

$$F_2 = H = \frac{1}{2} \left(p_\theta^2 + \frac{p_\varphi^2}{\sin^2 \theta} \right) + \cos \theta$$