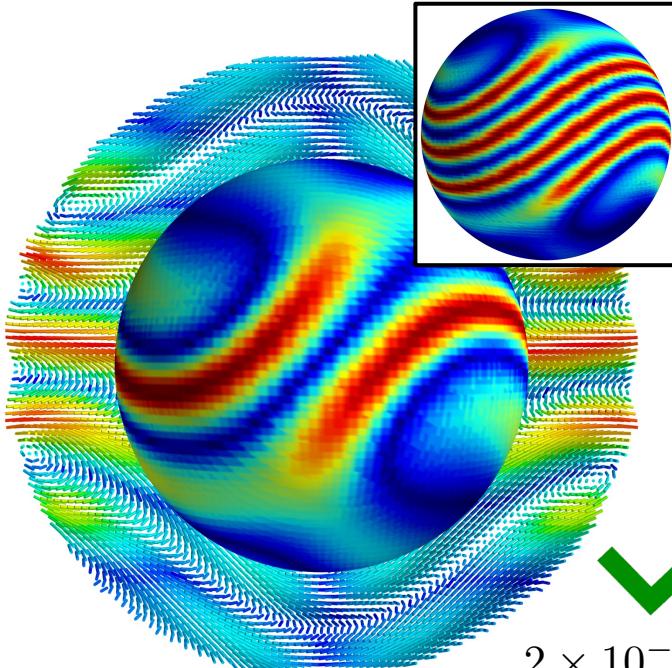


$2 \times 10^{-5} \text{ J/m}^2$   
planar  
anchoring

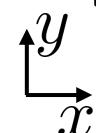
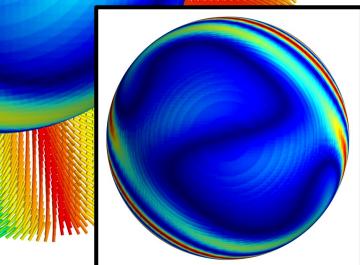
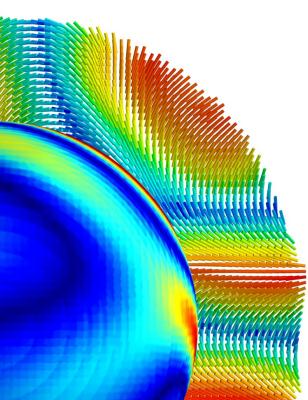


L. Tran DOI:  
10.1103/  
PhysRevResearch.  
2.023128

$n \cdot \hat{r}$



$2 \times 10^{-4} \text{ J/m}^2$   
planar  
anchoring

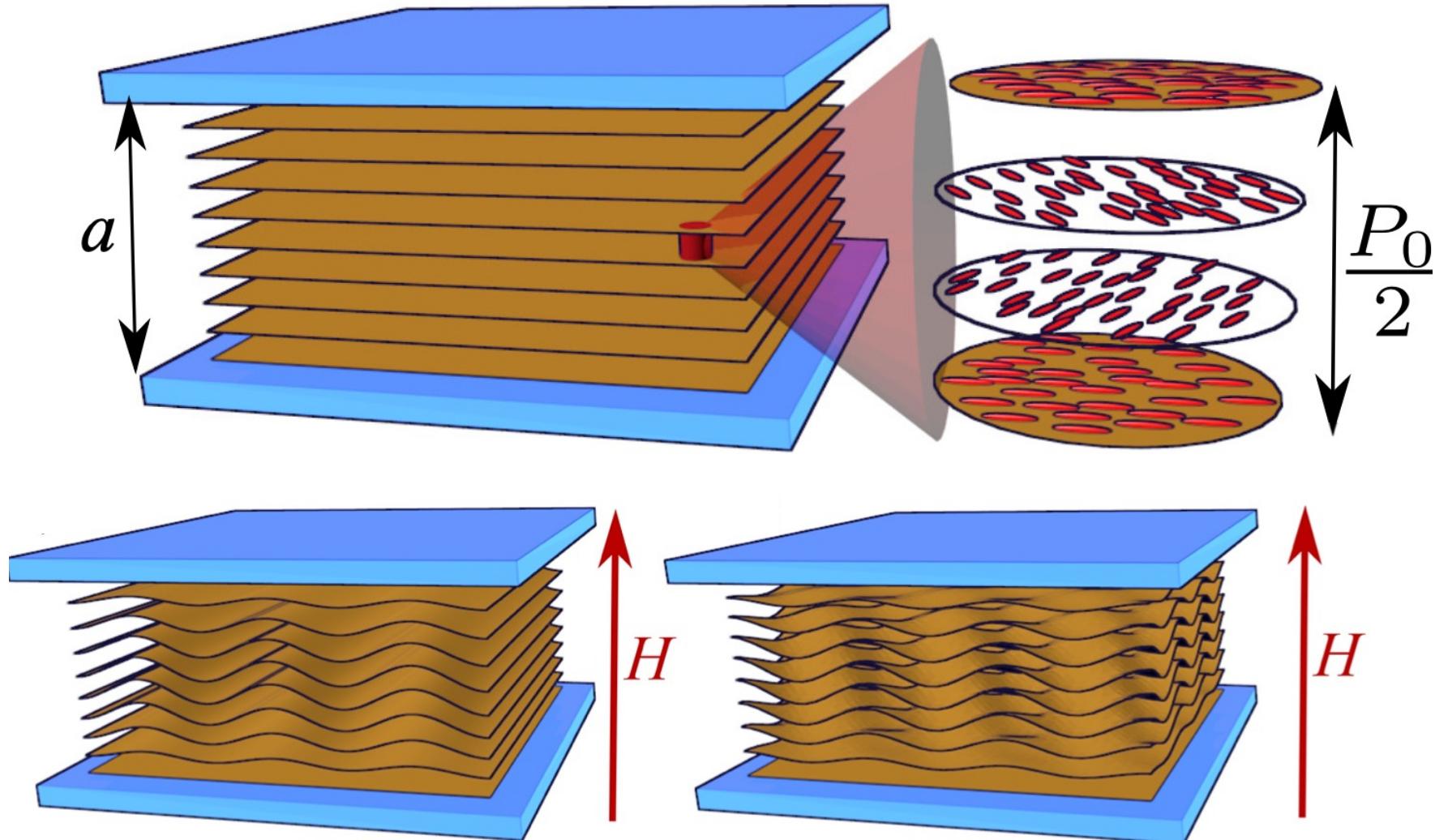


# Undulations? Some history...

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Cholesterics strained by external fields

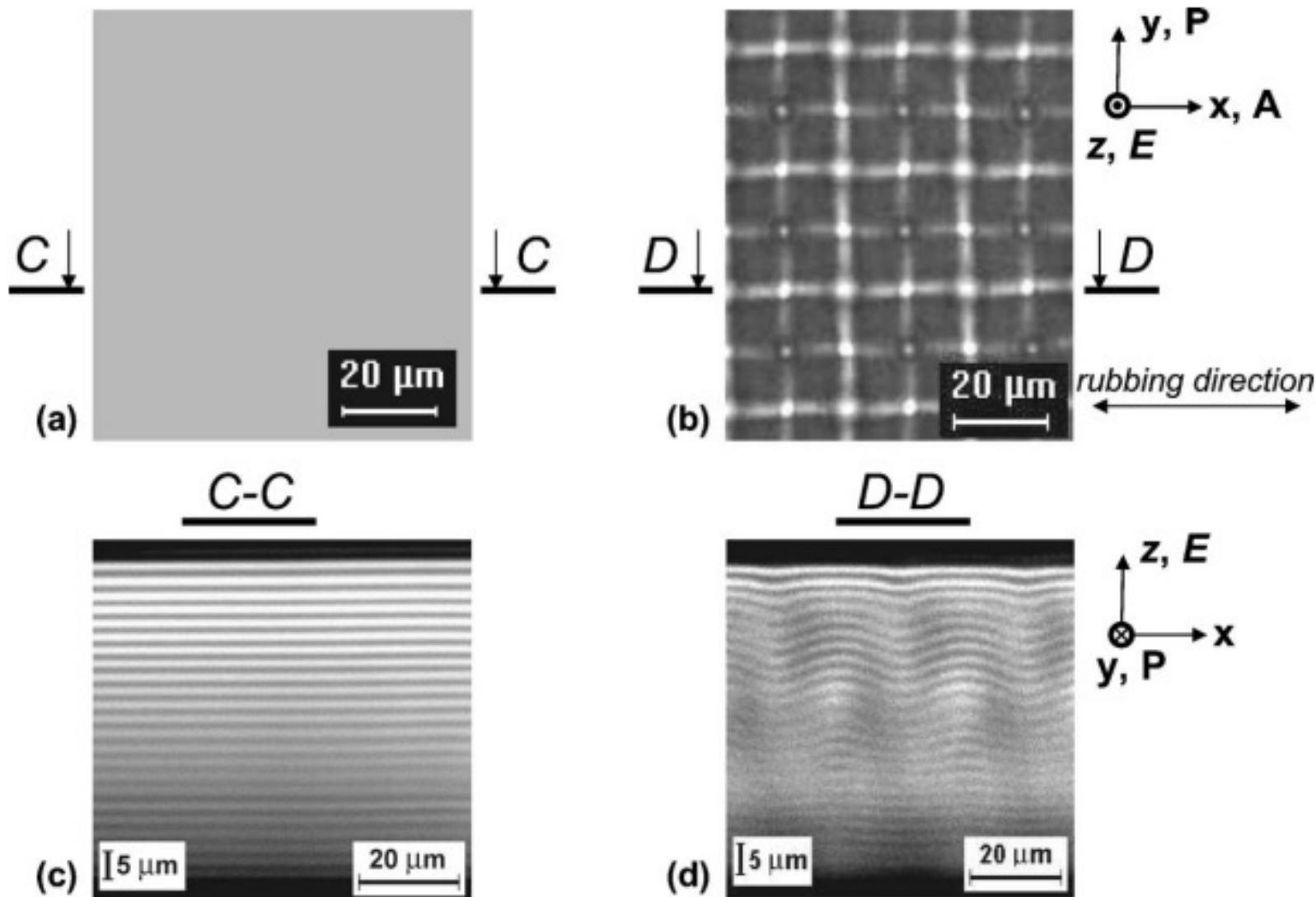


Initial studies by W. Helfrich (1970)  
and J. P. Hurault (1973)

**Helfrich-Hurault Instability**

# Helfrich-Hurault in experiments

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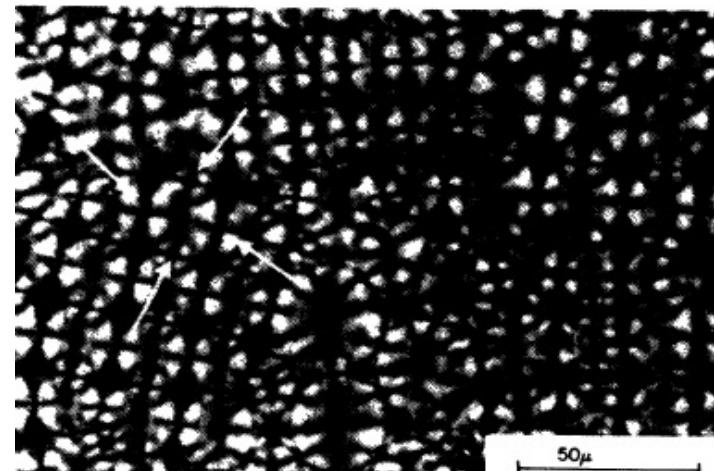
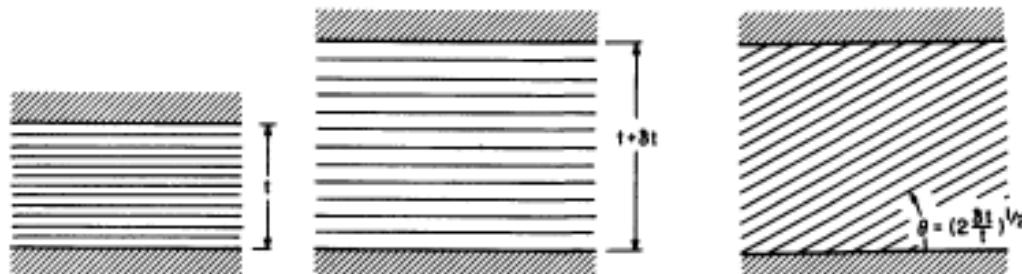


# Helfrich-Hurault also for smectics

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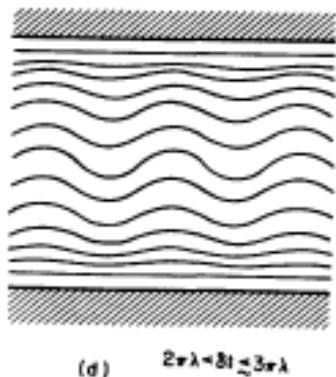


Under mechanical strain

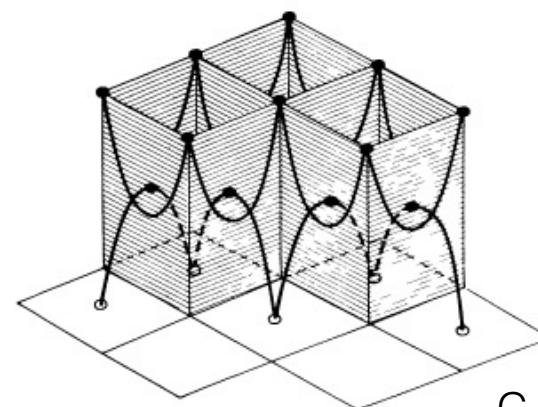
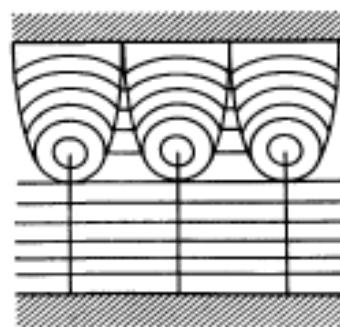


(a)  $\delta t \ll 2\pi\lambda$

(c)



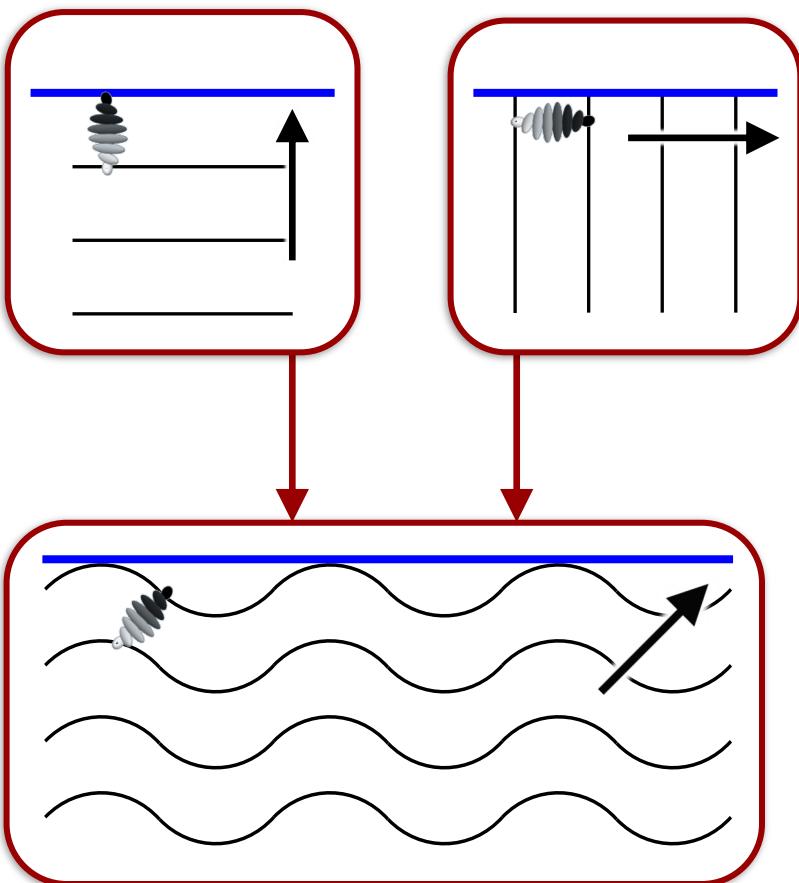
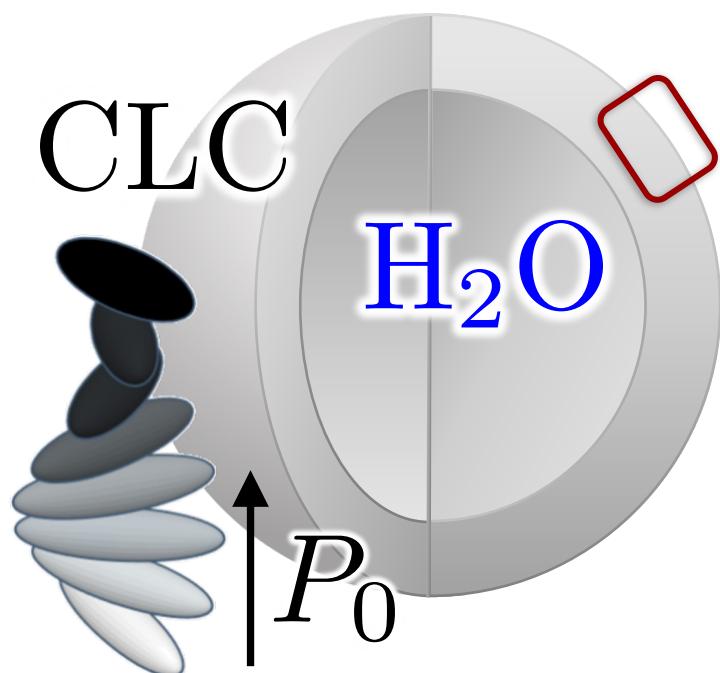
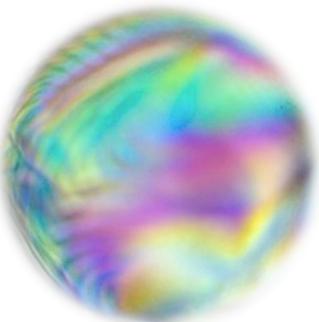
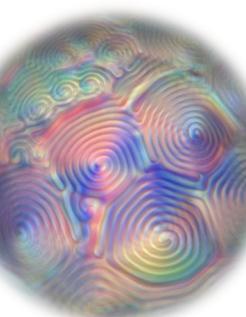
$2\pi\lambda < \delta t \lesssim 3\pi\lambda$



N. Clark & R.B. Meyer,  
*Appl. Phys. Lett.*  
(1973) 22:493

C. Rosenblatt, *et al.*  
*Journal de Physique*  
(1977) 38.9:1105-1115

# Proposed mechanism: surface “field” L. Tran

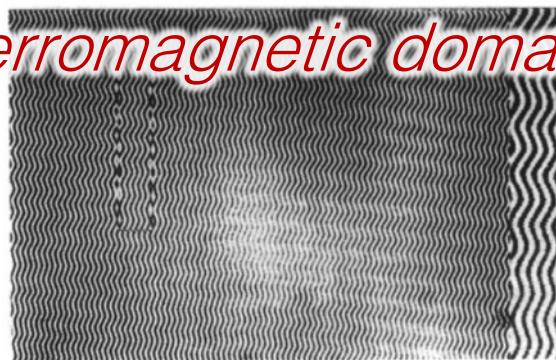
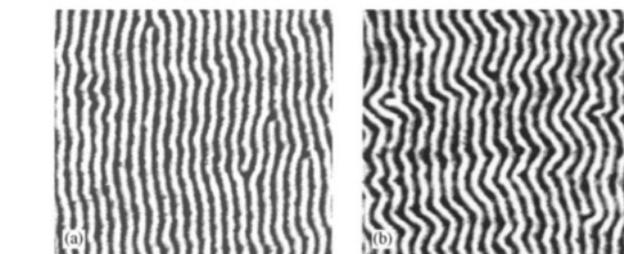
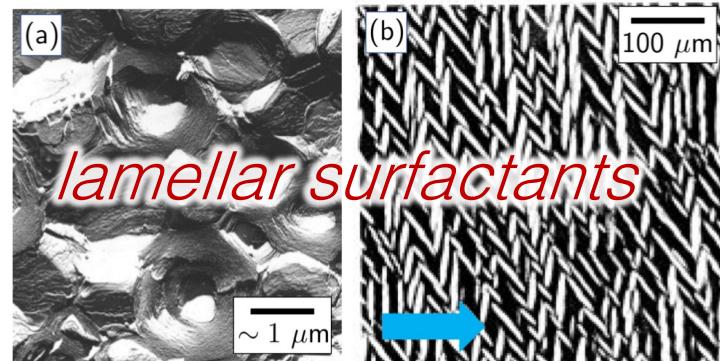
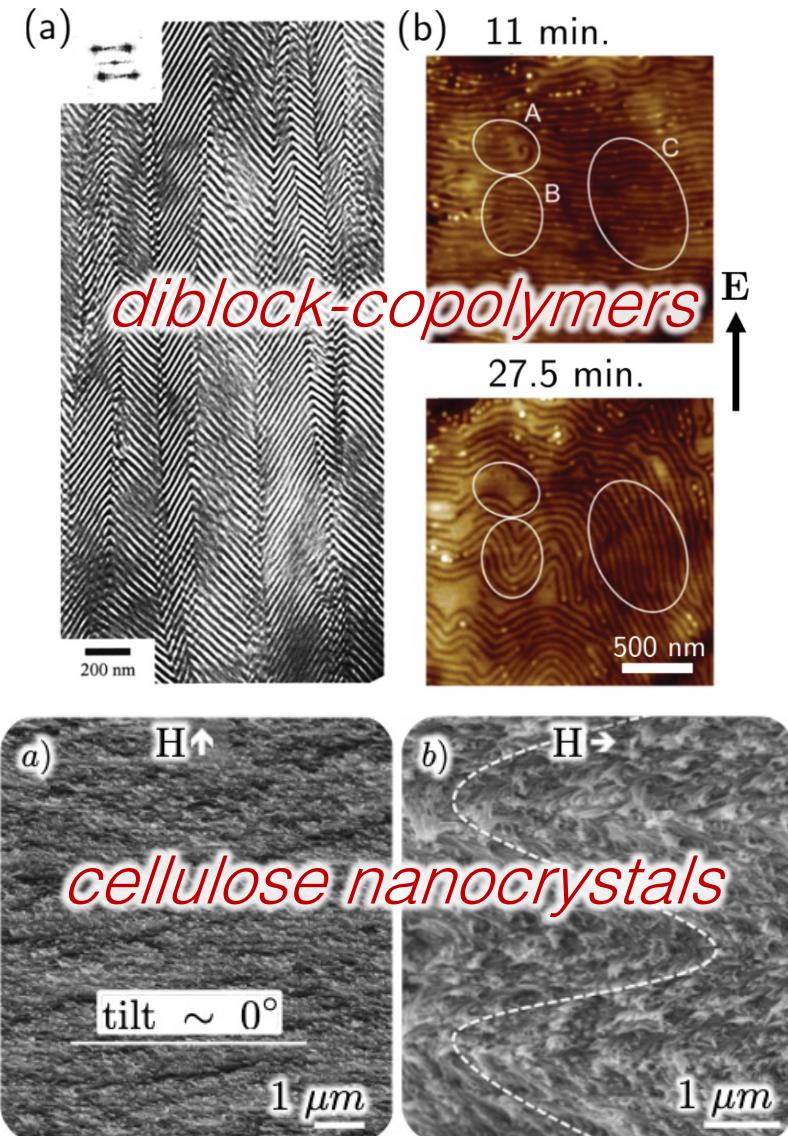


$$W_c \approx 10^{-5} \text{ J/m}^2$$

$$\lambda_x^* \equiv 2\pi/q_x^* \approx 2P_0$$

# Helfrich-Hurault in other materials

L. Tran DOI:  
10.48550/  
arXiv.2109.14668  
Accepted in Rev. Mod. Phys.



Y. Cohen *et al.* *Macromolecules* (2002) **33**(17):6502-6516; Liedel *et al.* *Small* (2015) **11**:6058-6064.

T. Gulik-Krzywicki, *et al.* *Langmuir* (1996) **12**:4668-4671; L. Ramos, *et al.* *Eur. Phys. J. B* (1999) **8**:67-72.

B. Frka-Petasic *et al.* *Adv. Mater.* (2017) **29**(32):1-7; M. Demand *et al.* *J. Magn. Magn. Mater.* (2002) **247**:147-152

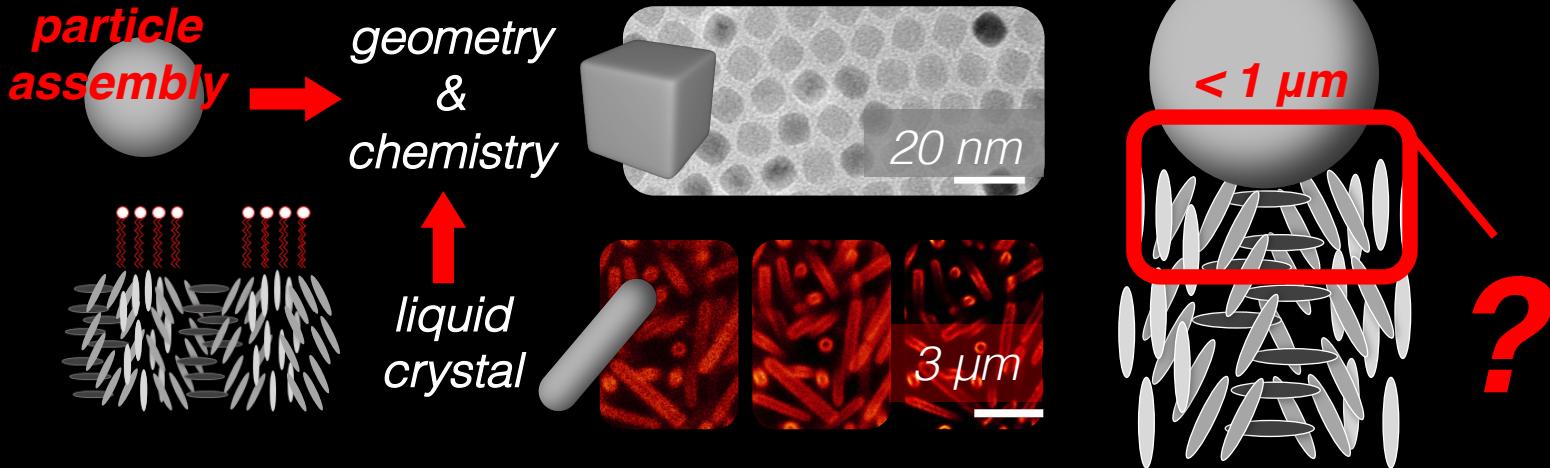
# Future directions

*I.tran@uu.nl*

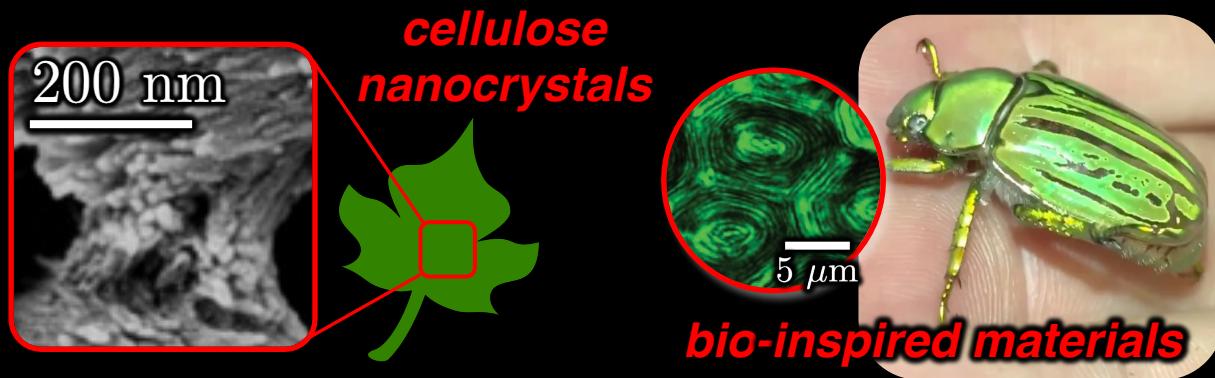
*L. Tran*



1



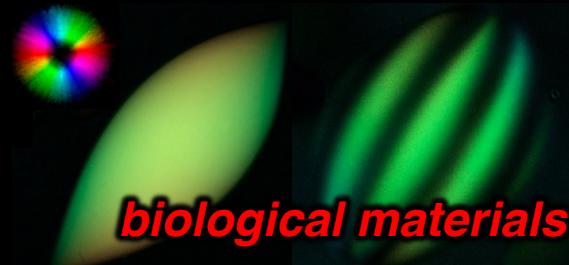
2



3

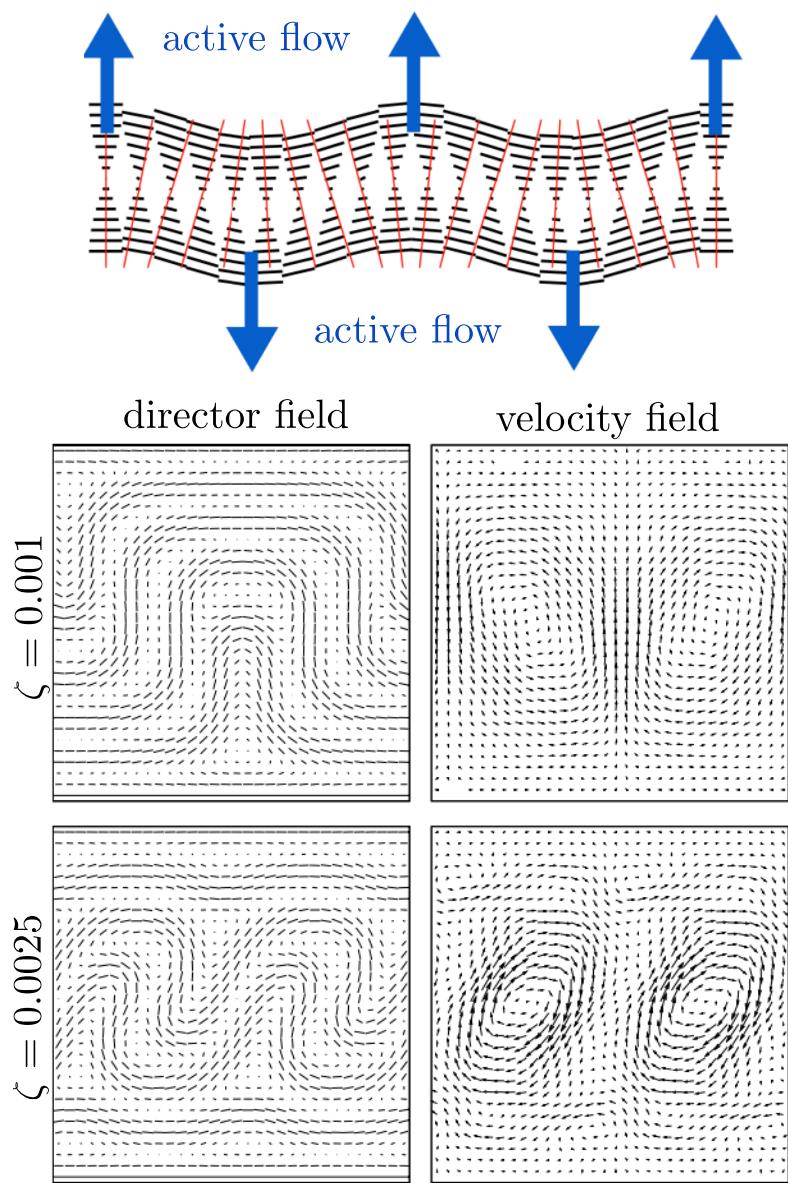


*LC ordering and confinement in biomimetic systems*



# Helfrich-Hurault in bio/active matter

L. Tran DOI:  
10.48550/  
arXiv.2109.14668  
*Accepted in Rev. Mod. Phys.*



Elongation zone of mung bean seedling



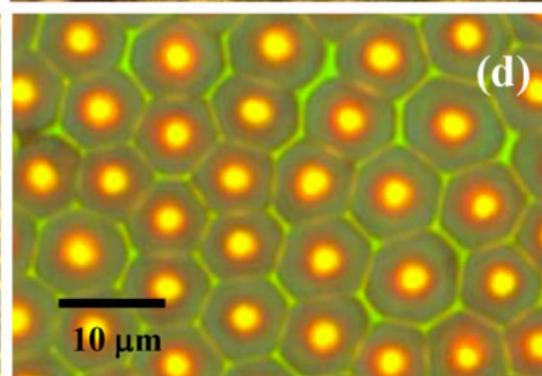
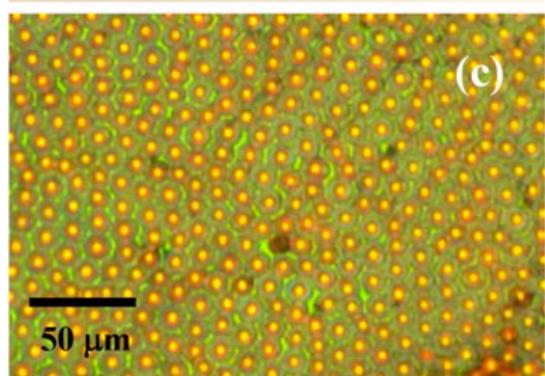
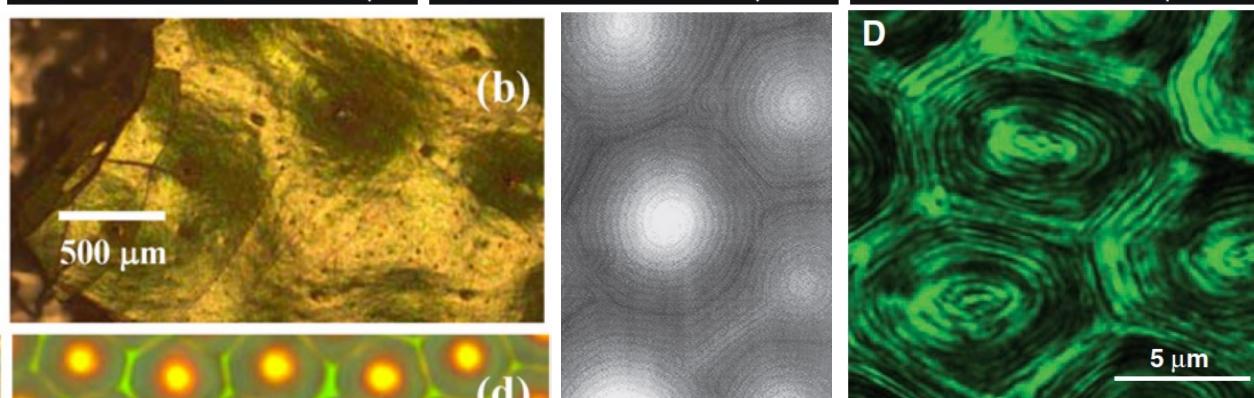
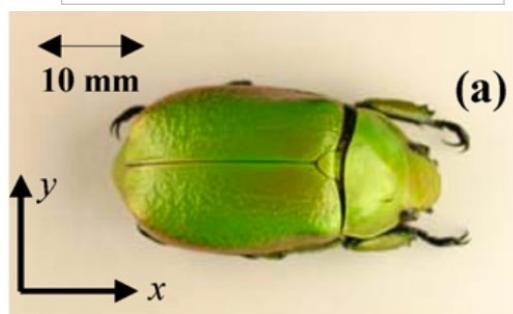
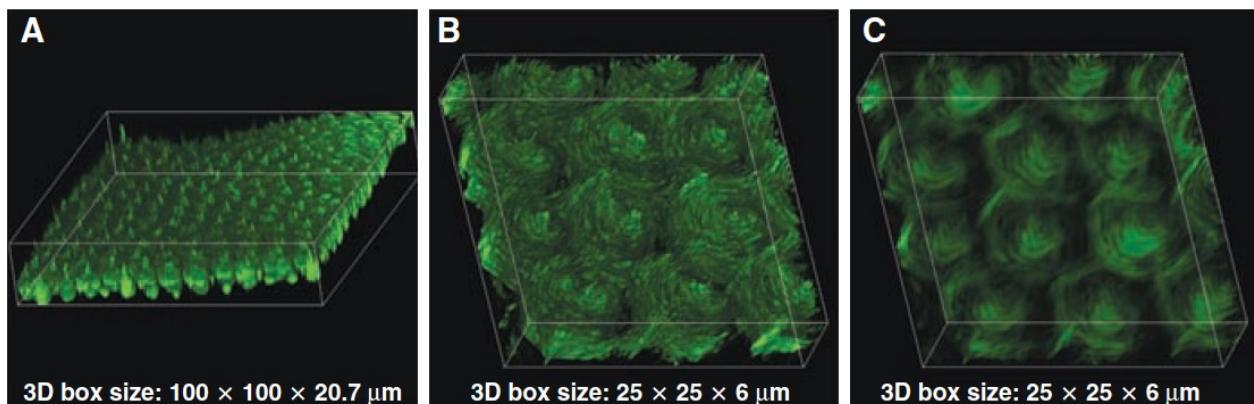
J.-C. Roland, et al. *Tissue and Cell*  
(1992) 24(3):335-345

# Cholesterics in the natural world

L. Tran



## Structural color



V. Sharma, M. Crne, J. O. Park, M. Srinivasarao, *Science* **325** (2009): 449-451

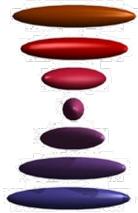
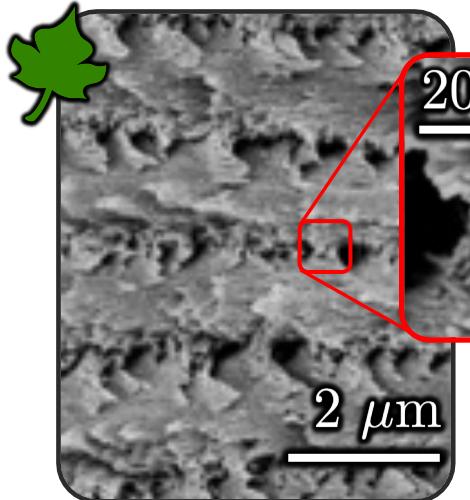
S. A. Jewell, P. Vukusic, & N. W. Roberts, *New Journal of Physics* **9** (2007) 99

# Cellulose nanocrystals

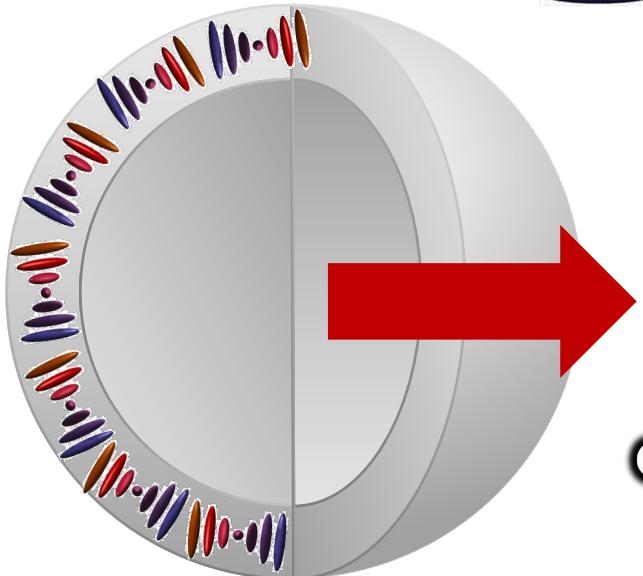
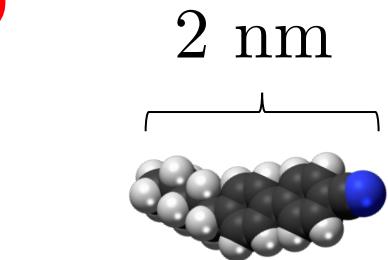
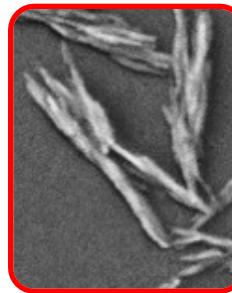
L. Tran



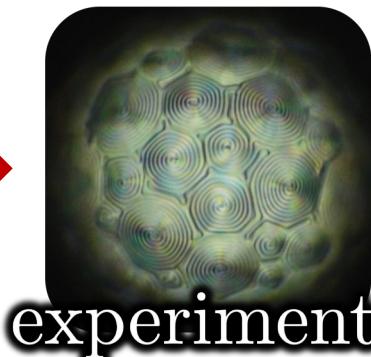
From molecular to colloidal LCs



Diogo Saraiva



small molecule

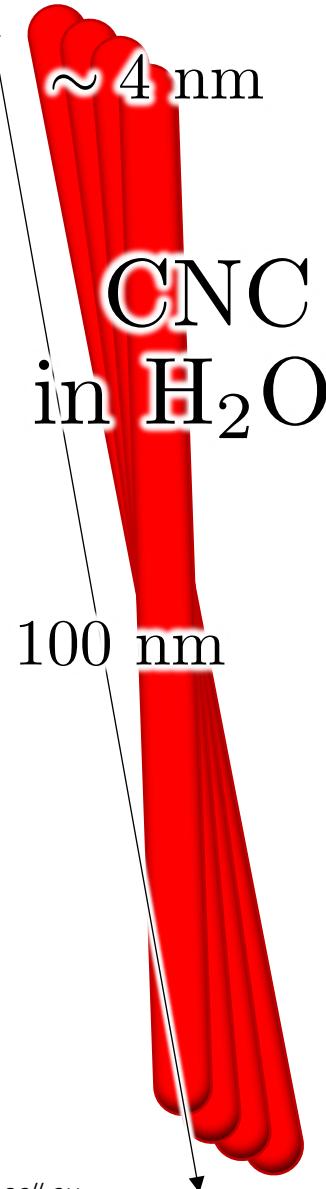


experiments

&



simulations



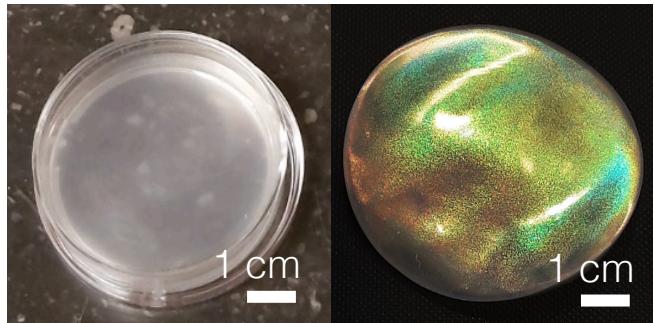
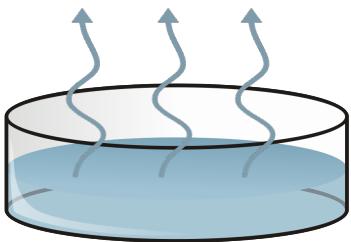
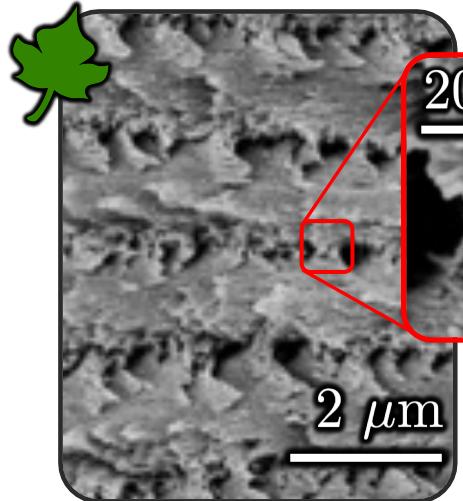
[nanocrystacell.eu](http://nanocrystacell.eu)

L. Tran, *et al.*, *Phys. Rev. X*(2017) 7:041029.

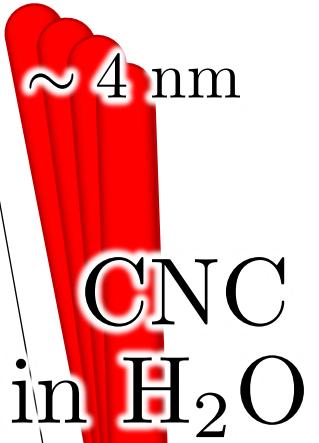
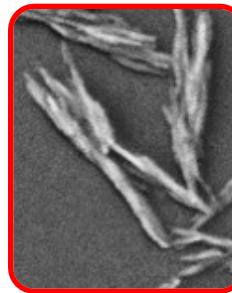
J. Majoinen, ... D.G. Gray, *Cellulose* (2012) 19:1599-1605.

# Photonic CNC assembly

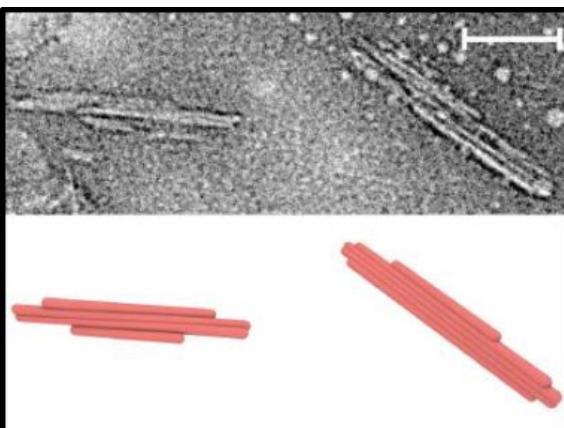
L. Tran



Diogo Saraiva



CNC bundles



Marjolein Dijkstra



[nanocrystacell.eu](http://nanocrystacell.eu)

M. Chiappini, *et al.*, *J. Chem. Phys.* (2022) 1:014904.

J. Majoinen, ... D.G. Gray, *Cellulose* (2012) 19:1599-1605.

# Confinement of colloidal nematics

L. Tran



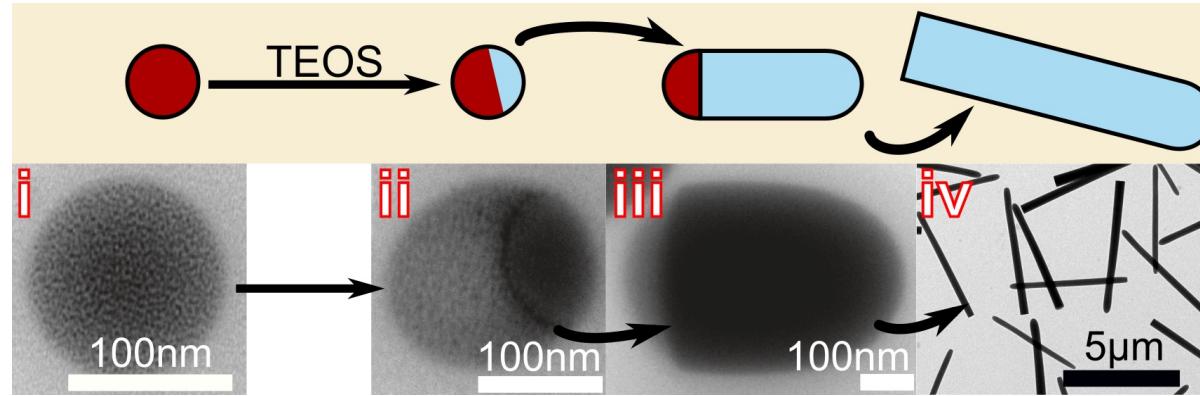
Ethan Jull



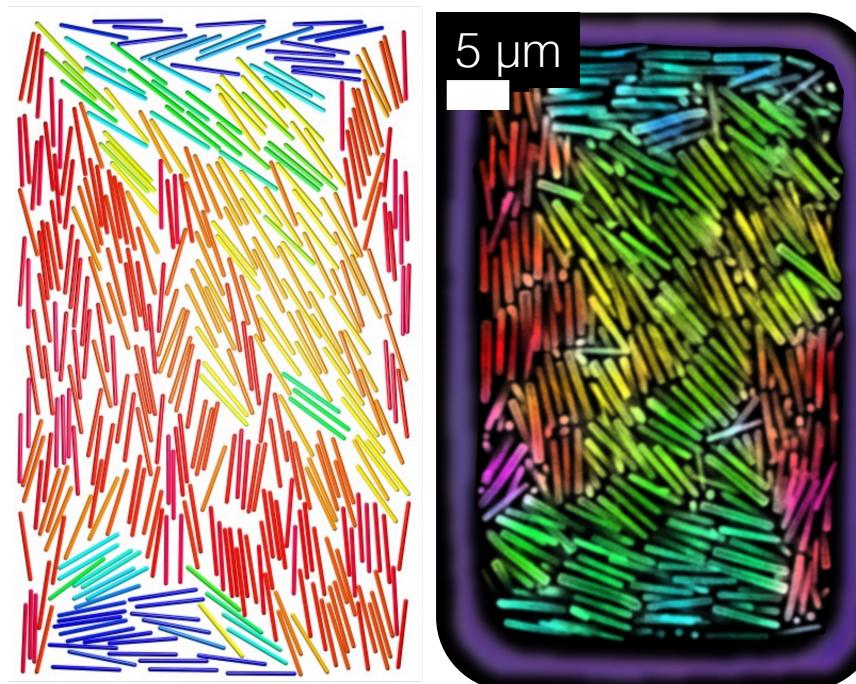
Gerardo C.  
Villalobos



Marjolein  
Dijkstra



A. Kuijk et al., "Synthesis of monodisperse, rodlike silica colloids with tunable aspect ratio", *JACS*, 133 (2011)



Rama Kotni



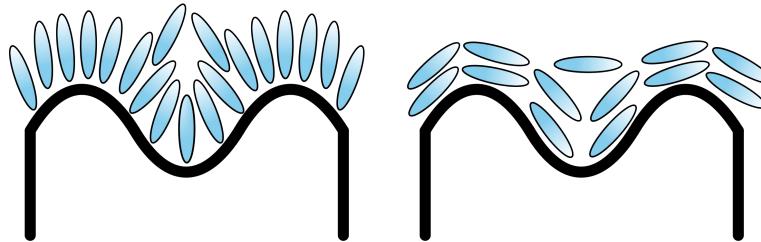
Alfons van  
Blaaderen

# Anchoring of colloidal nematics

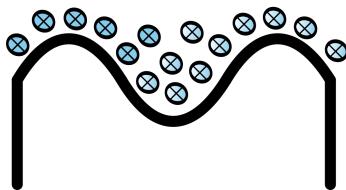
L. Tran



Ethan Jull



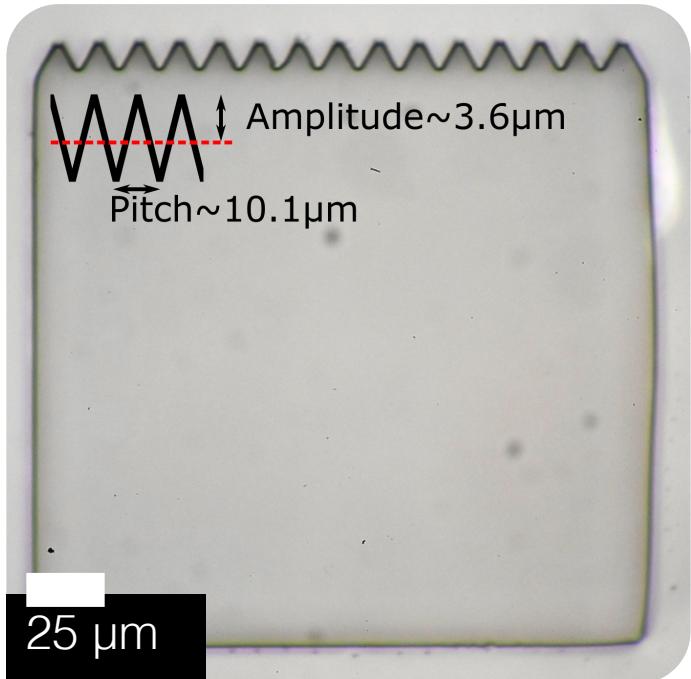
High elastic distortion



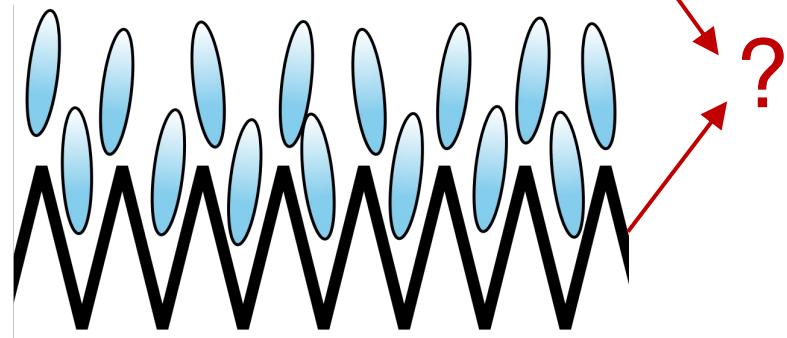
Low elastic distortion

**Berreman Model**

D. W. Berreman, *Phys. Rev. Lett.* 28 (1972)



Features approach size of the mesogen



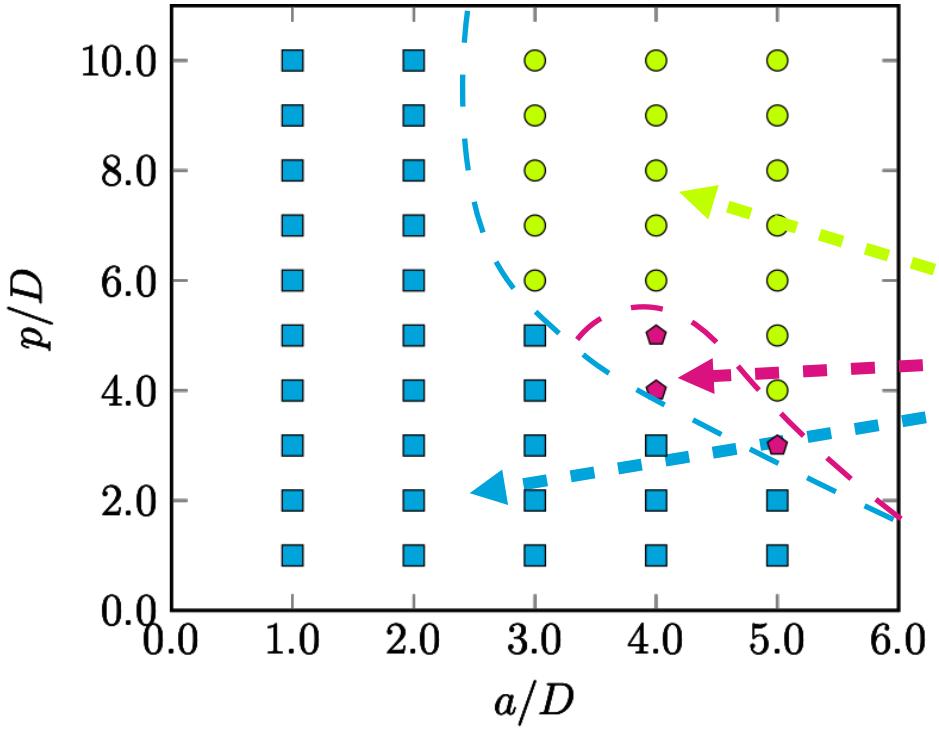
$$f_s = -\frac{1}{2} \boxed{W} (\mathbf{n} \cdot \mathbf{e})^2$$

# Anchoring of colloidal nematics

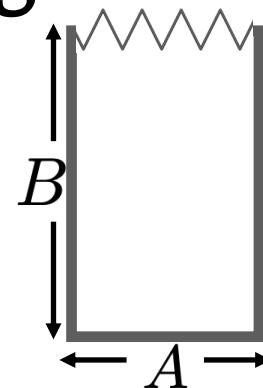
L. Tran



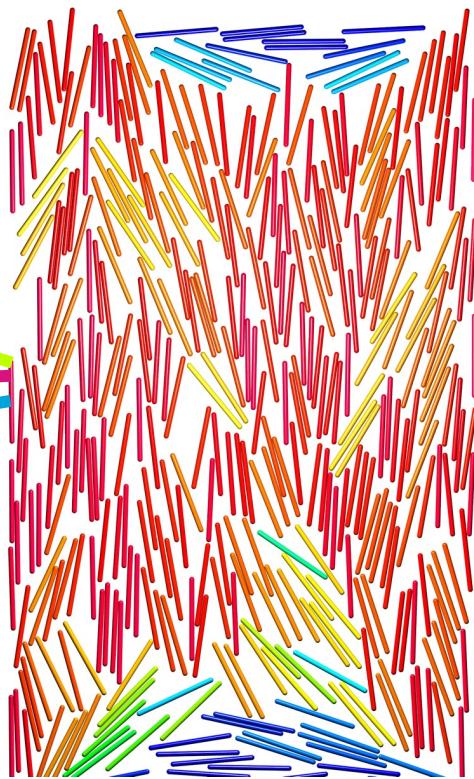
Ethan Jull



## Confined Colloidal System - Anchoring



$$A/L = 6$$
$$A/B = 0.6$$



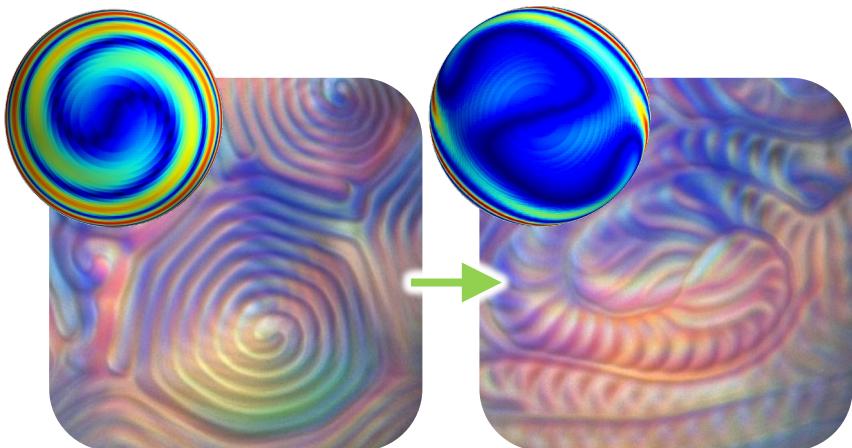
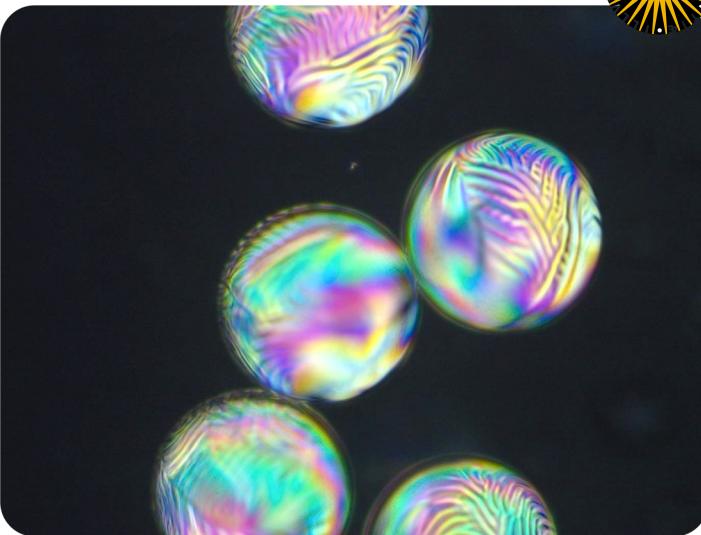
# Conclusions

*l.tran@uu.nl*

L. Tran



- *Helfrich-Hurault Instability:*  
Strain in periodic systems generates undulations
  - can be induced from surfaces
  - is widely applicable to lamellar systems
  - DOI:10.48550/arXiv.2109.14668
- *My collaborators in this work:*
  - Max Lavrentovich (UT Knoxville)
  - Teresa Lopez-Leon (ESPCI)
  - Randy Kamien (UPenn)
  - Christophe Blanc (Montpellier)



Thank you:

SIMONS  
FOUNDATION



MARIE CURIE ACTIONS

NWO