

# ***Climate extremes*** *from statistics to society*

Andrea Toreti



# Outline

Characterising

*EVT, TX90p, SU, FD, ...*

Predicting

*Z500, PV, AMO, ...*

Evaluating

*CMIP5, CORDEX,...*

Impacts

# Characterising

Different approaches, different data sets, different problems

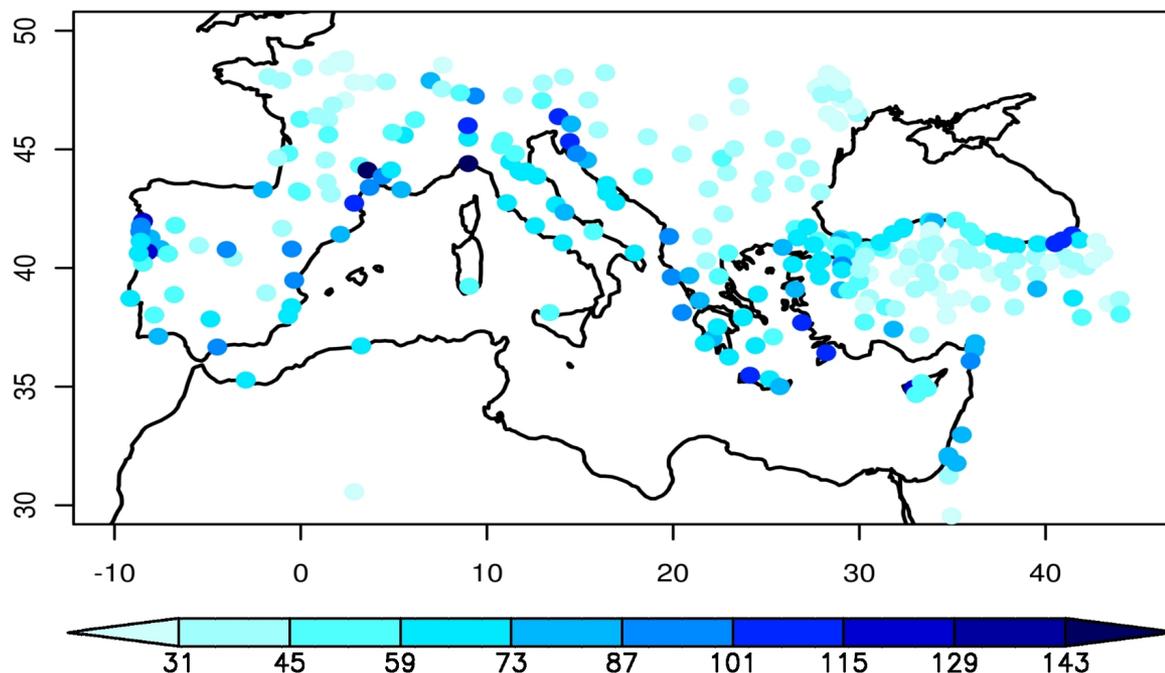
EVT, index-based, others, ...

observations from weather stations, satellite-ground observations, reanalysis, ...

Spatio-temporal scales

# Characterising I

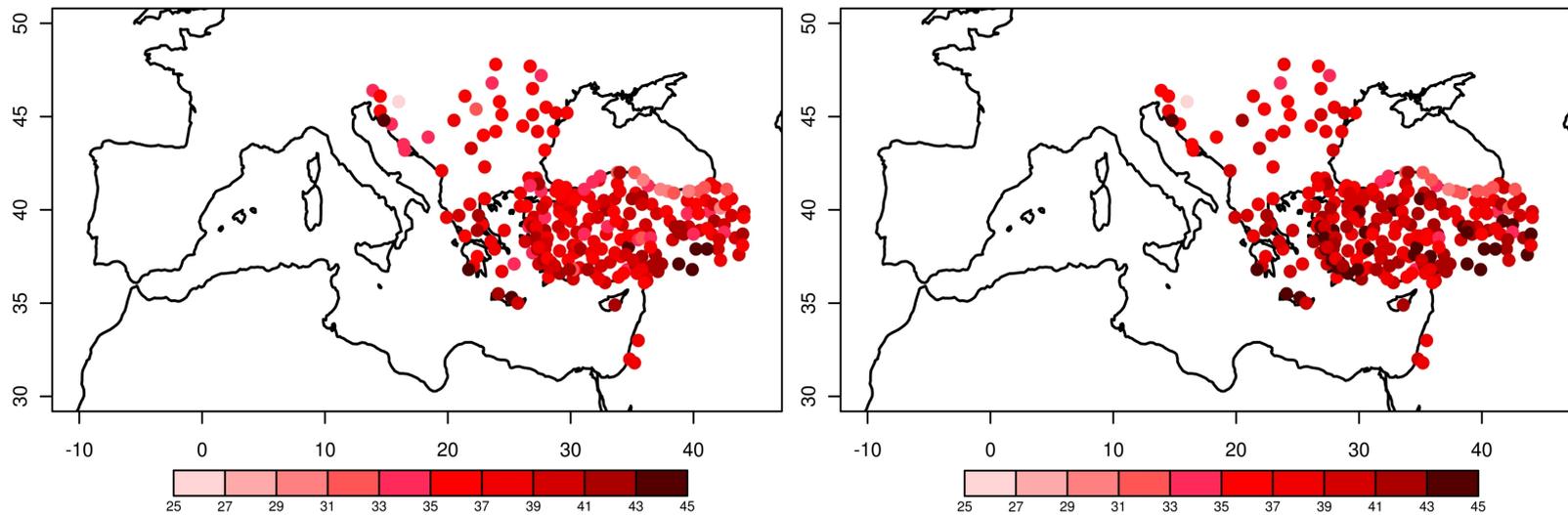
stationary univariate POT approach



*Estimated 5-y ret levels of daily precipitation in winter. Data from the last 5 decades. Source: Toreti, 2010*

# Characterising II

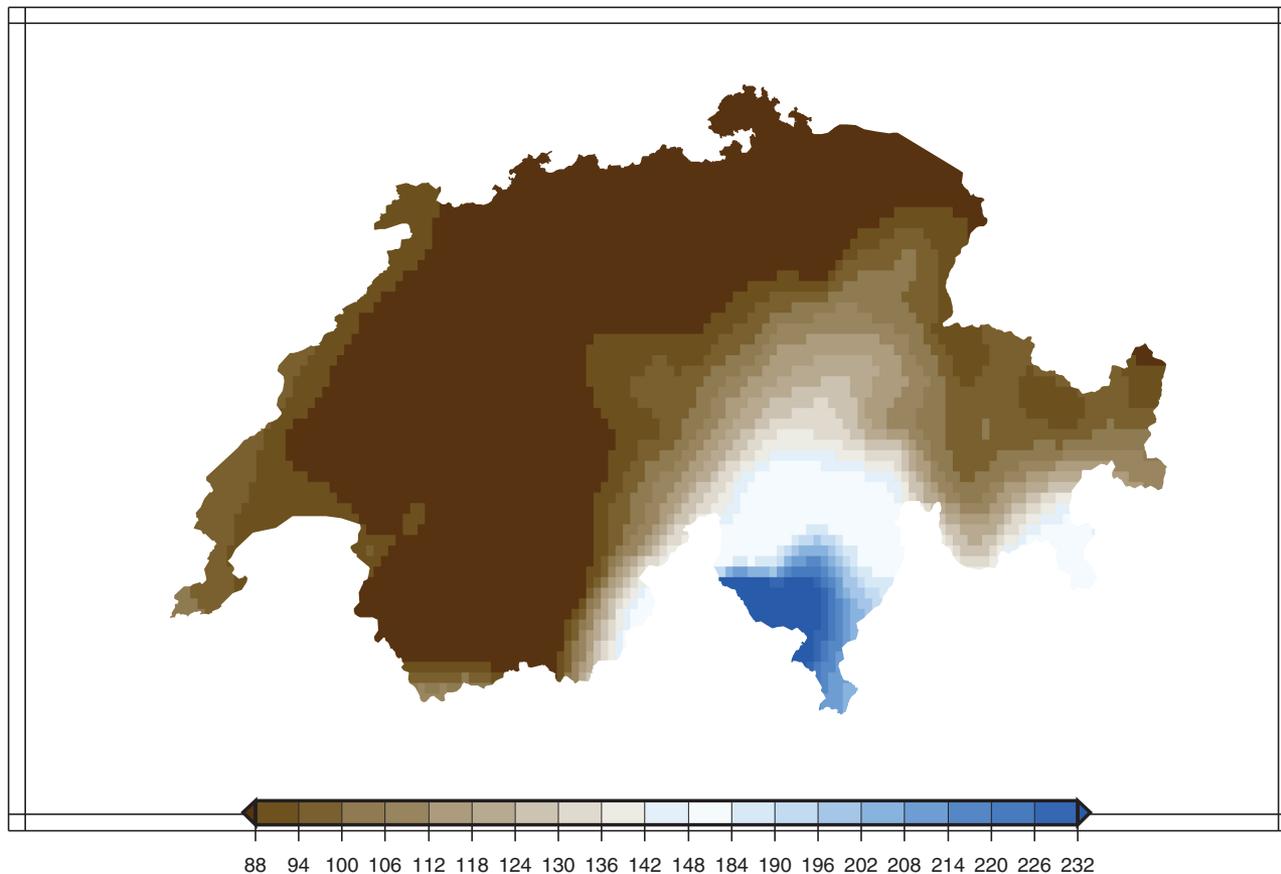
time-dependent location, univariate GEV approach



*Estimated 5-y ret levels of daily maximum temperature in summer. Data from the last 5 decades. Source: Toreti, 2010*

# Characterising III

(partially) non-stationary approach



*Estimated 50-y ret levels of daily precipitation in autumn. Data from 2001-2010.  
Source: Naveau et al. 2014, WRR 50*

# Characterising III

## EVT - GP family

$$\bar{G}_{\sigma,\xi}(y) = 1 - G_{\sigma,\xi}(y) = \begin{cases} (1 + \xi \frac{y}{\sigma})^{-1/\xi} & \text{if } \xi \neq 0, \\ \exp(-\frac{y}{\sigma}) & \text{if } \xi = 0. \end{cases}$$

$\sigma(\mathbf{X})$  and assuming  $\xi$  constant

## Probability weighted moments

$$\mu_r(\mathbf{X}) = \mathbb{E}[Y(\mathbf{X})\bar{G}_{\sigma(\mathbf{X}),\xi}^r(Y(\mathbf{X}))] \quad \text{where } Y(\mathbf{X}) \text{ follows } GP(\sigma(\mathbf{X}), \xi)$$

$$\mu_r(\mathbf{X}) = \sigma(\mathbf{X}) \frac{1}{(1+r)(1+r-\xi)}$$

# Characterising III

$$\mu_r(\mathbf{X}) = \sigma(\mathbf{X})\mathbb{E}[Z\overline{G}_{1,\xi}^r(Z)] \quad Z \sim GP(1, \xi)$$

by using  $\mu_0(\mathbf{X})$ ,  $\mu_r(\mathbf{X})$  and  $\mu_s(\mathbf{X})$

$$\xi = \frac{(1+s)^2 - (1+r)^2\alpha_{rs}}{(1+s) - (1+r)\alpha_{rs}} \quad \text{and} \quad \sigma(\mathbf{X}) = \mu_0(\mathbf{X})(1 - \xi)$$

$$\alpha_{rs} = \frac{\mathbb{E}[Z\overline{G}_{1,\xi}^r(Z)]}{\mathbb{E}[Z\overline{G}_{1,\xi}^s(Z)]}$$

$\xi$  becomes function of only  $\alpha_{r,s}$

# Characterising III

Let  $\hat{\mu}_0(\mathbf{X})$  and  $\hat{\alpha}_{rs}$  be the estimators of  $\mu_0(\mathbf{X})$  and  $\alpha_{rs}$

by selecting  $r = 1$  and  $s = 2$

$$\hat{\xi} = \frac{9 - 4\hat{\alpha}}{3 - 2\hat{\alpha}} \quad \text{and} \quad \hat{\sigma}(\mathbf{X}) = \hat{\mu}_0(\mathbf{X})(1 - \hat{\xi})$$

$$\hat{\mu}_0(\mathbf{X}) = \frac{1}{\sum_i K(\mathbf{X} - \mathbf{X}_i)} \sum_{i=1}^n Y(\mathbf{X}_i) K(\mathbf{X} - \mathbf{X}_i)$$

where  $K$  is a Kernel

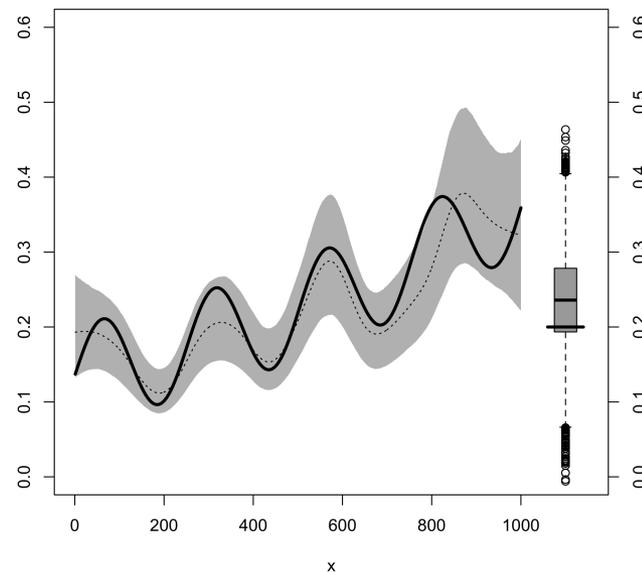
# Characterising III

To estimate  $\alpha_{rs}$

$$Z'_i = Y(\mathbf{X}_i) / \hat{\mu}_0(\mathbf{X}_i)$$

use your favourite method (e.g. U-statistic approach) to estimate

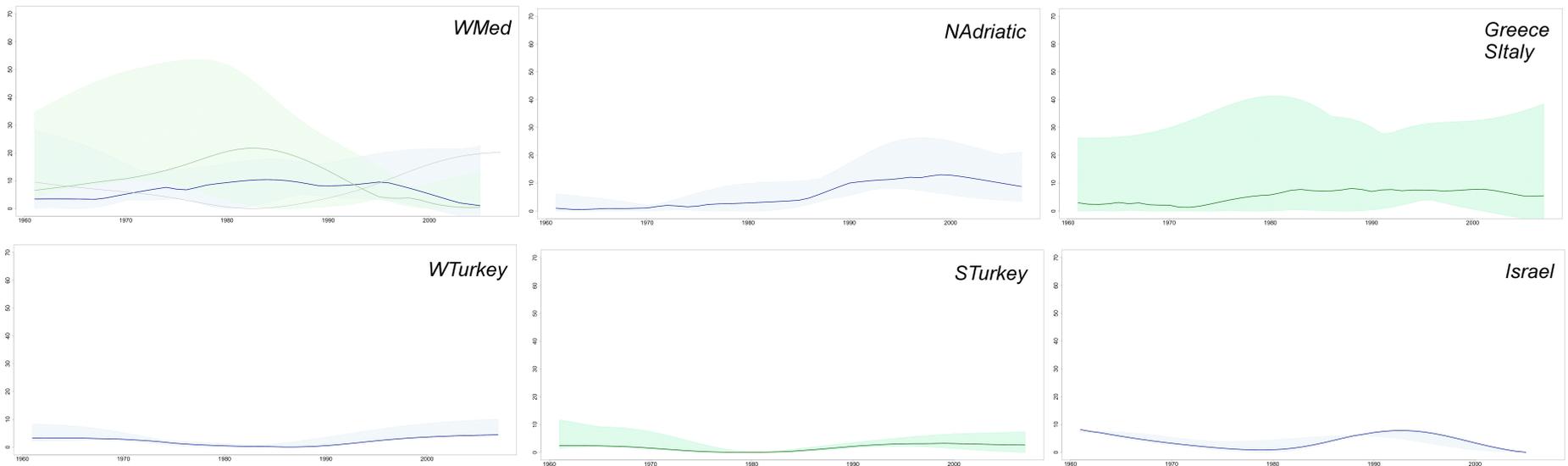
$$\mathbb{E}[Z' \overline{G'}_{1,\xi}^r(Z')] \text{ for } r = 1, 2$$



Source: Naveau et al., 2014. WRR 50

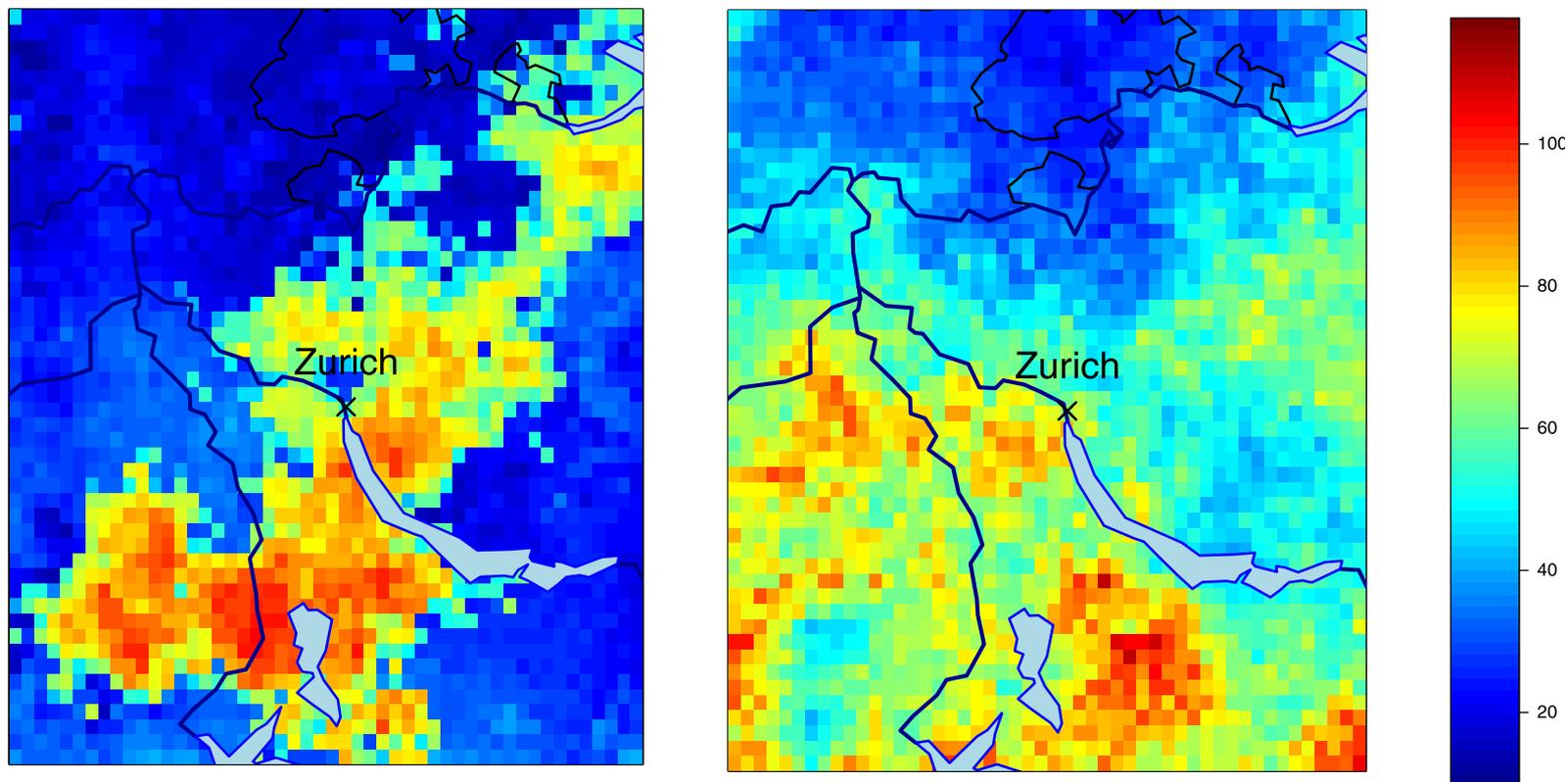
# Characterising III

an attempt to model and understand the temporal evolution of precipitation extremes



# Characterising IV

## Max-stable models



*One realisation from the Schlather and Brown Resnick models applied to daily summer precipitation from 1962 to 2008. Source: Davison et al., 2012. Statistical Science 27*

# Characterising $\mathbf{V}$

$$Y(\mathbf{s}) \sim GEV(\mu(\mathbf{s}), \sigma(\mathbf{s}), \xi(\mathbf{s}))$$

$$Y(\mathbf{s}) = \mu(\mathbf{s}) + \frac{\sigma(\mathbf{s})}{\xi(\mathbf{s})} [X(\mathbf{s})^{\xi(\mathbf{s})} - 1]$$

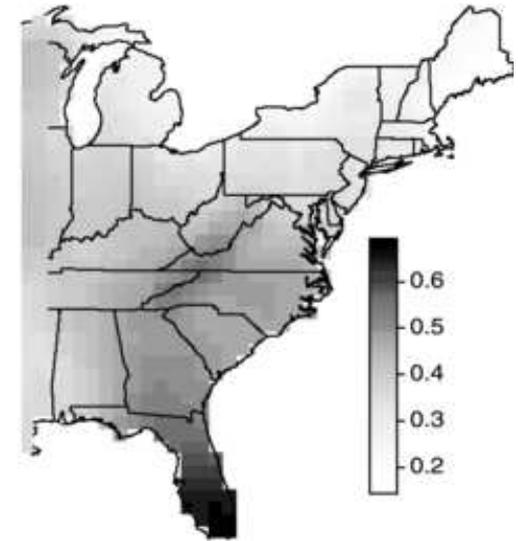
$$X(\mathbf{s}) = U(\mathbf{s})\theta(\mathbf{s}) \text{ with } U(\mathbf{s}) \sim GEV(1, \alpha, \alpha)$$

$$\theta(\mathbf{s}) = \left[ \sum_{l=1}^L A_l w_l(\mathbf{s})^{1/\alpha} \right]^\alpha \text{ with } A_l \sim PS(\alpha)$$

$$Y(\mathbf{s}_i) | A_1, \dots, A_2, \dots, A_L \sim_{indep} GEV[\mu^*(\mathbf{s}_i), \sigma^*(\mathbf{s}_i), \xi^*(\mathbf{s}_i)]$$

Hierarchical spatial model for precipitation extremes

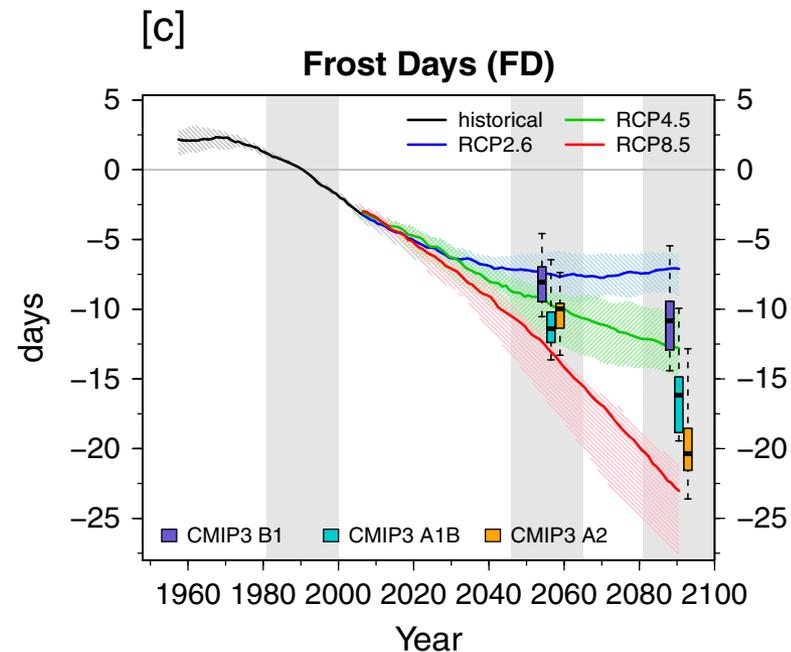
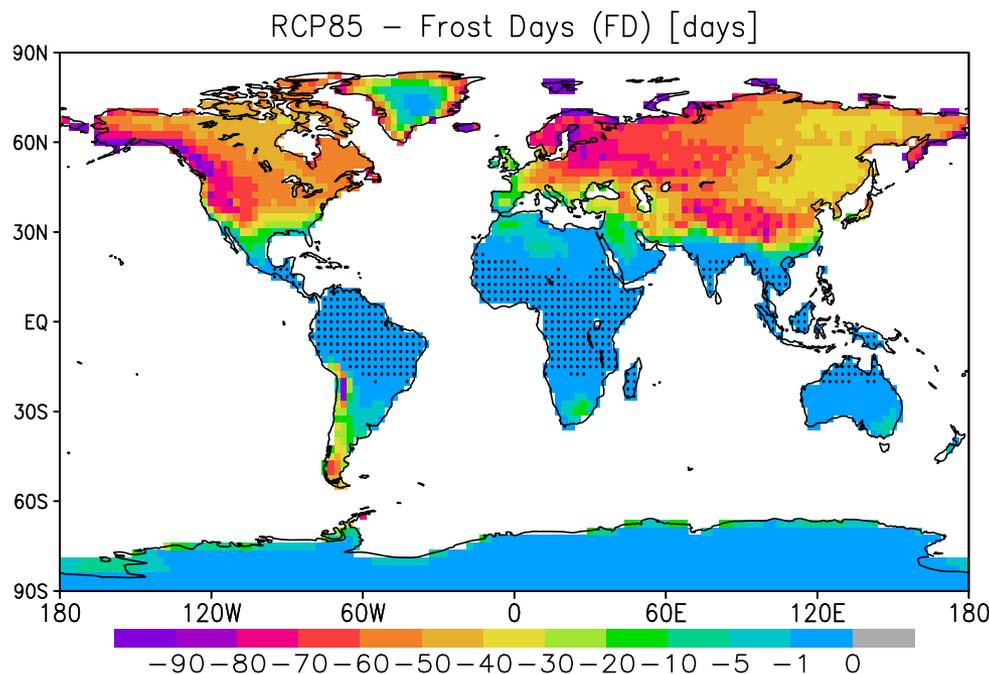
Source: Reich and Shalby 2012. Ann. Appl. Stat. 6



(c) GEV shape,  
posterior mean

# Characterising VI

## Index-based approach



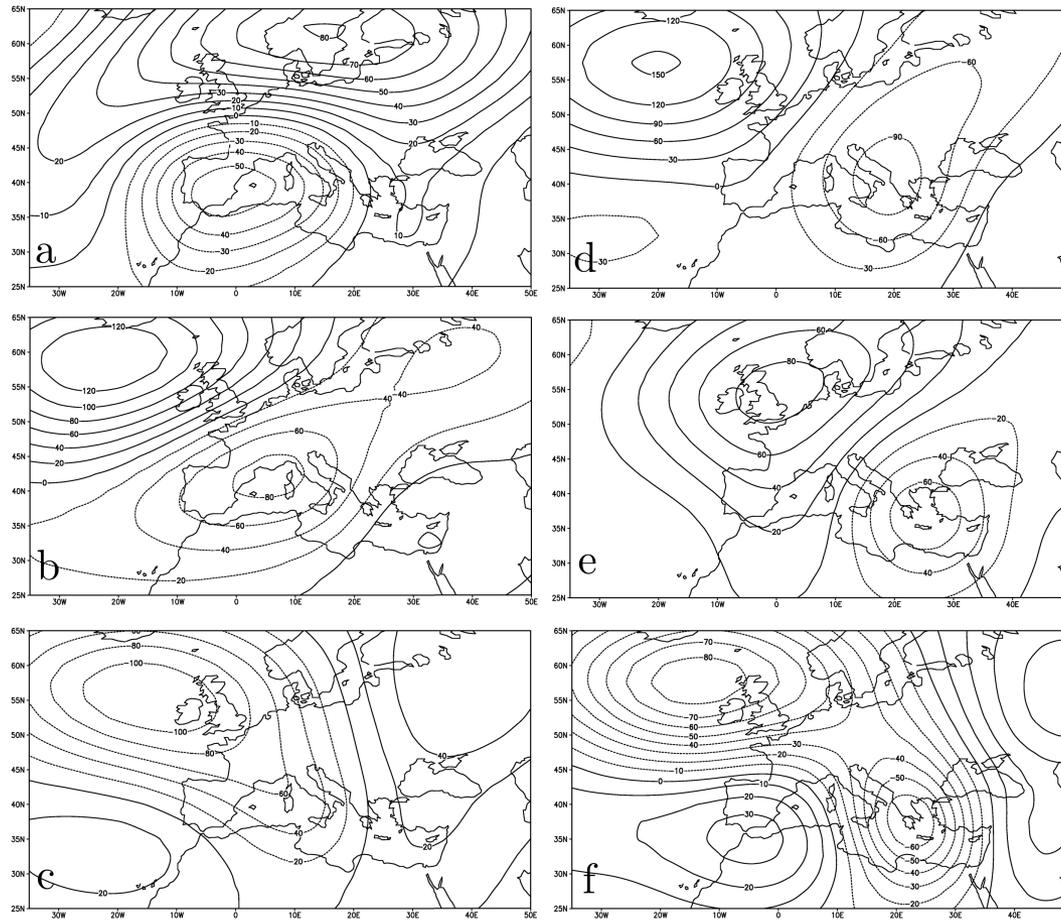
2081-2100 Changes w.r.t. 1981-2000. Source: Sillmann et al. 2013, JGR 118

# Characterising

- Erroneous data
- Inhomogeneities
- Missing data
- inhomogeneous spatial coverage
- Complexity of the events is often not captured
- Computational and statistical issues when dealing with large data sets
- Constraints and assumptions for large regions

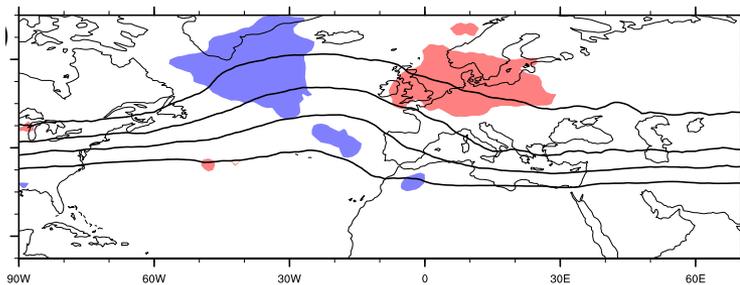
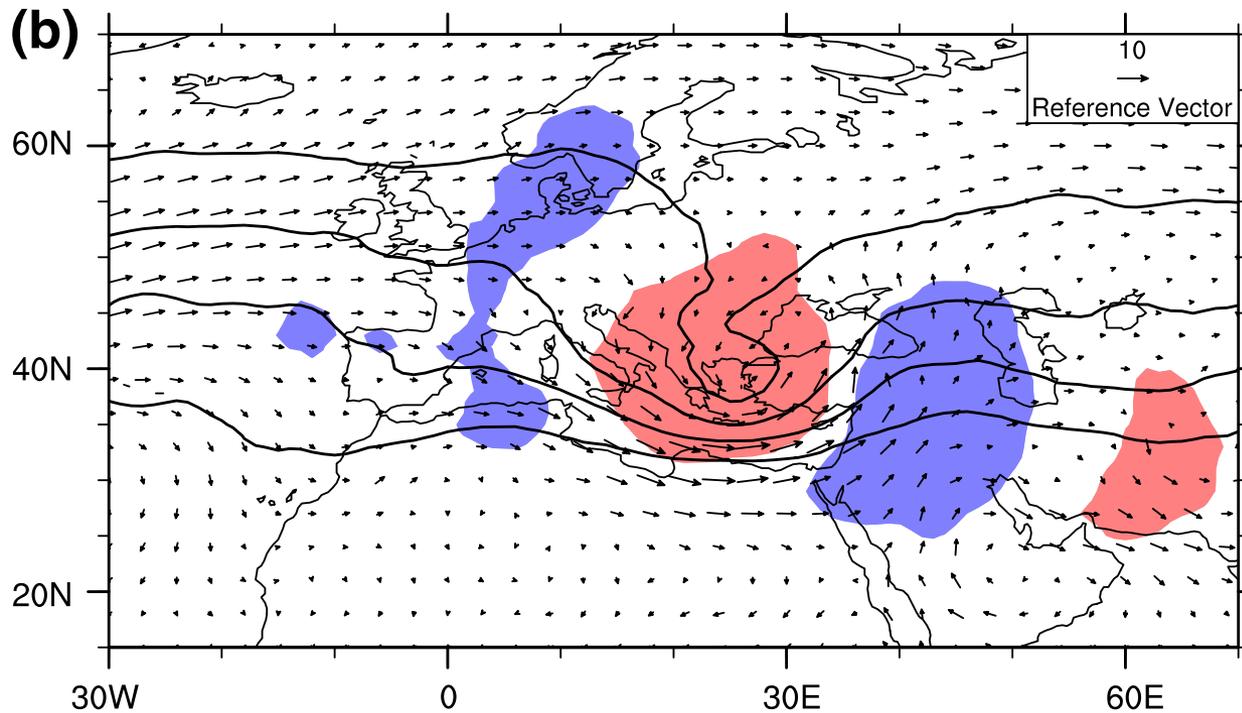
# Predicting I

## Synoptic patterns associated with extreme preci



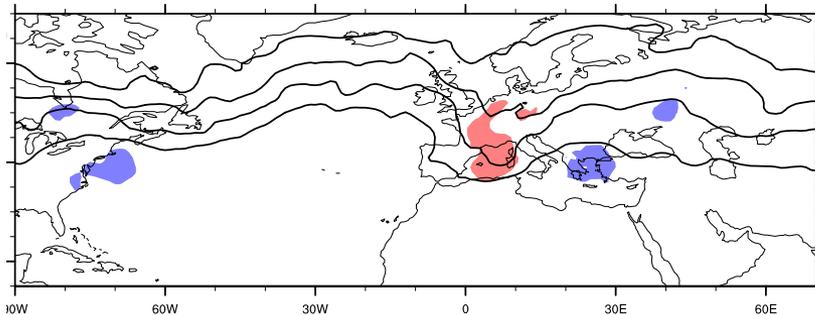
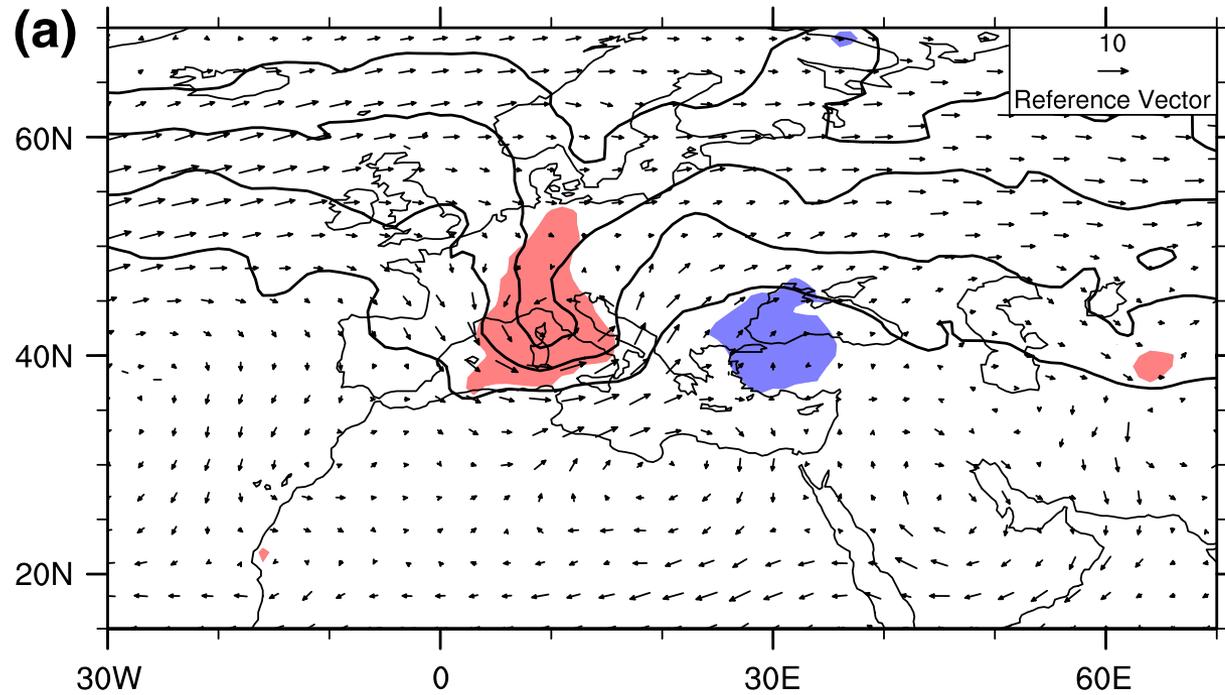
Z500 anomalies associated with precipitation extremes. Source: Toreti et al., 2010. NHESS 10

# Predicting I



*PV anomalies and wind at 850 hPa DJF associated with precip extremes in Western Turkey. Source: Toreti et al. 2016, Climate Dynamics in press*

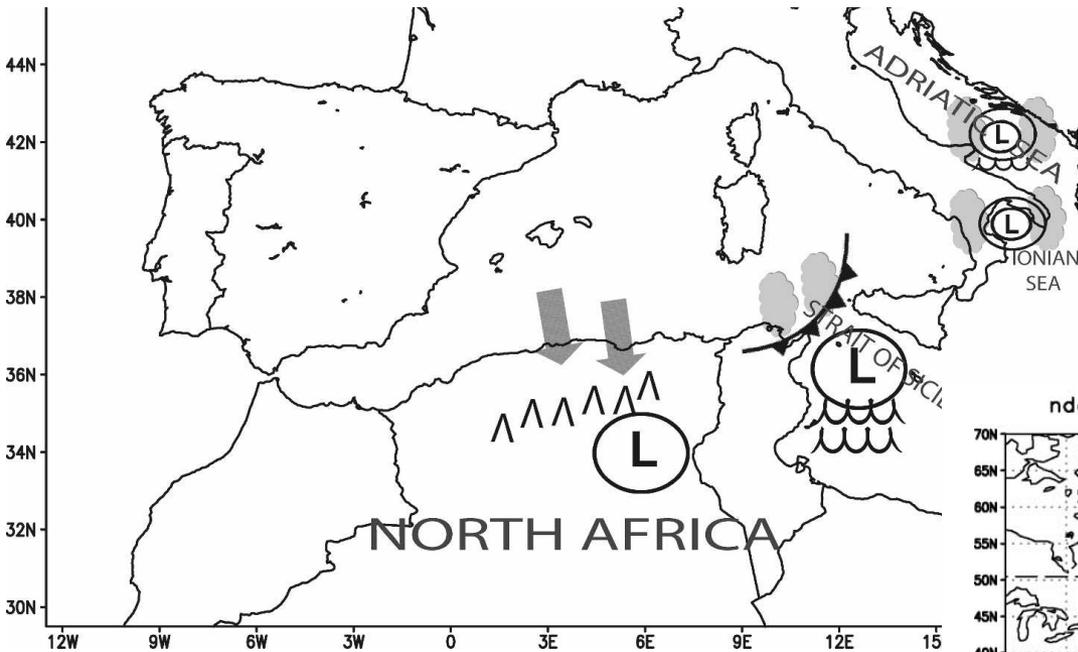
# Predicting I



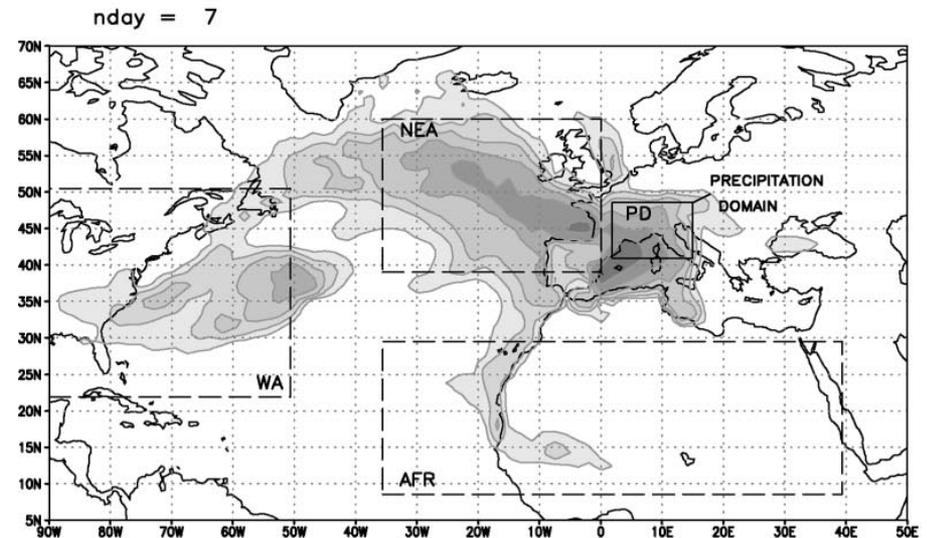
*PV anomalies and wind at 850 hPa DJF associated with precip extremes in Po Valley. Source: Toreti et al. 2016, Climate Dynamics in press*

# Predicting I

*Other factors contributing to precipitation extremes*

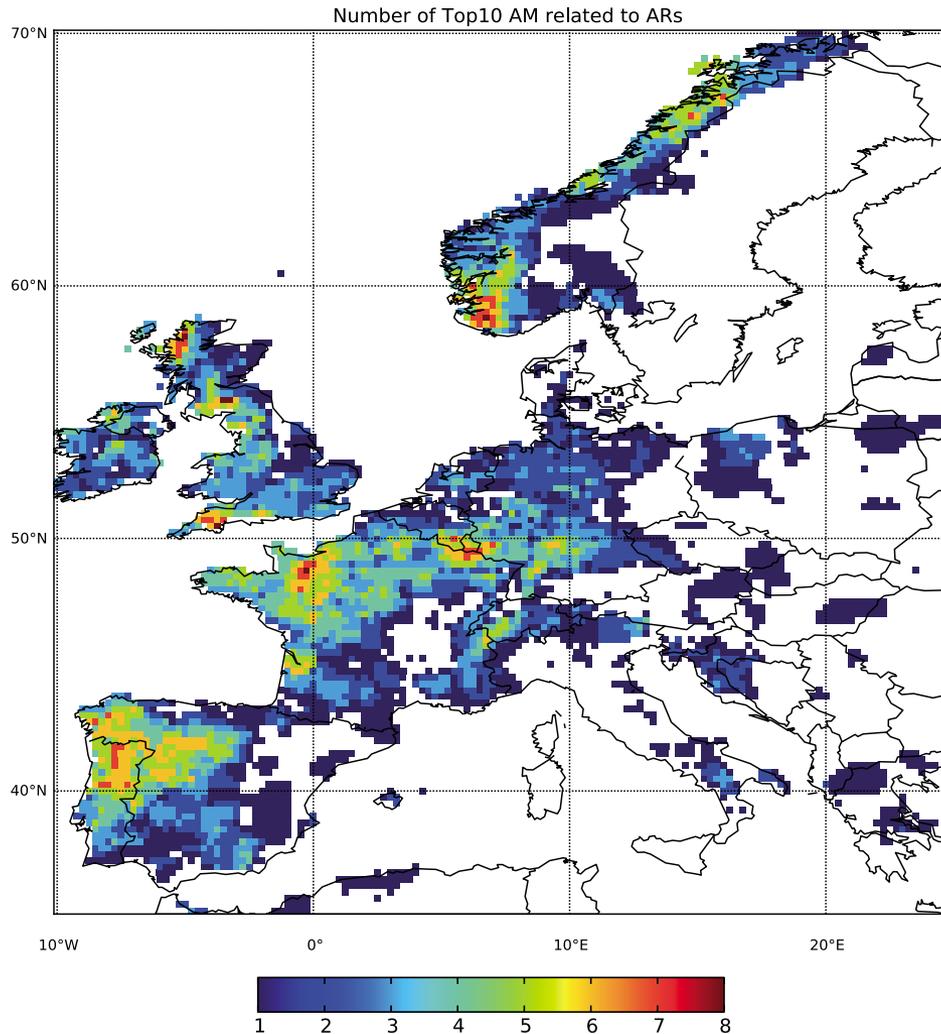


Source: Moscatello et al., 2008. MWR 136



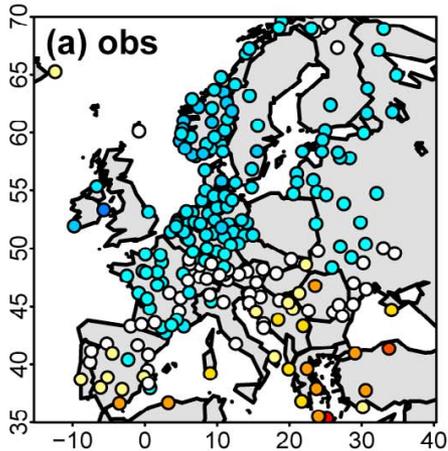
Source: Turato et al., 2004. J Hydromet 5

# Predicting I

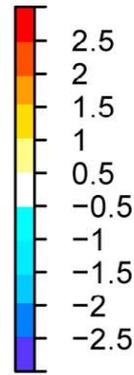


# Predicting II

## Cold Spell winter 2009-10

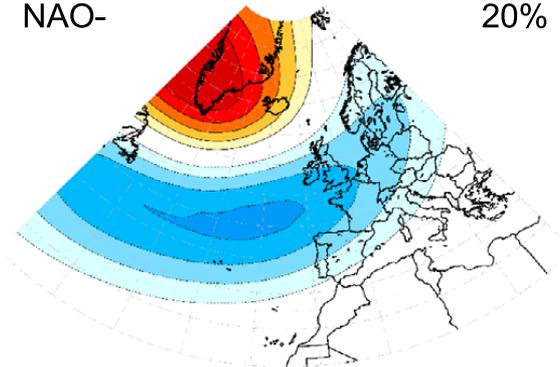


Normalised winter temperature anomalies

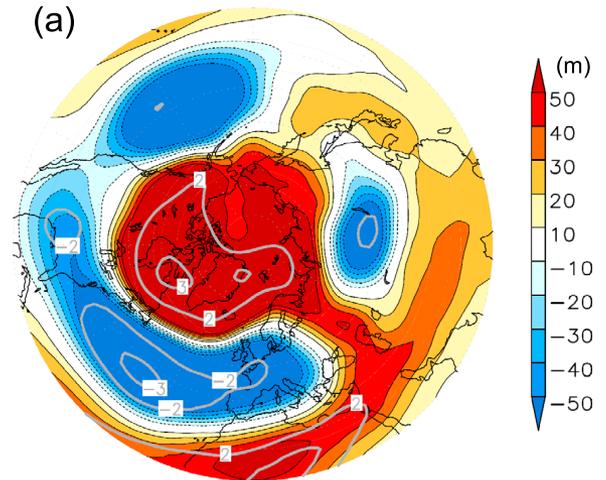


NAO-

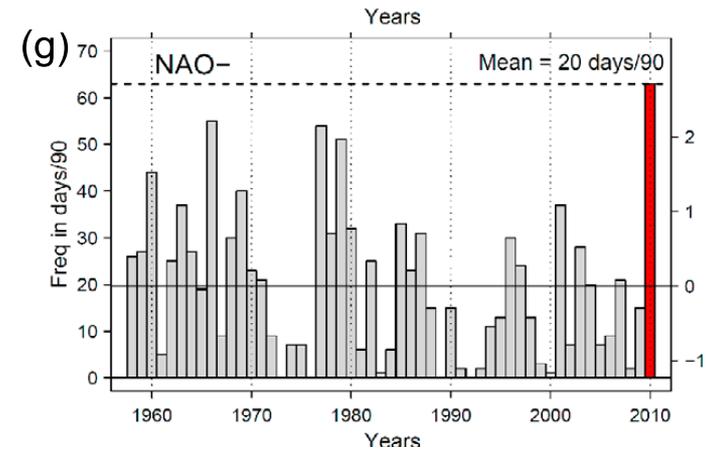
20%



Negative NAO

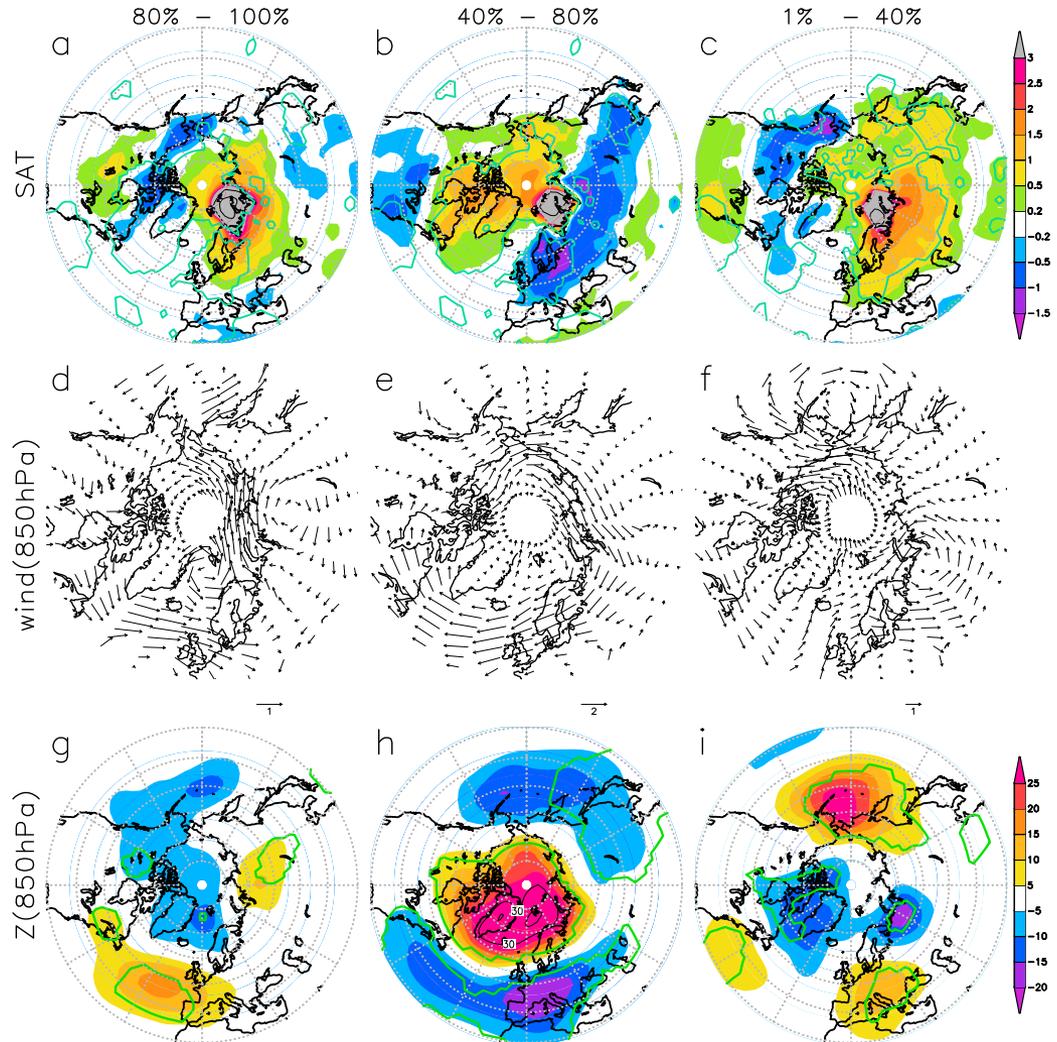
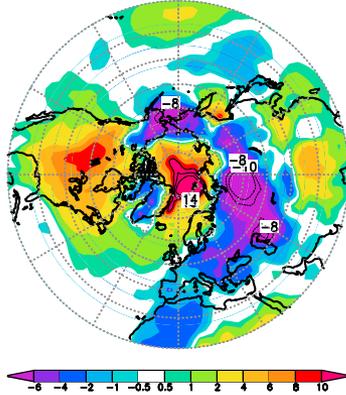


Anomalies of Z500



# Predicting II

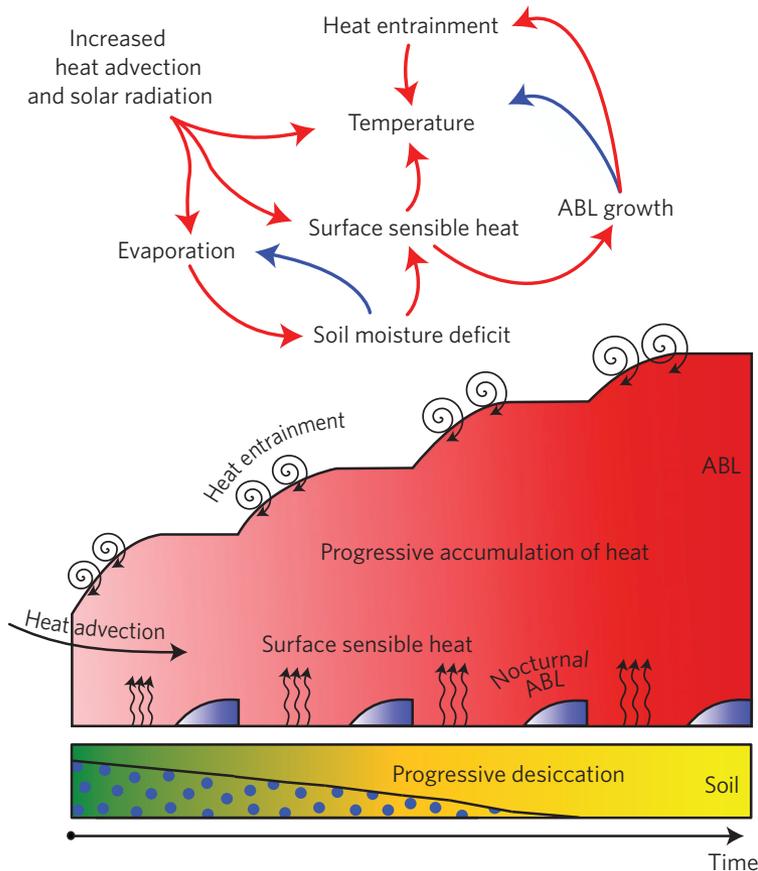
a) Jan 2006 SAT anom.



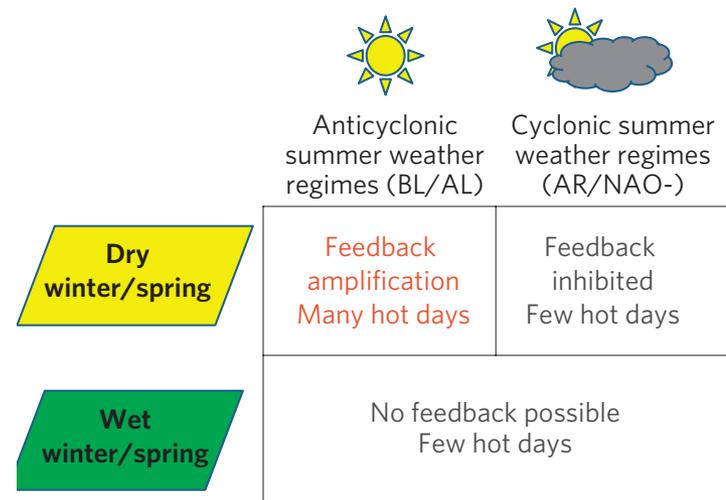
*Nonlinear response to decrease in the Barents-Kara sea ice concentration.*

*Source: Petoukhov and Semenov 2010, JGR 115*

# Predicting III

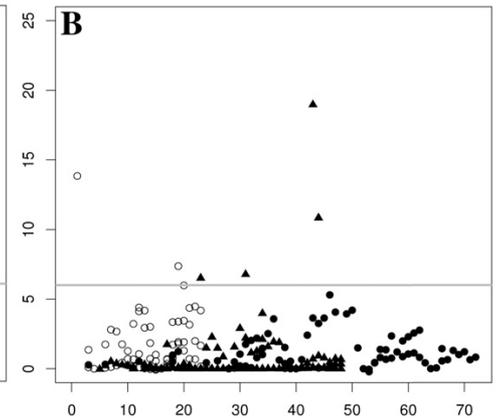
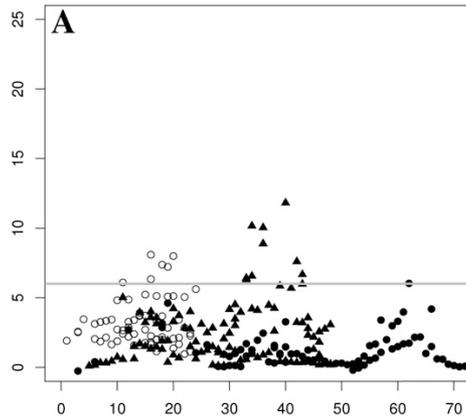
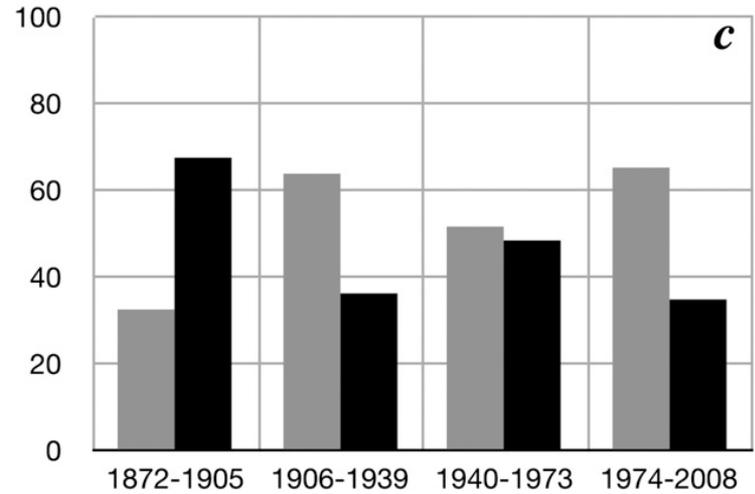
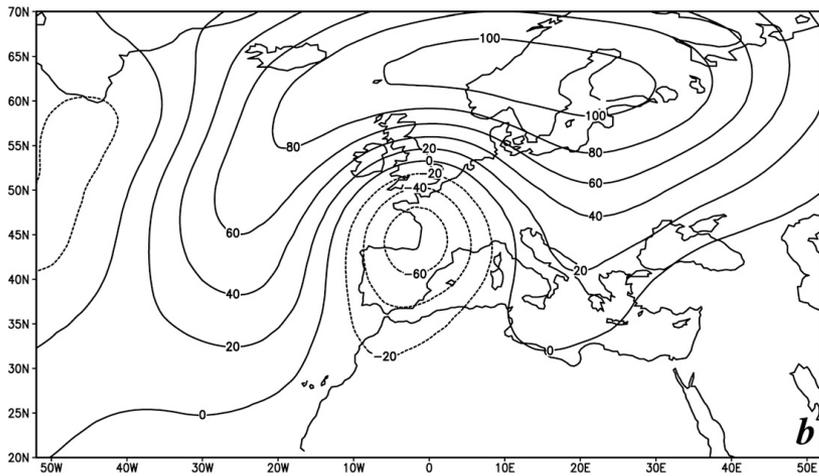
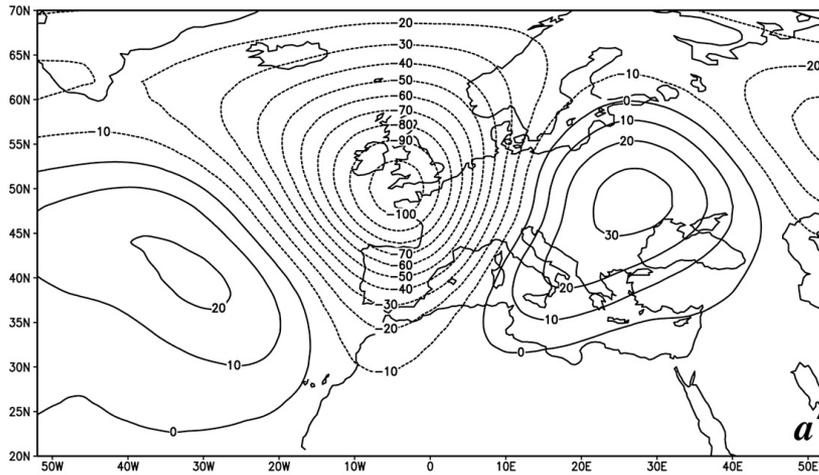


Soil moisture - air temperature interaction in the development of mega heat waves. Source: Miralles et al. 2014, Nature Geoscience 7.



Sensitivity of hot days to summer atm circulation and soil moisture conditions. Source: Quesada et al. 2012, NCC 2.

# Predicting IV

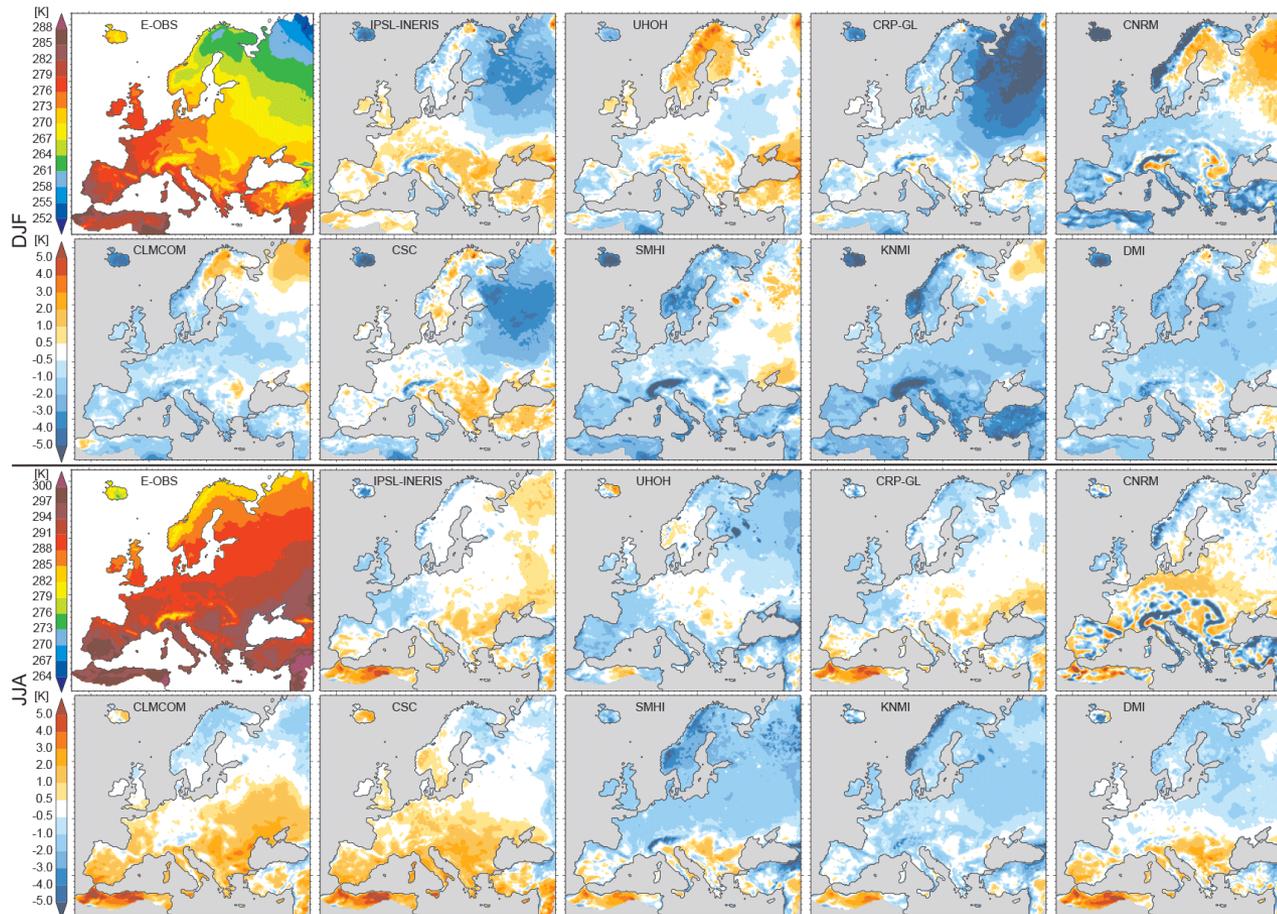


*Z500 anomalies associated with Debris Flows in the souther Swiss Alps and convective time scales. Source: Toreti et al. 2013, JAMC 52*

# Predicting

- Interactions of different phenomena acting at different spatio-temporal scales
- coarse resolution of available reanalyses
- nonlinear processes

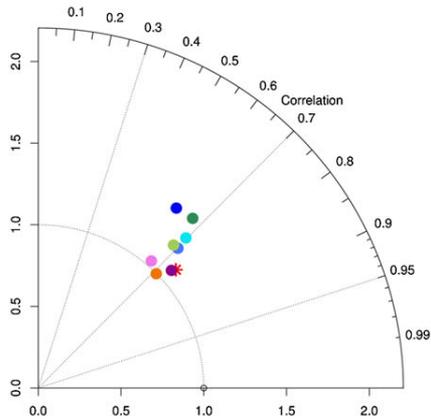
# Evaluating I



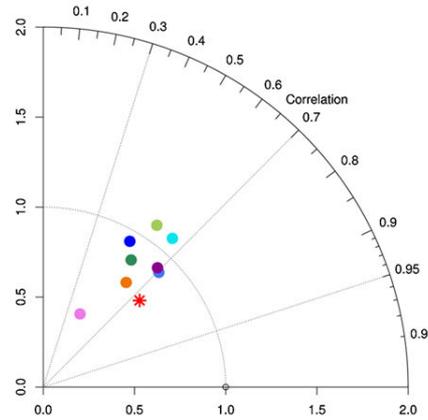
*Bias in mean seasonal temperature of EUR-11 cordex runs 1989-2008.  
Source: Kotlarski et al. 2014, Geosci. Model Dev., 7*

# Evaluating II

**c**



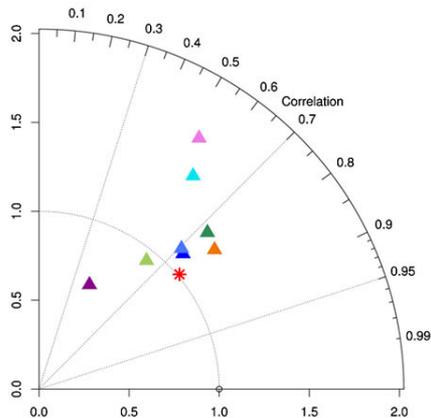
**e**



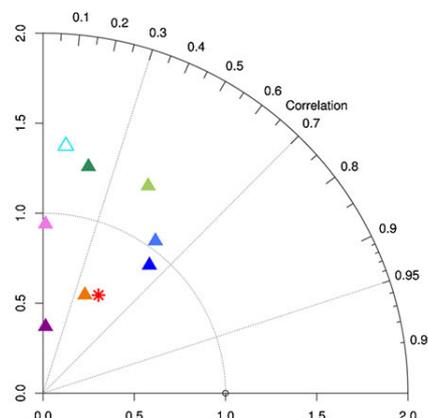
- CMCC
- HadES
- MIROC
- CNRM
- INM
- MRI
- \* ensemble mean
- HadCC
- IPSL

*Taylor diagrams for estimated 50 year return levels in winter and summer over (c, d) northern Eurasia and (e, f) North America . Source: Toreti et al. 2013, GRL 40.*

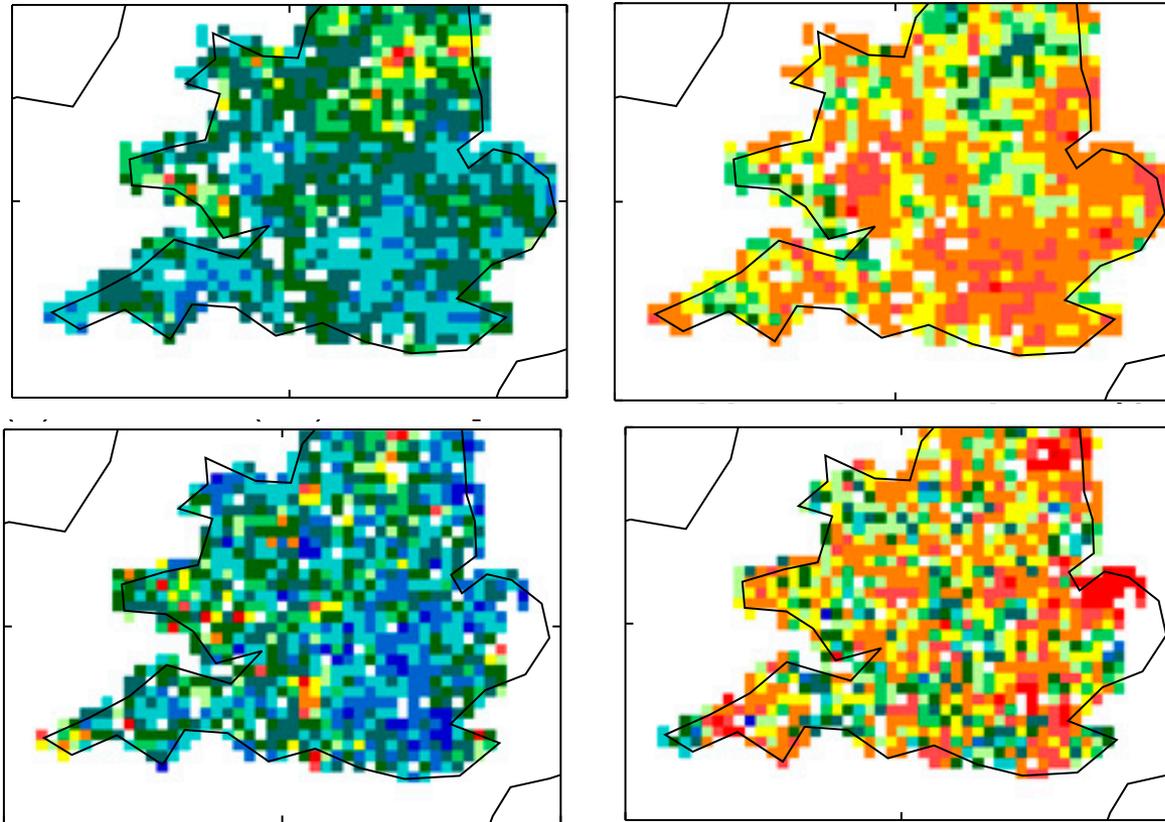
**d**



**f**



# Evaluating III



*Estimated GPD parameters for winter (DJF) precipitation extremes. Model w.r.t. observations  
Source: Chan et al. 2014, J Clim 27*

# Evaluating IV

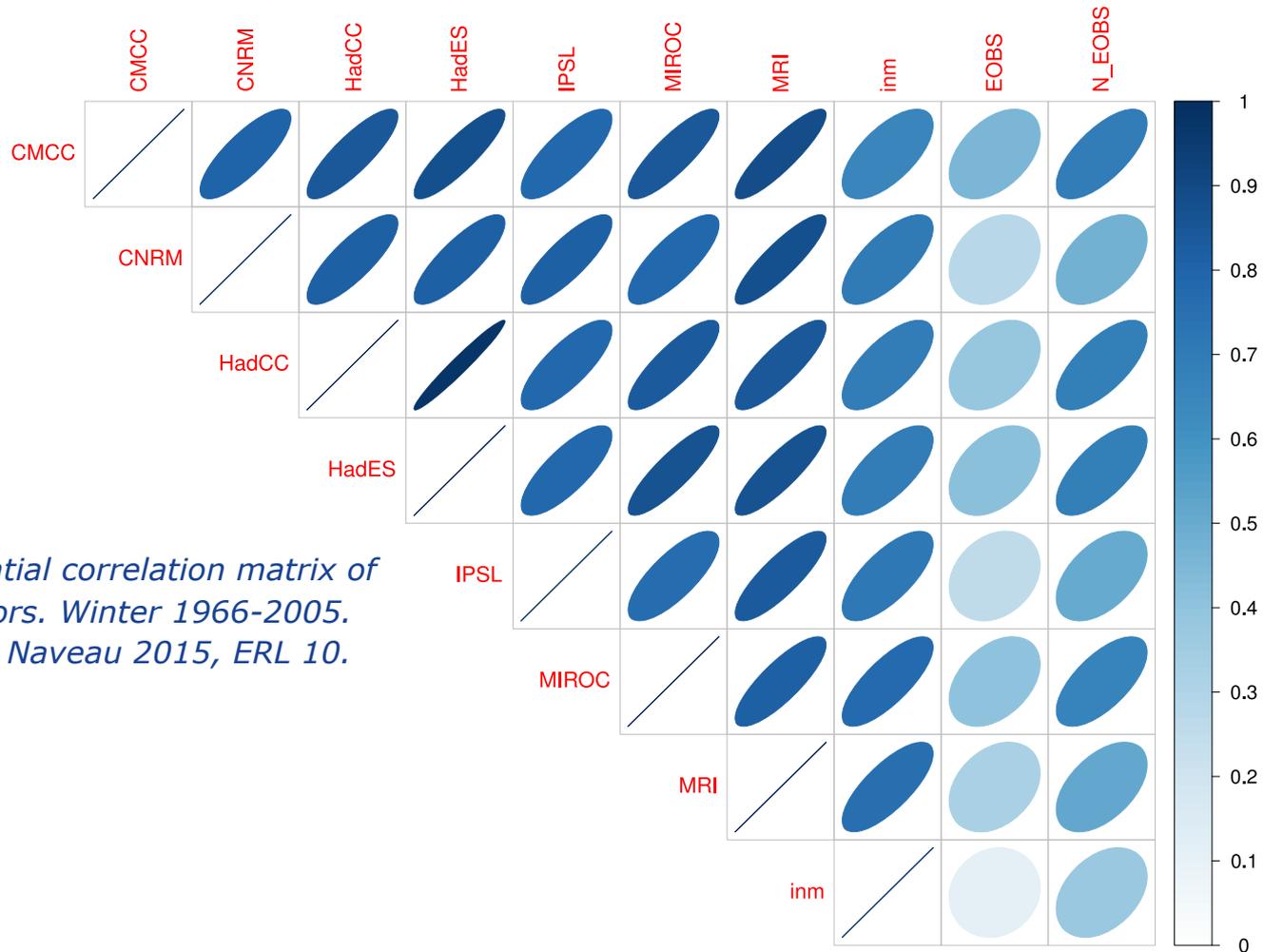
non-parametric approach

$$A = \frac{mn}{N} \int_{-\infty}^{\infty} \frac{(\bar{G}_m - \bar{F}_n)^2}{(\bar{H}_N)} dH_N$$
$$\bar{H}_N = \frac{n\bar{F}_n + m\bar{G}_m}{N}; \quad N = n + m$$

$$T = (A - \mathbb{E}(A))\sigma_A^{-1}$$

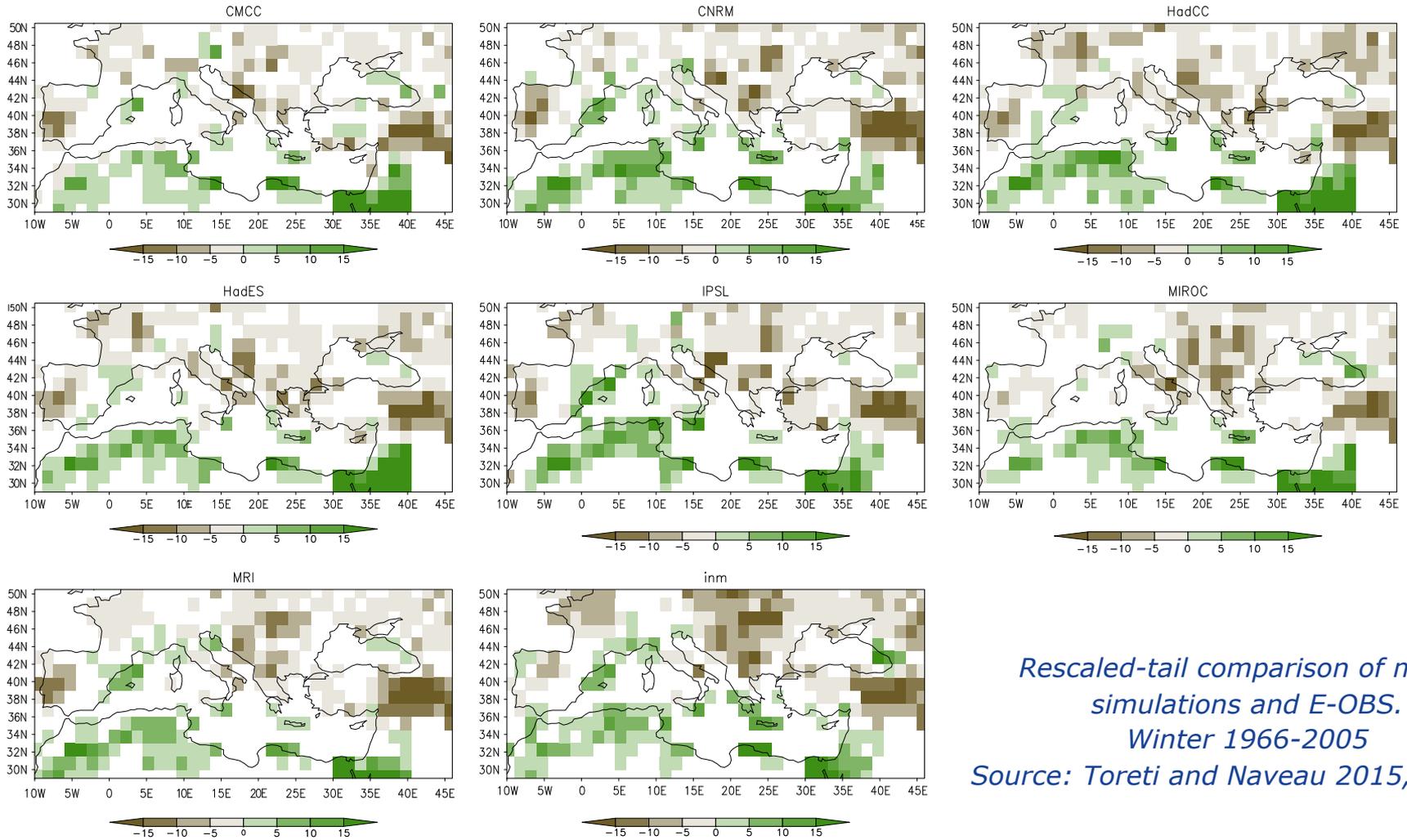
$$I(f_e; g_e) = \mathbb{E}_{f_e} \left\{ \log \left( \frac{f_e(X_e/\mu_0^{X_e})}{g_e(X_e/\mu_0^{X_e})} \right) \right\}$$

# Evaluating IV



*Spearman-based spatial correlation matrix of the tail scaling factors. Winter 1966-2005. Source: Toreti and Naveau 2015, ERL 10.*

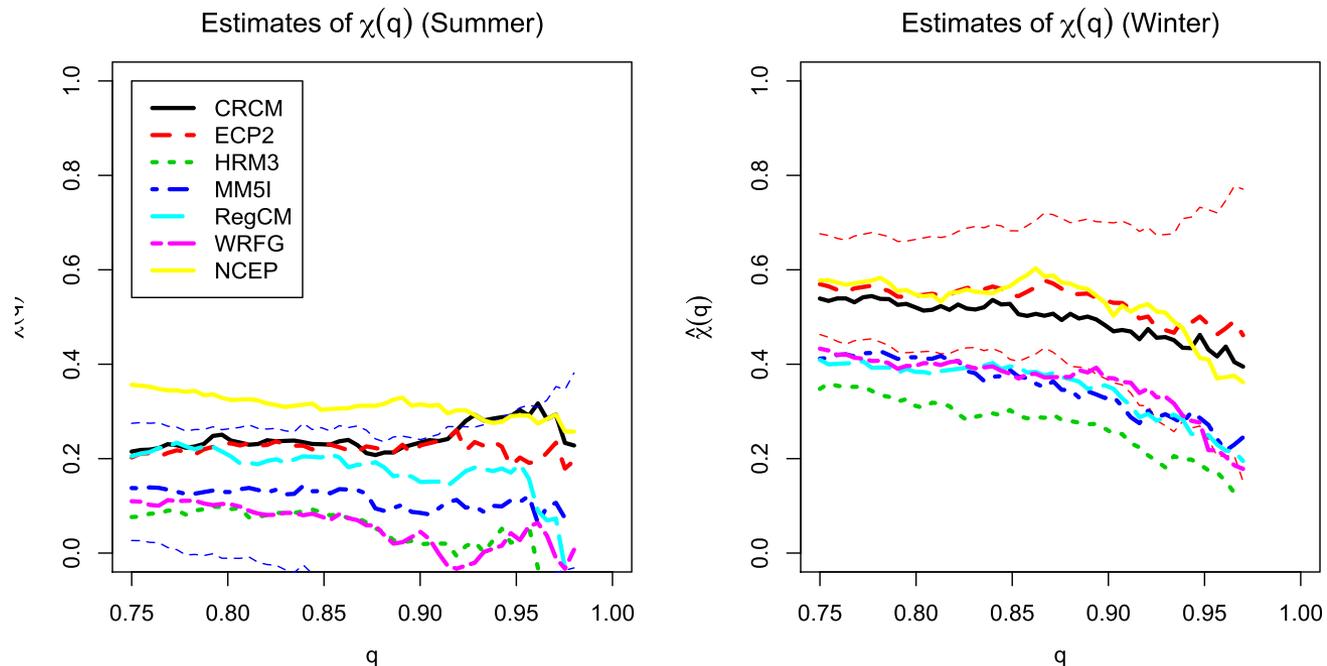
# Evaluating IV



*Rescaled-tail comparison of model  
simulations and E-OBS.  
Winter 1966-2005  
Source: Toreti and Naveau 2015, ERL 10.*

# Evaluating V

$$\chi(q) = 2 - \frac{\log \mathbb{P}(Z_2 < z_q, Z_1 < z_q)}{\log \mathbb{P}(Z_2 < z_q)}$$

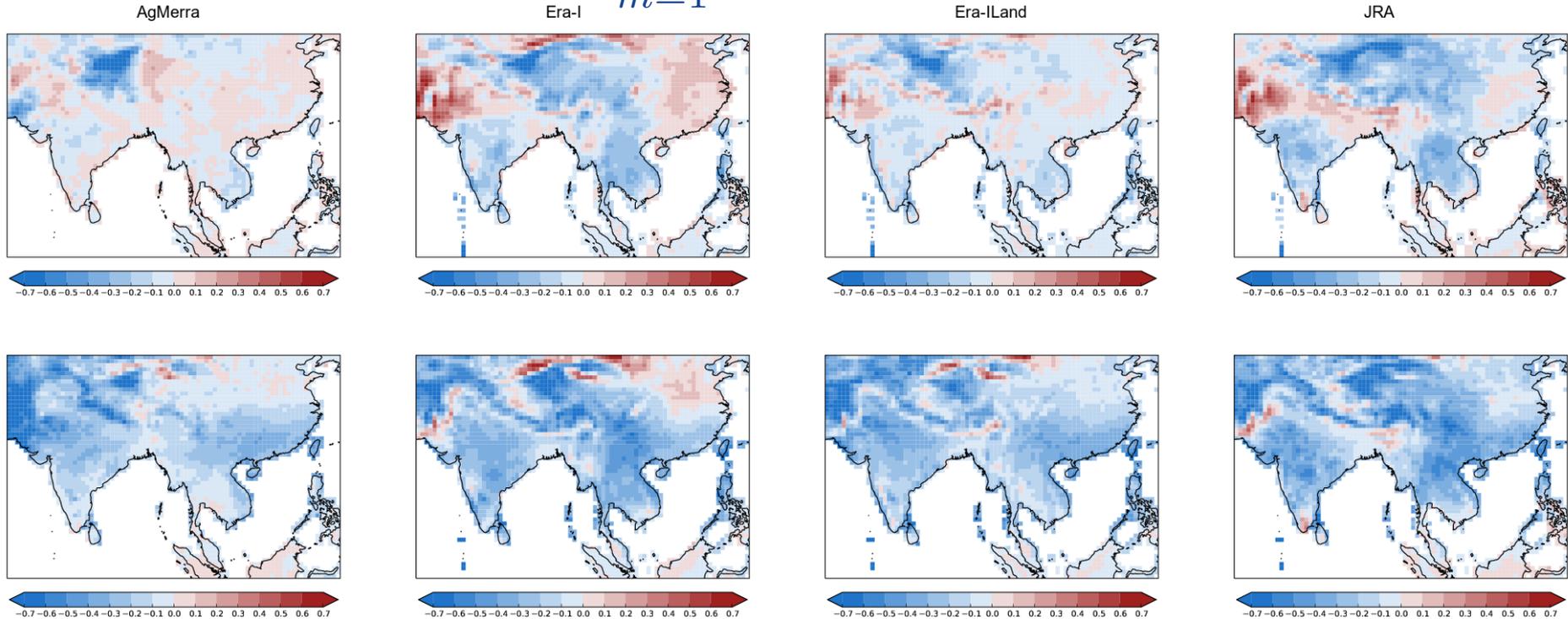


*Tail dependence of NARCCAP RCMs w.r.t NCEP reanalysis over Pacific region.*

*Source: Weller et al. 2013, JGR 118.*

# Evaluating VI

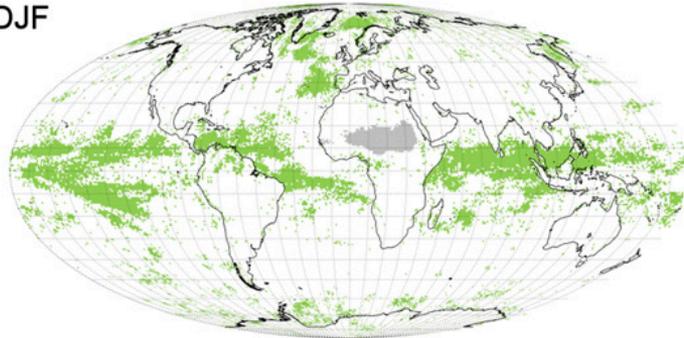
$$D(x) = \sum_{m=1}^{12} p_m(x) \log_2 (12 p_m(x))$$



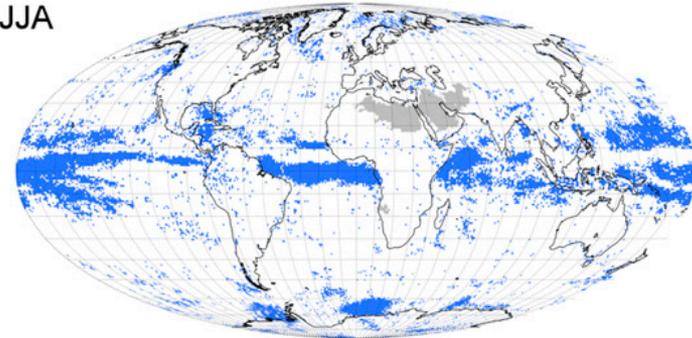
*Comparison of estimated precipitation seasonality of reanalyses with Aphrodite and Chirps. Source: Ceglar et al. 2016, submitted.*

# Evaluating VII

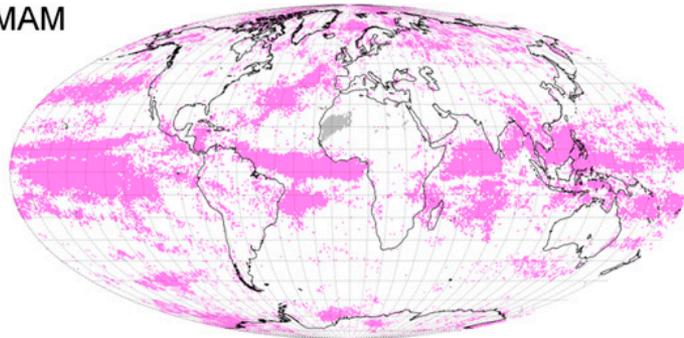
DJF



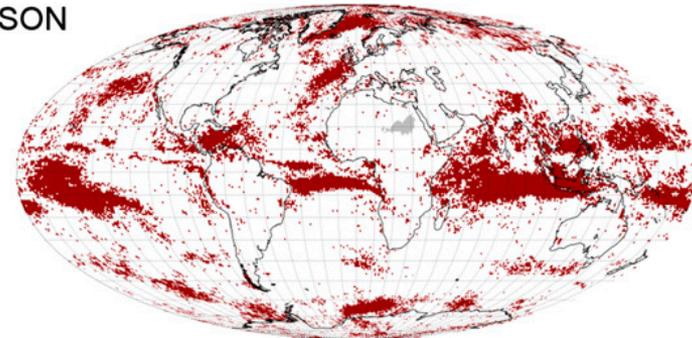
JJA



MAM

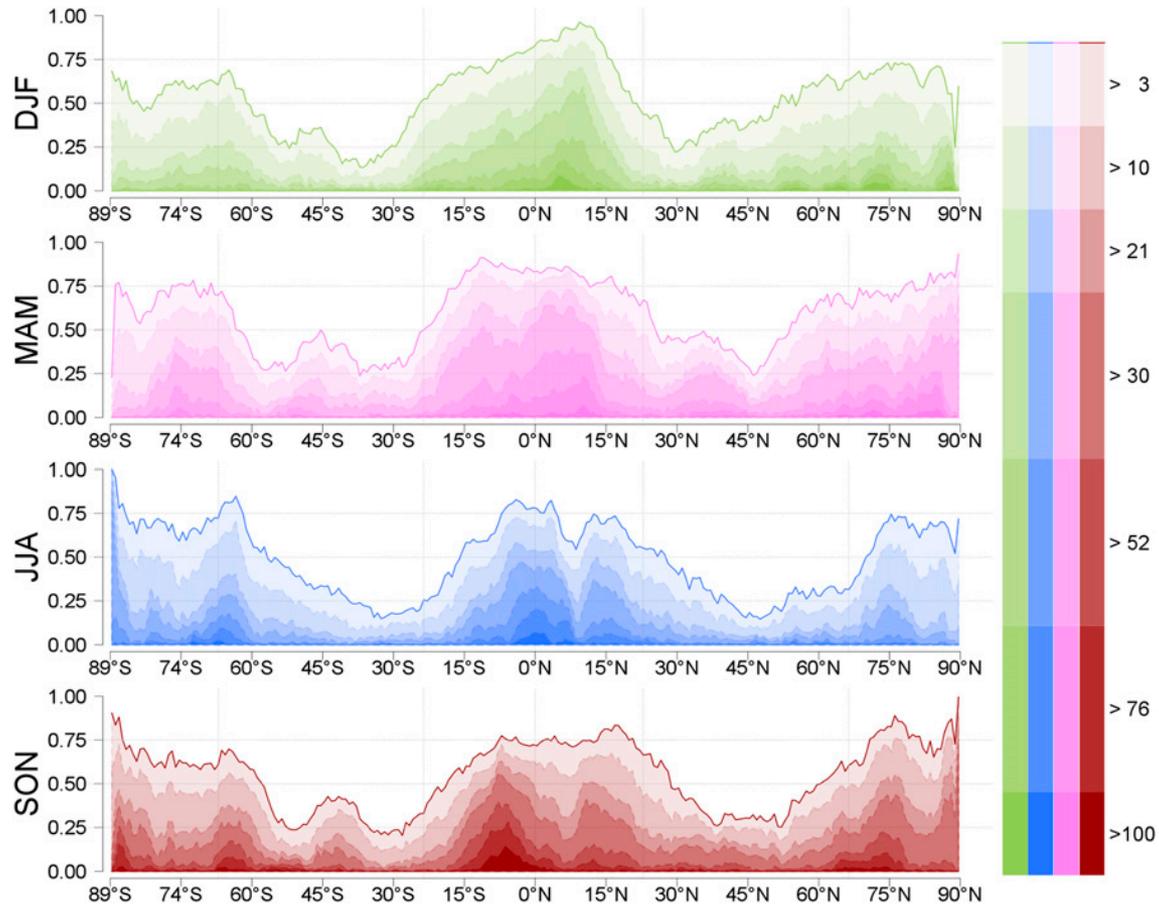


SON



*Seasonal maps of points having a minimal length to estimate internal variability longer than 30 years. Source: Schindler et al. 2015, J Climate 28*

# Evaluating VII

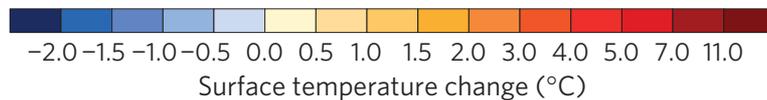
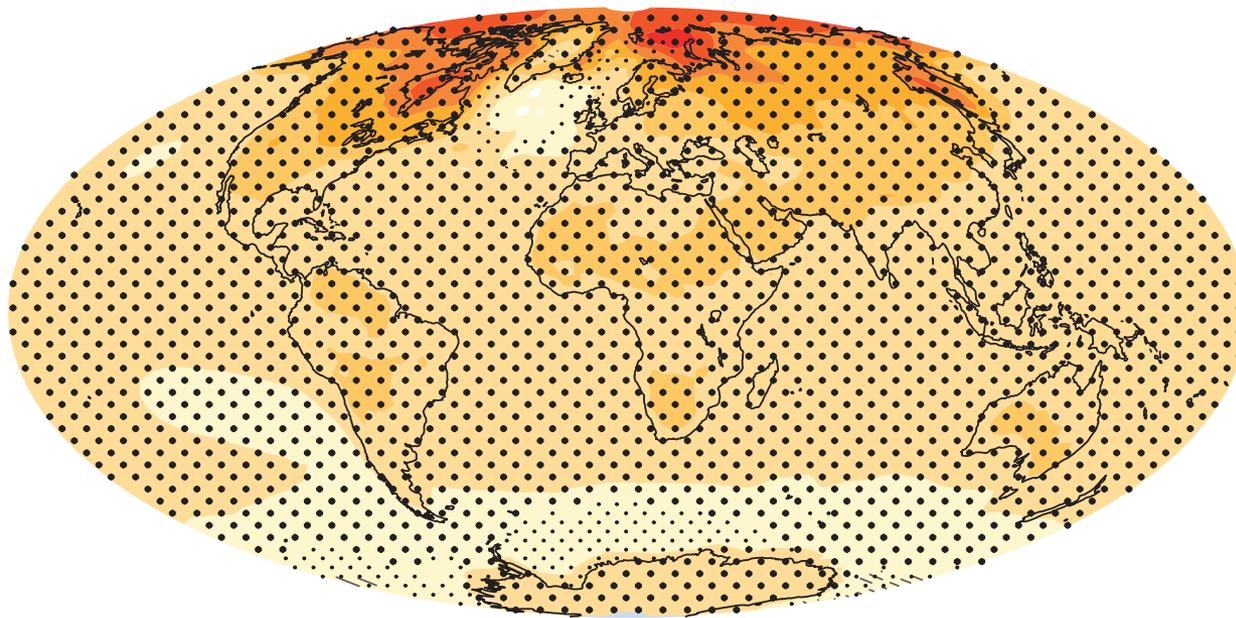


*Zonal plots of % of points having minimum length longer than some fixed thresholds. Source: Schindler et al. 2015, J Climate 28*

# Evaluating VIII

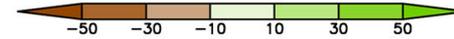
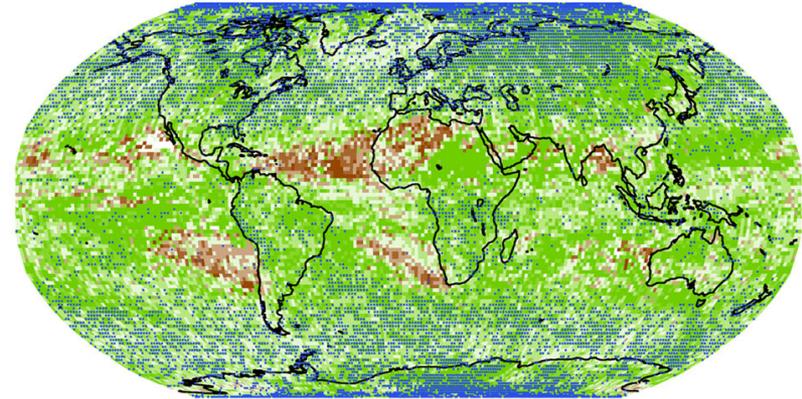
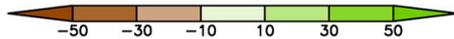
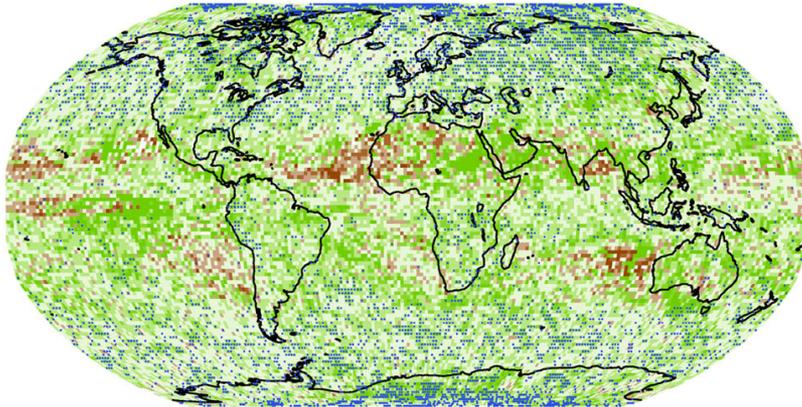
RCP85: 2016–2035

DJF

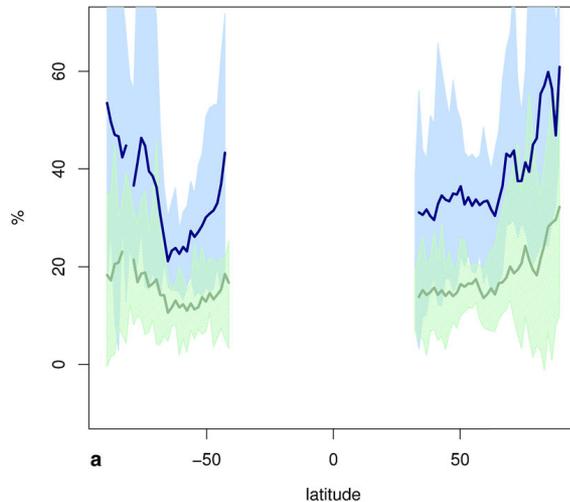


*Temperature changes w.r.t. 1986-2005. Source: Knutti and Sedlacek 2013, NCC1716*

# Evaluating IX



*Ensemble mean changes under RCP8.5. 2020-2059 and 2060-2099 w.r.t. 1986-2005 during winter. Source: Toreti et al., 2013*

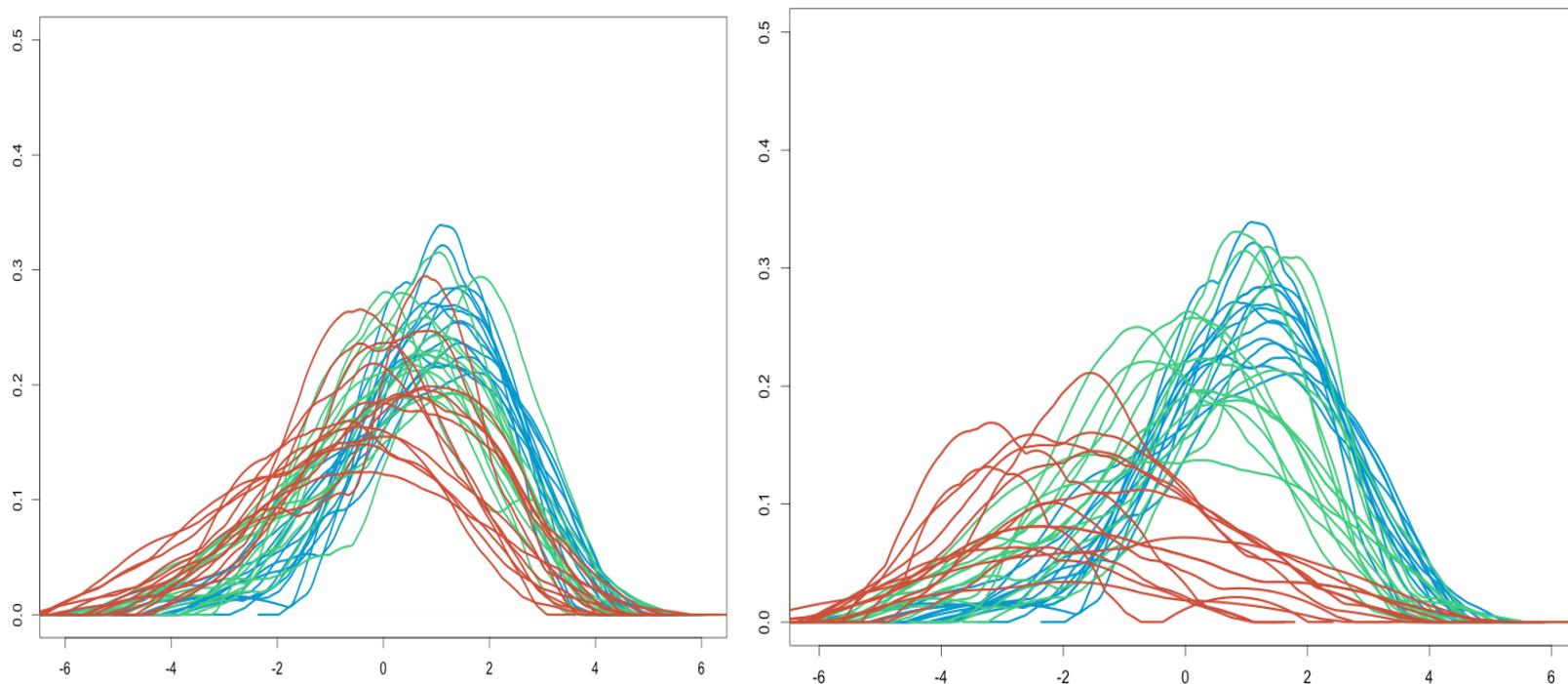


**Changes in 50-y ret. levels of extreme precipitation**

*Zonal mean changes under RCP8.5. 2020-2059 (green) and 2060-2099 (blue) w.r.t. 1986-2005 during winter. Source:*

*Toreti et al. 2013, GRL 40*

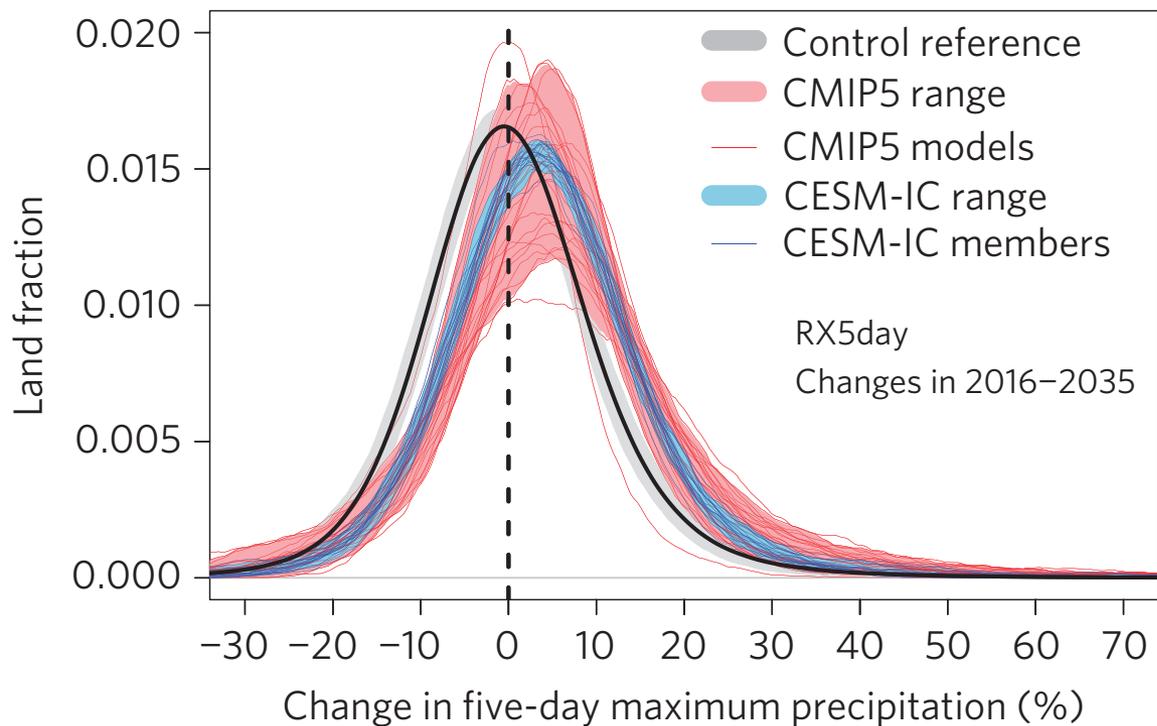
# Evaluating X



*Estimated PDFs of the (transformed) spatial extension of early cold spells over Europe. Blue lines are associated with the historical simulation (1976-2005), green lines with the mid-century (2020-2049) and red lines with the end of the century (2070-2099). Left Panel: RCP4.5. Right Panel: RCP8.5.*

*Source: Toreti et al., in preparation*

# Evaluating XI



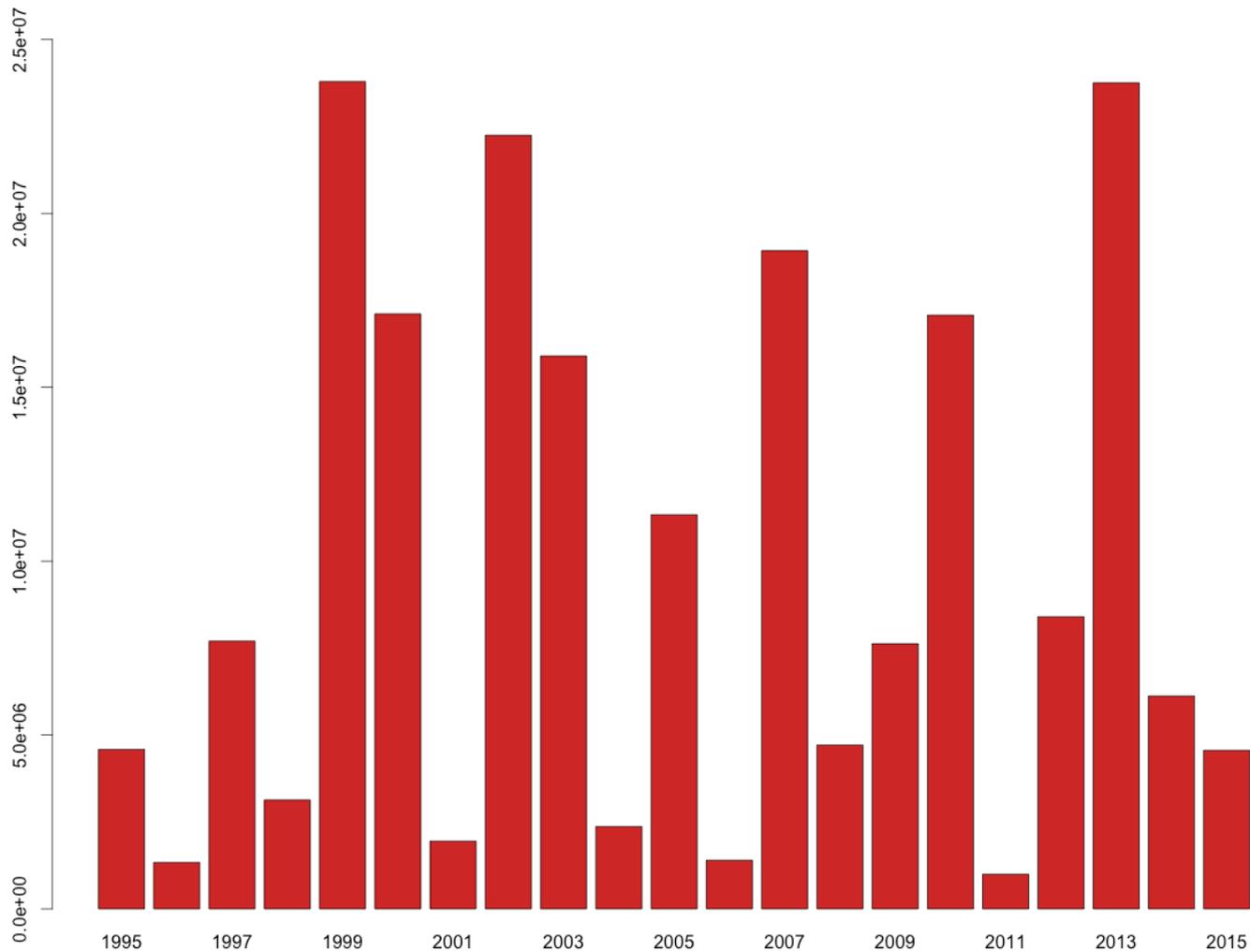
*Spatial pdfs of changes in land points 66° N - 66° S*

*Source: Fischer et al. 2013, NCC 3*

# Evaluating

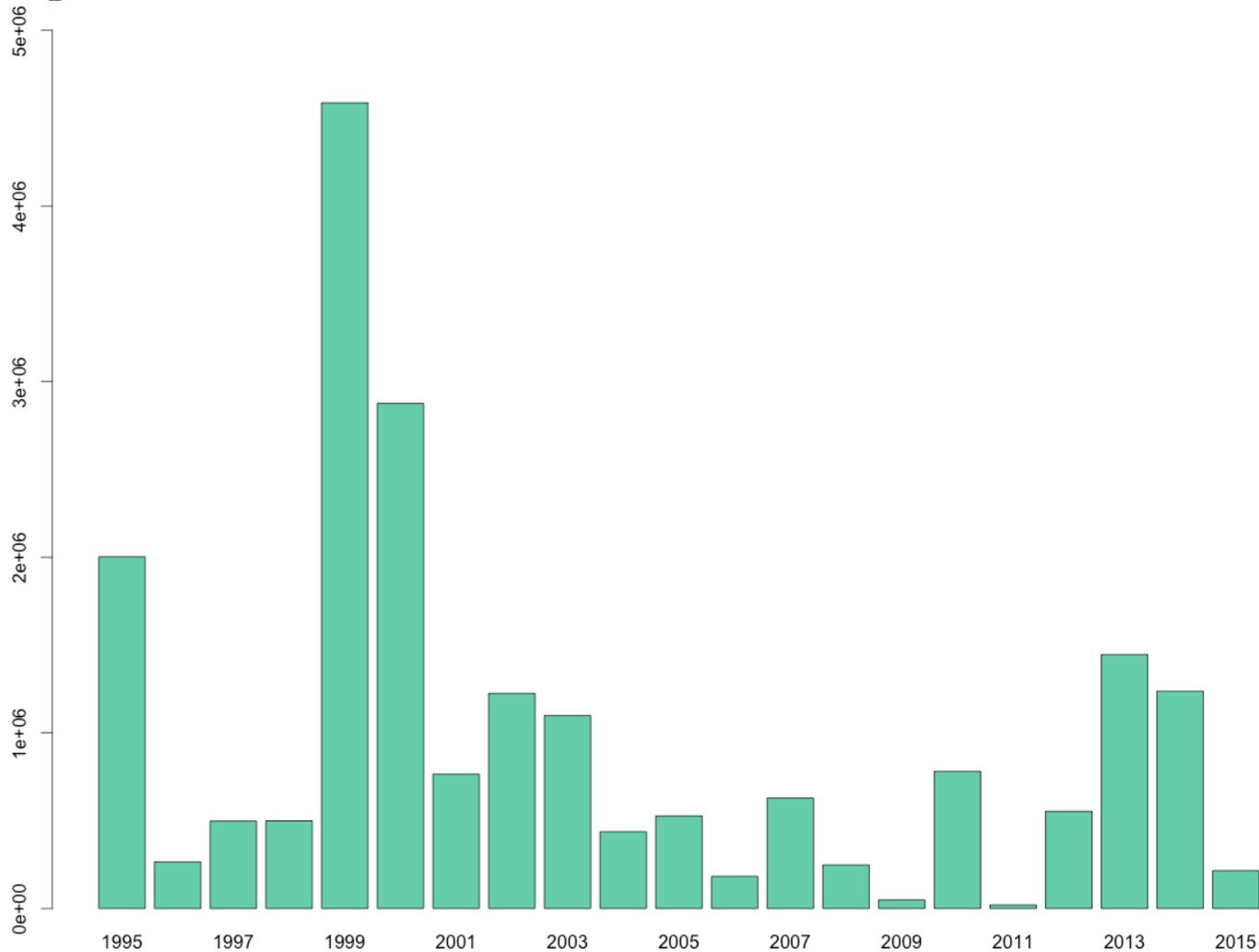
- Grid based evaluations
- complexity of extreme events not really captured
- Gridded observations not anymore available at the current resolution of regional climate models

# Impacts I



Total damages (10<sup>3</sup> \$) caused by extremes events (floods, drought, extreme temp, storms) in Europe. Data from: EM-DAT, The CRED/OFDA International Disaster Database 2016.

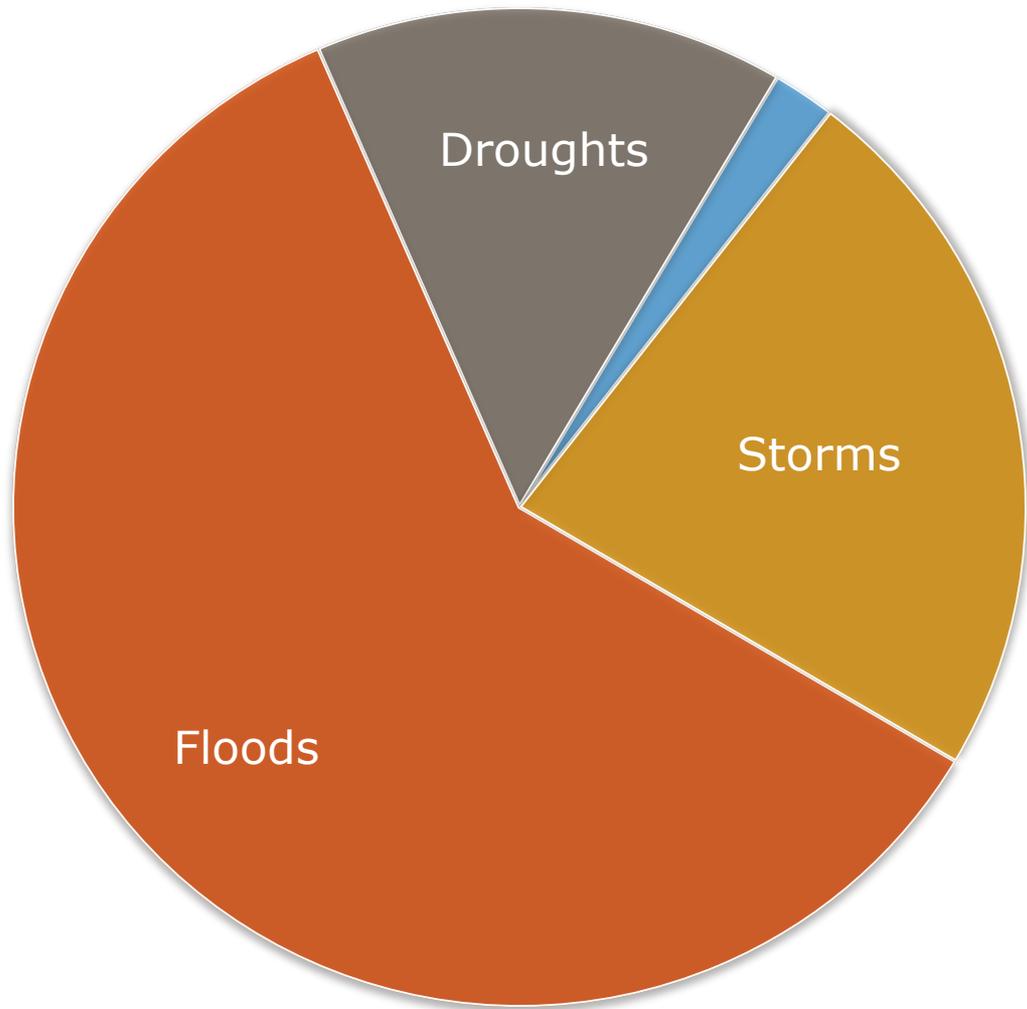
# Impacts I



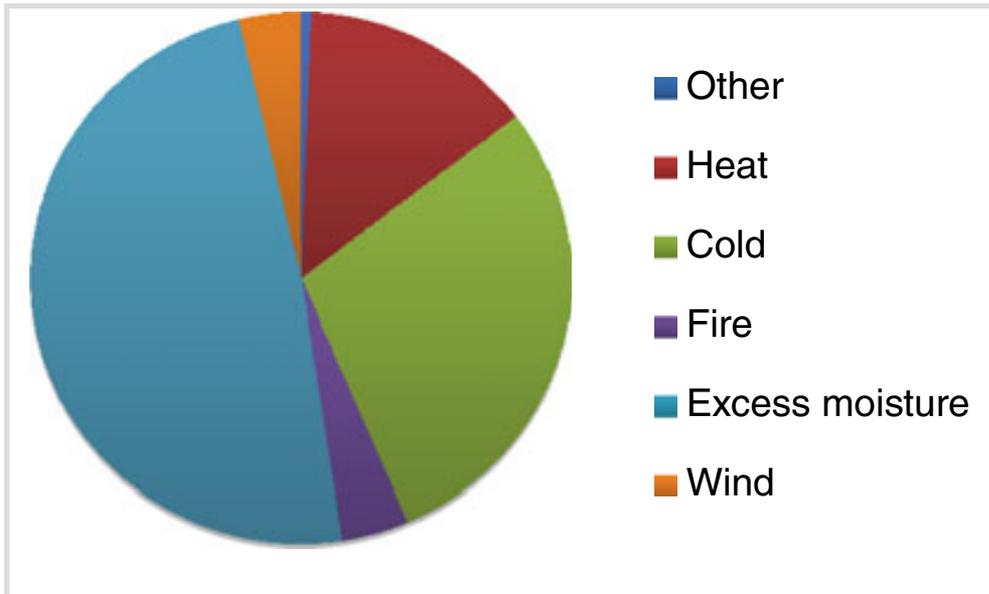
*Total number of people affected by extremes events (floods, drought, extreme temp, storms) in Europe. Data from: EM-DAT, The CRED/OFDA International Disaster Database 2016.*

# Impacts II

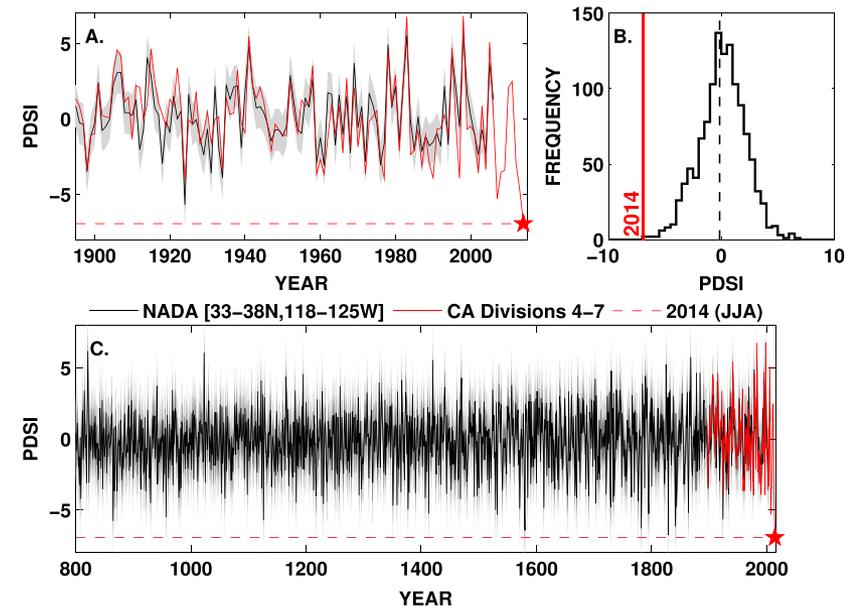
*2003-2013, Developing Countries. Average percentage share of damage and loss to crops by type of hazard. Adapted from FAO, 2015.*



# Impacts II

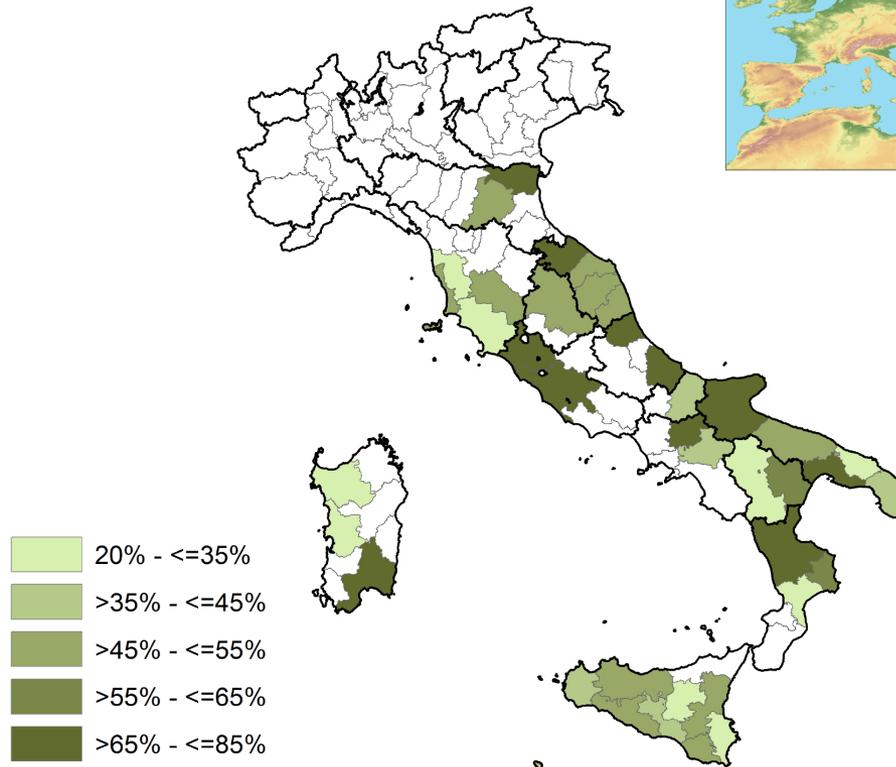


*Estimated total losses from disasters attributable to different extremes (1993-2007) - California agriculture. Source: Lobell et al., 2011*



*The 2012-2015 California drought. 2014 PDSI value w.r.t. the historical and reconstructed values. Source: Griffin and Anchukaitis, 2014.*

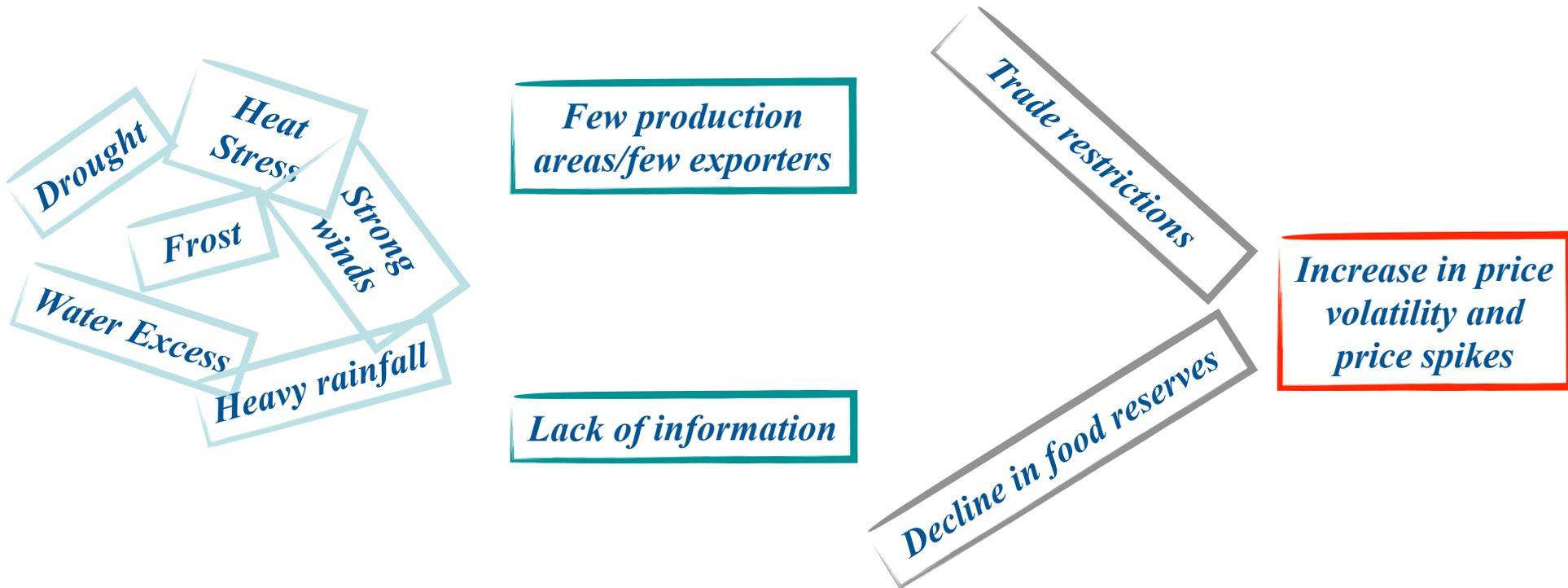
# Impacts II



*Number of concurrent early heat waves and significant negative yield anomalies of durum wheat in the period 1995–2013 (% w.r.t. the total number of year with significant negative yield anomalies). Source: Fontana et al. 2015, NHESS 15*

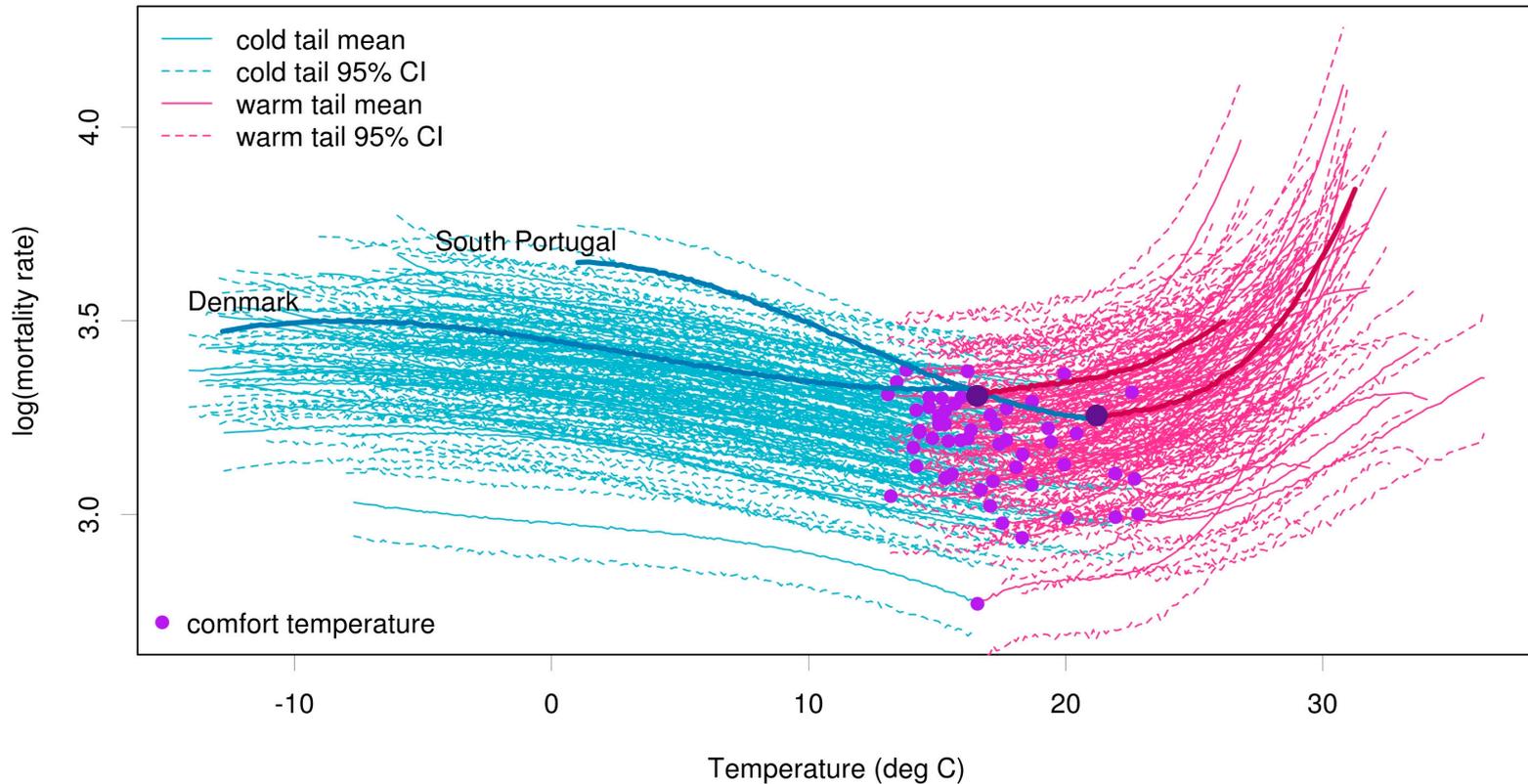
# Impacts II

cascade of events



Adapted from von Braun and Tadesse, 2012

# Impacts III



*Estimated mortality and comfort zone in 54 European regions, 1998-2003.  
Source: Lowe, 2015*

# Impacts

- Interaction of different extremes as well as occurrence of favourable/triggering conditions
- non-climatic factors
- many variables are needed
- Bias in model outputs

# Open issues, new challenges,...

- Modelling multivariate extremes having different spatio-temporal scales
- Understanding of past and current changes in extremes still limited
- Process/event oriented evaluation of models
- lack of high resolution gridded observations
- Gap between impact community and climate community

# Thank you!

*The views here expressed are purely those of the author and may not in any circumstances be regarded as stating an official position of the European Commission.*



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