



de Sitter space as a Glauber-Sudarshan state

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- **Four dimensional de Sitter space is a Glauber-Sudarshan state in string theory I, II, Suddhasattwa Brahma, K.D, Radu Tatar et al 2007.00786, 2108.08365; de Sitter space is a Glauber-Sudarshan state in string theory, 2007.11611**
- **Crisis on infinite earths: short-lived dS vacua in the string theory landscape, Heliudson Bernardo, Suddhasattwa Brahma, KD, Radu Tatar, 2009.04504**
- **Quantum Break-Time of de Sitter, G. Dvali, C. Gomez and S. Zell, 1701.01776; Quantum Breaking Bound on de Sitter and Swampland, G. Dvali, C. Gomez, S. Zell, 1810.11002**

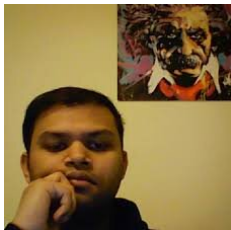
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- **de Sitter vacua in type IIB string theory: Classical solutions and quantum corrections**, K.D, Rhiannon Gwyn, Mohammed Mia, Evan McDonough and Radu Tatar **1402.5112**.
- **$\overline{D3}$ and dS**, Eric Bergshoeff, K.D, Renata Kallosh, Antoine Van-Proyen, Timm Wrase, **1502.07627**
- **Quantum Corrections and the de Sitter Swampland Conjecture**, K.D, Maxim Emelin, Evan McDonough, Radu Tatar, **1808.07498**
- **de Sitter vacua in the string landscape**, K.D, Mir Mehedi Faruk, Maxim Emelin, Radu Tatar, **1908.05288**; **How a four-dimensional de Sitter solution remains outside the swampland**, **1911.02604**

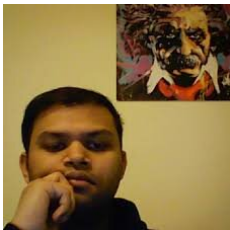
Cast of characters

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Suddhasattwa Brahma

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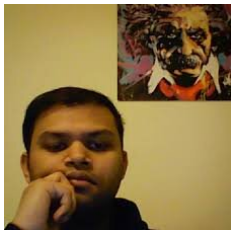


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Heliudson Bernardo

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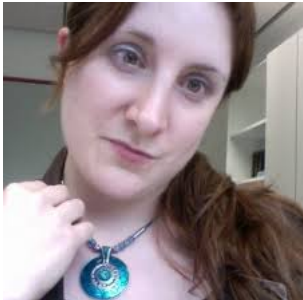
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Dasgupta (McGill)



BIRS, Banff, Alberta: July 5, 2023

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- How to realize de Sitter in the string landscape
- How to realize it as a **Glauber-Sudarshan state** instead of a **vacuum**
- Why is this a hard problem?
- Although hard, it may still be a doable problem!

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My aim here is to argue that such a system **can** be solved in string theory!

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which is a de Sitter space with a flat slicing with Λ the cosmological constant and the temporal coordinate t has a range $-\infty \leq t \leq 0$, with the late time regime given by $t \rightarrow 0$.

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- Provides easy answers to hard questions like entropy, vacuum energy, trans-Planckian cosmic censorship (TCC), etc. thus explaining **why** we want to construct it in a UV complete theory.

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In the following I'll try to answer at least some of the above questions, while motivating the others.

For computational efficiency we will study this from M-theory point of view, where the metric takes the following form.

$$ds^2 = g_s^{-8/3} \eta_{\mu\nu} dx^\mu dx^\nu + g_s^{-2/3} H^2 \left(F_1(t) g_{\alpha\beta} dy^\alpha dy^\beta + F_2(t) g_{mn} dy^m dy^n \right) + g_s^{4/3} |dz|^2,$$

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So how are we to realize such a background?

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You could say that it'll then be impossible to solve the system, or some of you may ask: how do we even know that Wilsonian method of integrating out high energy modes work when the modes are themselves **changing with respect to time**? We will come back to the latter question, if time permits, but for the first question: lets see what we can do.

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So question: what are the allowed perturbative terms at small g_s and low energies?

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What is the G-flux ansatz? Here it appears three possibilities.

$$\mathbf{G}_{MNPQ}(g_s, y) = \sum_k \mathcal{G}_{MNPQ}^{(k)}(y) \left(\frac{g_s}{H} \right)^{2k/3}, \quad (M, N) \in \mathcal{M}_4 \times \mathcal{M}_2$$

$$\mathbf{G}_{MNab}(g_s, y) = \mathbf{F}_{MN}(y, g_s) \Omega_{ab}(y, g_s), \quad \mathbf{G}_{0ijM} = \partial_M \left(g_s^{-4} \epsilon_{0ij} \right)$$

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The latter condition keeps the 4d Newton's constant time independent. Question now is: what strategy do we follow to determine whether the above background is consistent or not?

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As a result, to any given powers of $\frac{g_s^{|a|}}{M_p^b}$ there are literally an infinite number of operators, thus killing both the g_s and M_p hierarchies!

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Note that we have derived our results by going deep in the core of M-theory/IIB without using any adhoc hypothesis.

Loss of g_s and M_p hierarchies mean that there is no simple EFT description in four-dimensions with de Sitter isometries.

I just gave an example with perturbative quantum terms. Similar and more drastic violation of the EFT happens with non-perturbative, topological and (worse) with non-local quantum terms.

Thus we **cannot** get de Sitter with any classical sources, and even with any amount of quantum terms if the G-flux components are **time-independent**. Nothing can save the day there, and these backgrounds are truly in the swampland.

Note that we have derived our results by going deep in the core of M-theory/IIB without using any adhoc hypothesis. So Vafa is not wrong when he said that these backgrounds are in the swampland!

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In fact we can do even better. We can realize the above background as a **Glauber-Sudarshan** state over a supersymmetric Minkowski background.

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Why is finding de Sitter space in string theory a hard problem?

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The EOMs however can only provide a local picture, but the existence of a solution, or even the Glauber-Sudarshan state, relies heavily on global constraints too. The global constraints come from flux quantizations, anomaly cancellations, moduli stabilization etc.

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- How the zero point energy gets renormalized in a non-supersymmetric background.
- How the geometry and the topology of the internal *compact* space, which is now a highly non-Kähler manifold, may be expressed.

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And many more; all in a top-down (not bottom up!) string theory set-up. As one may see, **most** need to be solved otherwise we cannot claim that we have a de Sitter solution in string theory! This is what makes it a **hard** problem.

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In this language, the EOMs discussed earlier appear as **Schwinger-Dyson equations**. The coherent state by itself is generated by displacing an **interacting** vacuum by the displacement operator.

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THANK YOU FOR YOUR ATTENTION!