

Regional CO₂ inversion through ensemble-based simultaneous state and parameter estimation

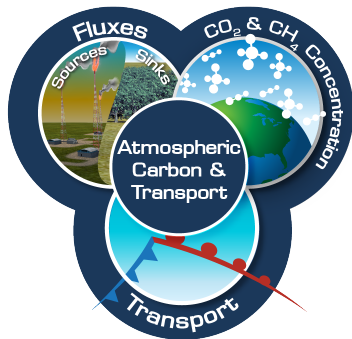
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Chalmers University of Technology

This project has received funding from the European Union's Horizon 2020 research and innovation programme under Grant Agreement No. 958927, the Swedish National Space Agency (2021-00149) and Biodiversity and Ecosystem services in a Changing Climate (BECC)

Background



Atmospheric Carbon and
Transport (ACT)–America

@PennState

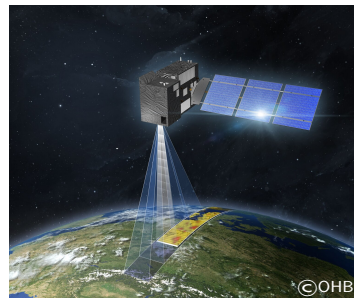
Funded by NASA



CO₂ Human Emissions (CHE)
Copernicus CO₂ (CoCO₂)

@LundUniversity

Funded by EU H2020



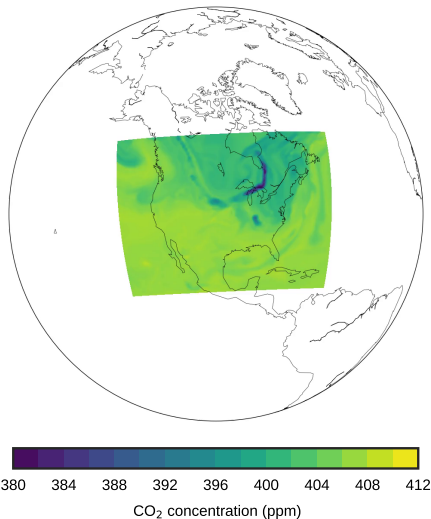
Monitoring anthropogenic CO₂
emissions from space
AVENGERS

@Chalmers

Funded by the Swedish National
Space Agency and EU

Modeling system

Development of a new regional CO₂ data assimilation system: TRACE



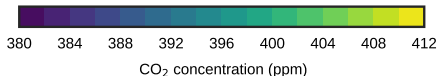
TRACE Regional Atmosphere–Carbon Ensemble system:

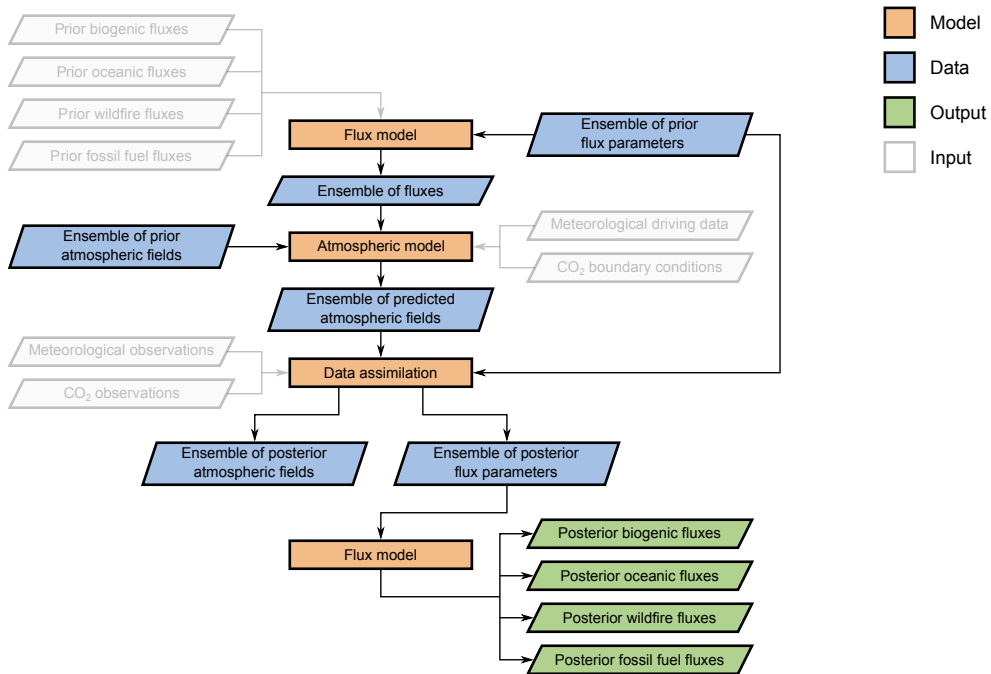
- Online atmospheric transport modeling using WRF-Chem
- Assimilation of meteorological observations to improve the modeled atmospheric transport
- Ensemble-based simultaneous state and parameter estimation (ESSPE) approach

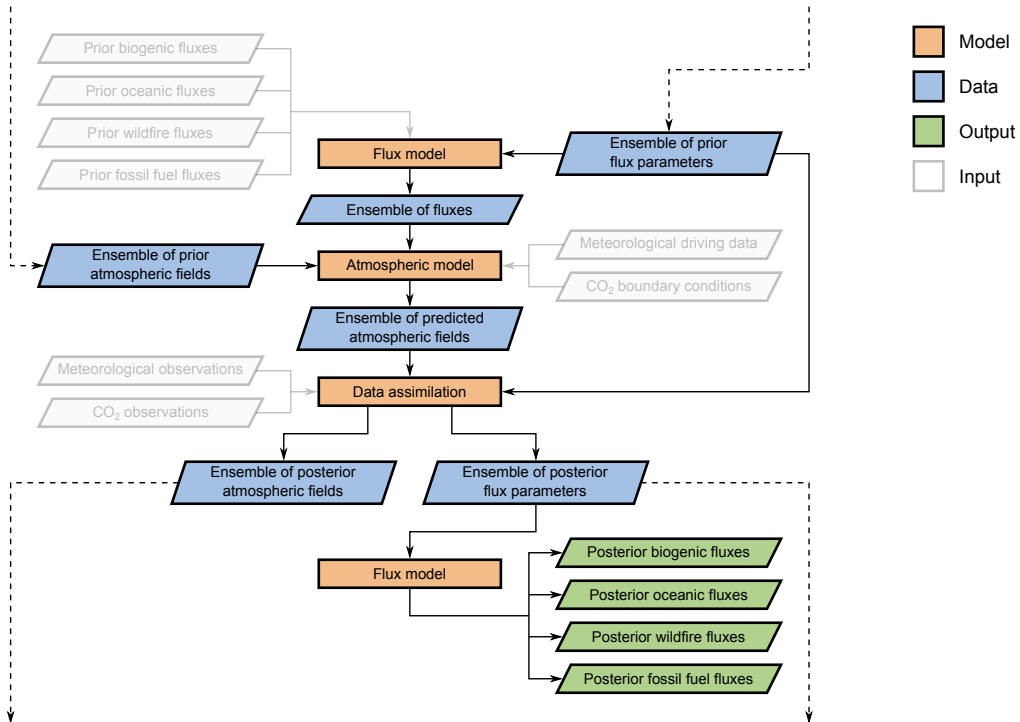
Development of a new regional CO₂ data assimilation system: TRACE

TRACE Regional Atmosphere–Carbon Ensemble system:

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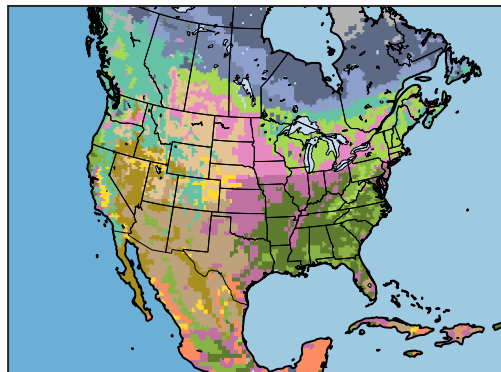
Flux model

The total surface CO₂ fluxes F are given by:

$$F(x, y, t) = s_{\text{bio}}(x, y, t) \cdot F_{\text{bio}}(x, y, t) + s_{\text{ocn}}(x, y, t) \cdot F_{\text{ocn}}(x, y, t) + s_{\text{ff}}(x, y, t) \cdot F_{\text{ff}}(x, y, t) + s_{\text{fire}}(x, y, t) \cdot F_{\text{fire}}(x, y, t)$$

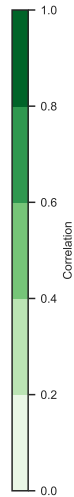
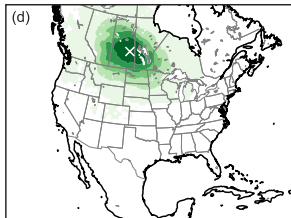
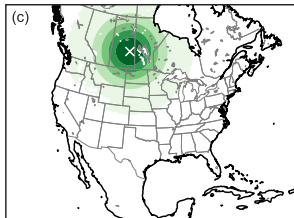
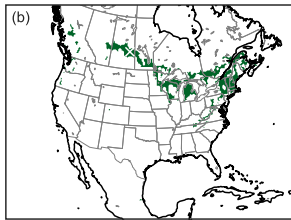
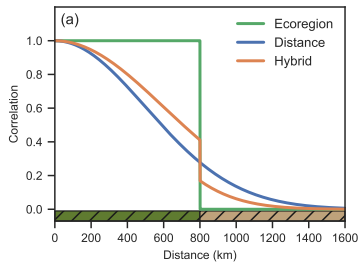
s_x are scaling factors for prior fluxes (F_x)

(Here we used prior fluxes from CT2019B)



Ecoregions based on Olsen (1985) classification

Flux parameter errors

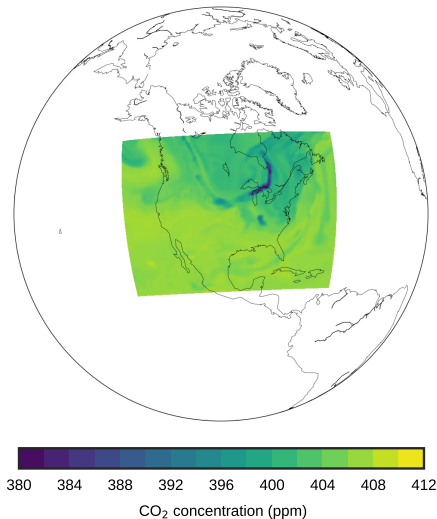


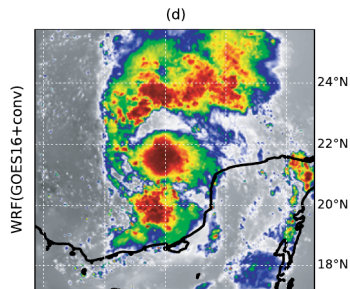
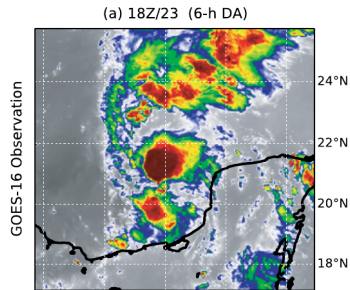
Different specifications for flux parameter error correlations:

- **Ecoregion**-specific parameters
- **Distance**-based decay
- **Hybrid** between distance and ecoregion

Atmospheric model

- WRF-Chem 3.6.1
- Modified to allow an ensemble of tracers in a single model run
- Driven by ERA-Interim (newest version uses ERA5)
- CO₂ lateral boundary conditions from CT-NRT v2017 and CT2019B (now also possible with CAMS)
- Currently 27 km horizontal resolution and 60 vertical layers





(Zhang et al. 2019 BAMS)

- Based on the PSU WRF EnKF system
- Deterministic ensemble square root filter
- Mature system for numerical weather prediction
- For CO_2 inversions, the state vector is augmented to include CO_2 concentrations and flux parameters:

$$\mathbf{x} = \begin{bmatrix} \vdots \\ \text{CO}_2 \\ \mathbf{s}_x \end{bmatrix}$$

- Flux parameters forecast using a persistence model

Localization

Spatial localization (Gaspari-Cohn function)

Radius of influence: 5,400 km

Inflation

Relaxation to prior perturbations (Zhang et al. 2004):

$$\mathbf{x}'^a \leftarrow (1 - \alpha)\mathbf{x}'^a + \alpha\mathbf{x}'^b$$

Relaxation to initial perturbations (Chen et al. 2023):

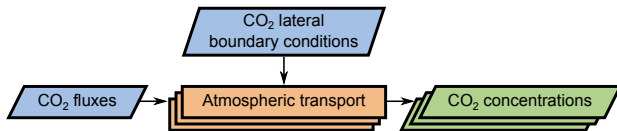
$$\mathbf{s}'^a \leftarrow \text{sgn}(\mathbf{s}'^a) \cdot \left[(1 - \beta) \cdot \text{abs}(\mathbf{s}'^a) + \beta \cdot \text{abs}(\mathbf{s}'^i) \right]$$

Here $\alpha = 0.2$ and $\beta = 0.1$

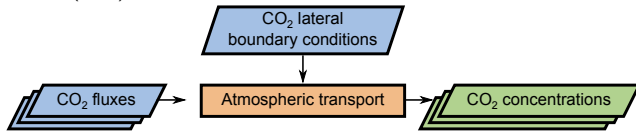
Forward simulations

Sensitivity experiments

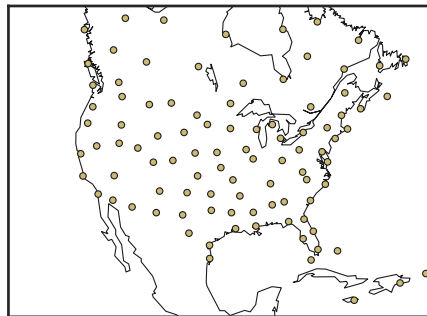
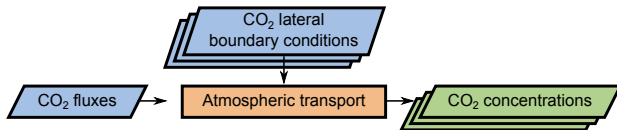
Transport (meteorological data assimilation)



Flux (80%)



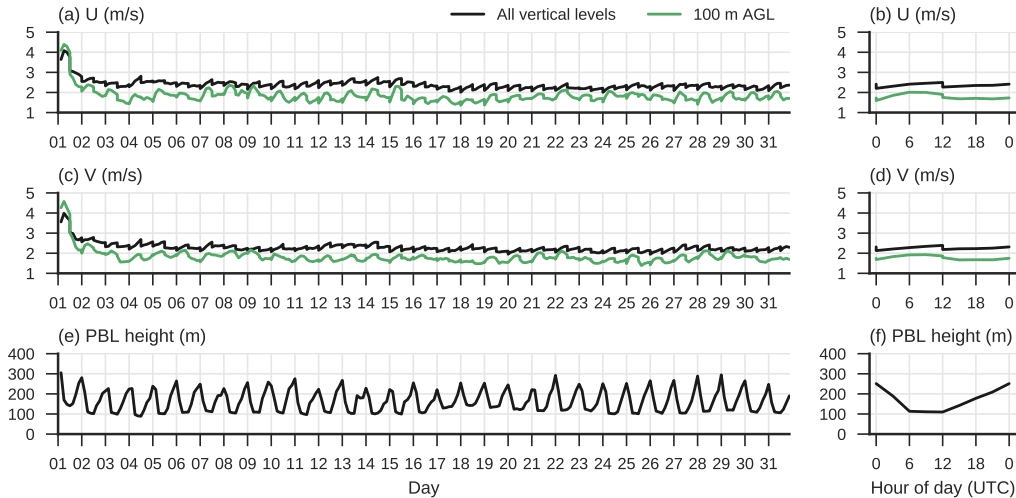
Background (4 global models)



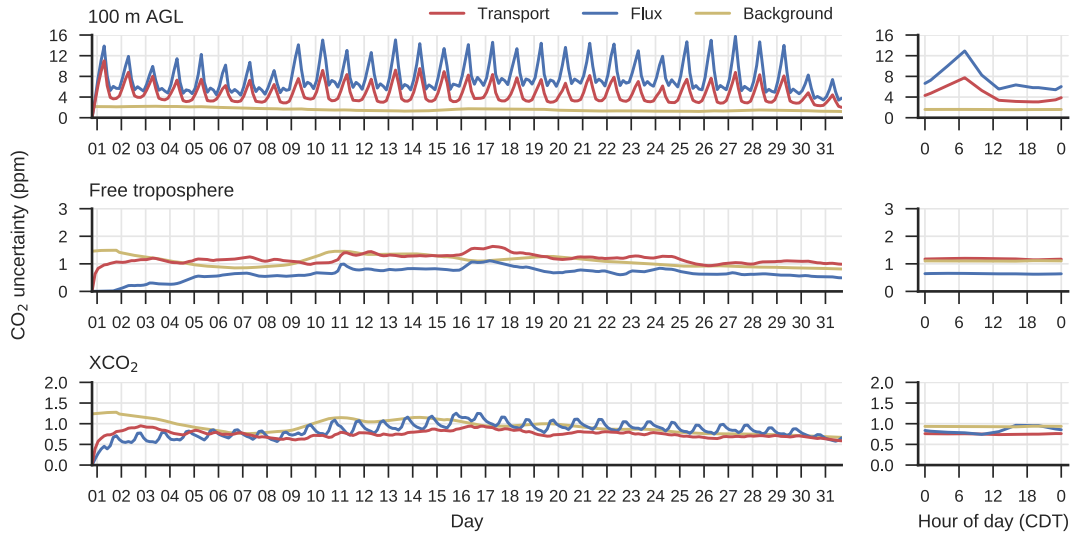
12-hourly synthetic rawinsonde observations assimilated to constrain atmospheric transport errors

(Chen et al. 2019 GRL)

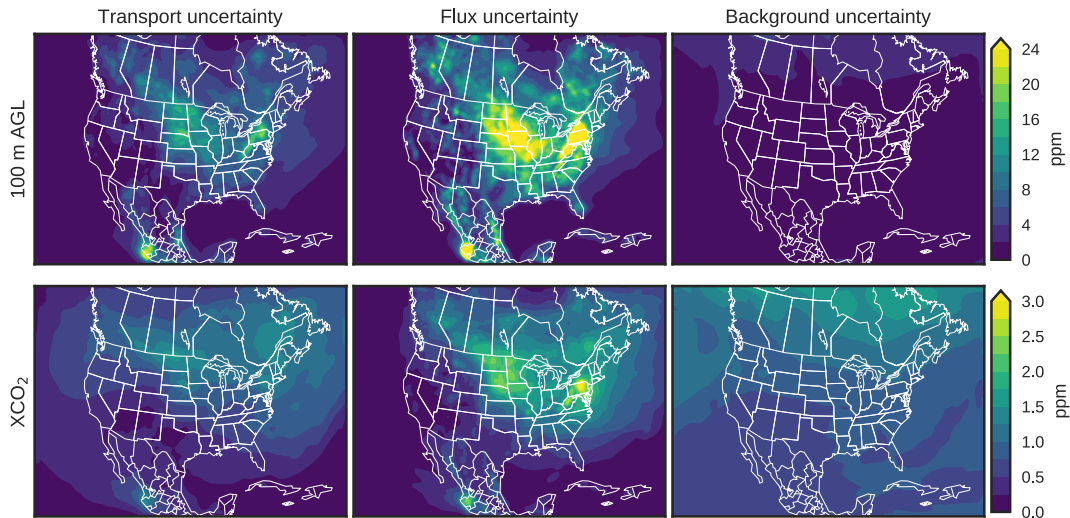
Flow-dependent atmospheric transport errors



Temporal evolution of CO₂ errors



Spatial variation of CO₂ errors



Inversions

Observing system simulation experiments

Focusing on July 2016

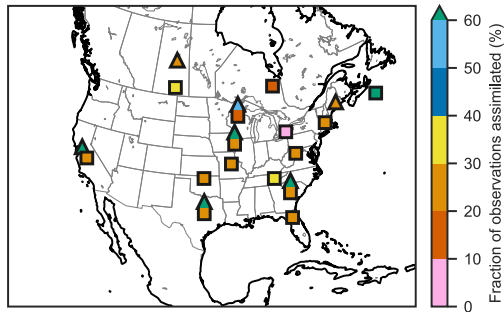
Assimilating 3-hourly synthetic CO₂ observations from ground-based network

Filter and fixed-lag smoother with a one-week window

0.8 and 0.4 uncertainty in land and ocean flux parameters, respectively

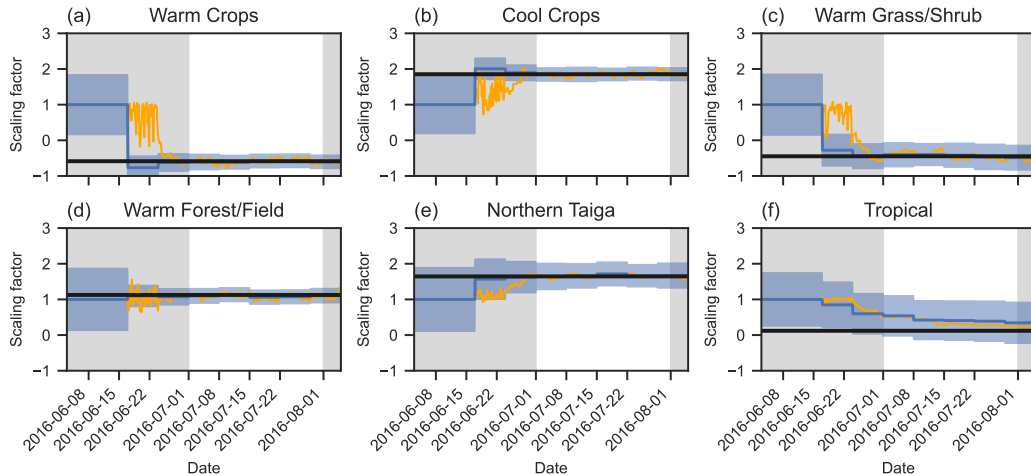
Two experiments:

- Ideal inversions with known errors
- Inversions with unknown errors



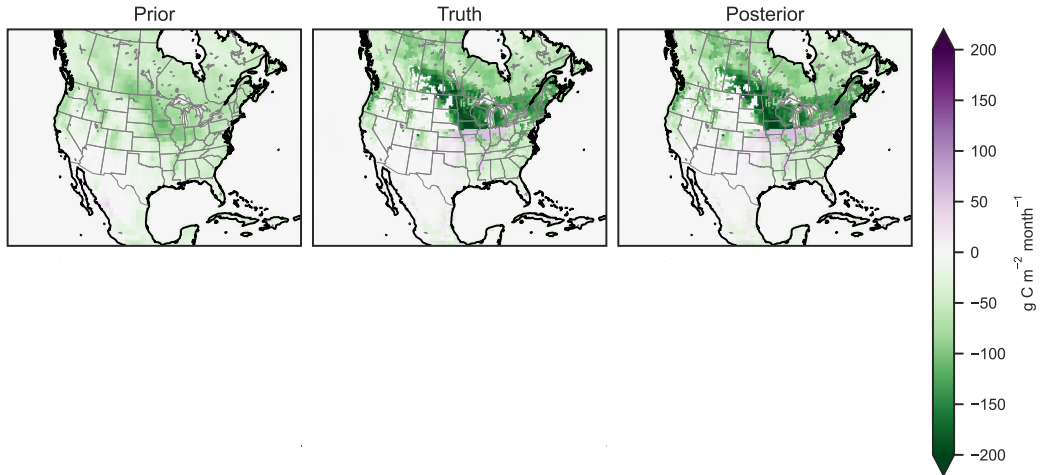
(Chen et al. 2023 JAMES)

Inversions with known errors statistics

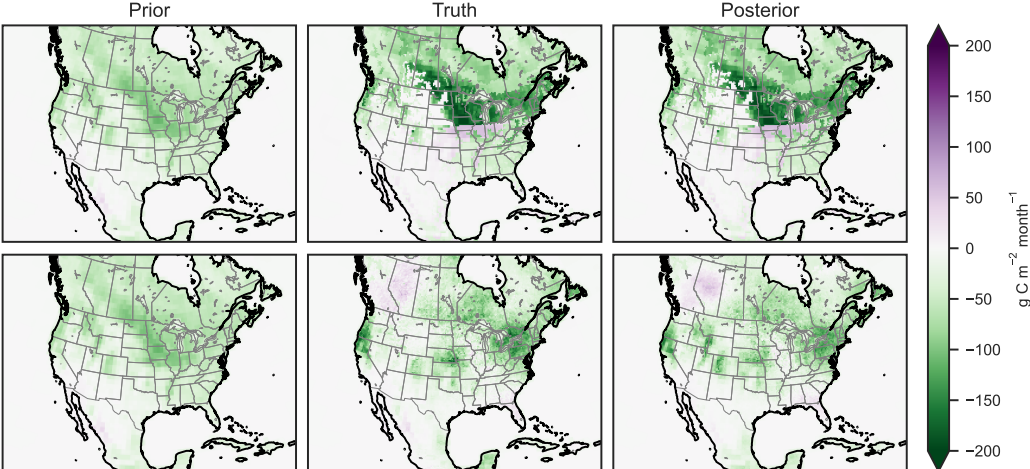


— Truth — Smoother — Filter ■ One ensemble std

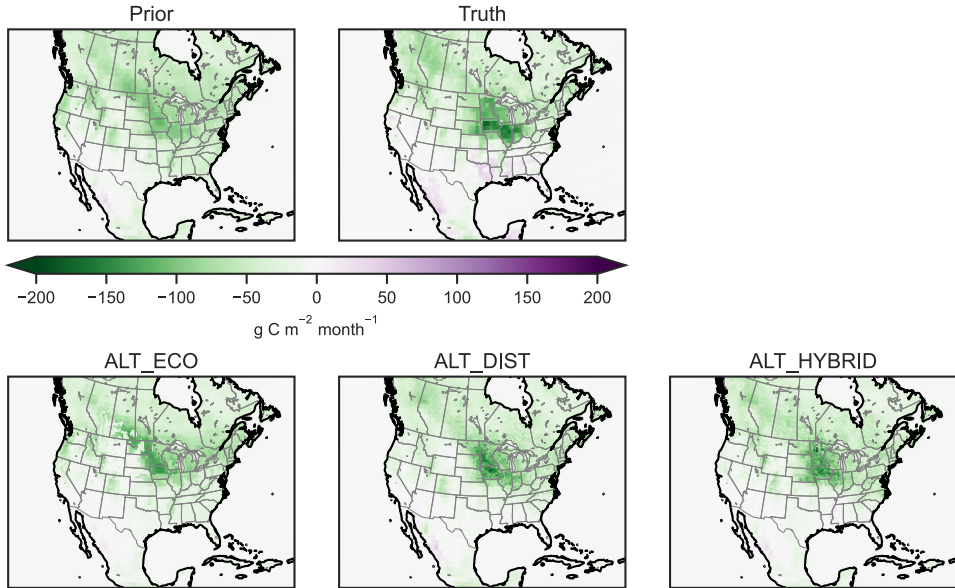
Inversions with known errors statistics



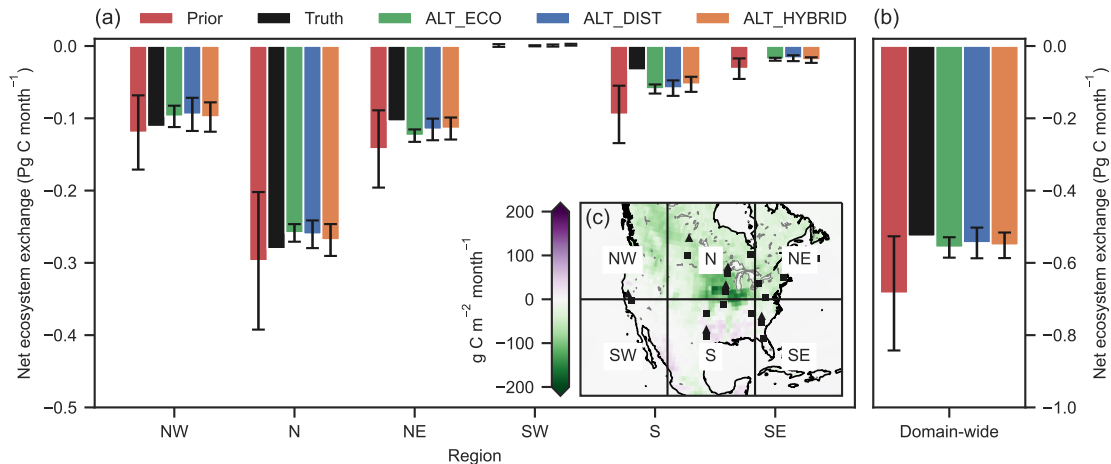
Inversions with known errors statistics



More realistic inversions with unknown errors

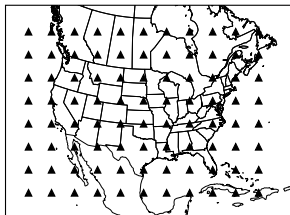


Regional fluxes and uncertainties

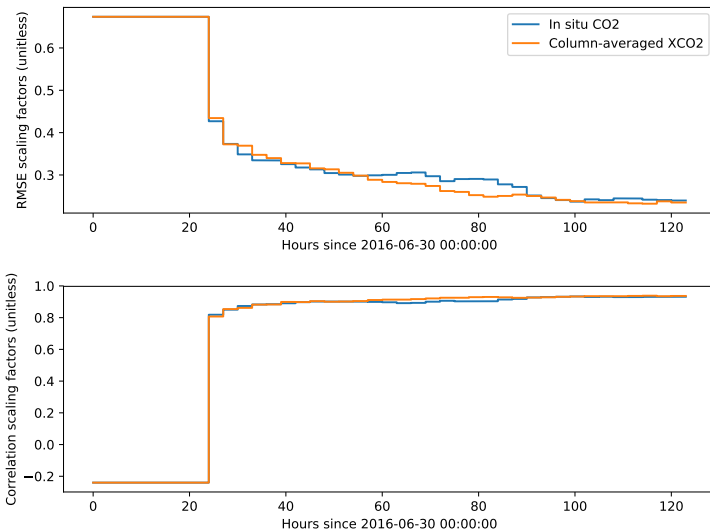


Future developments

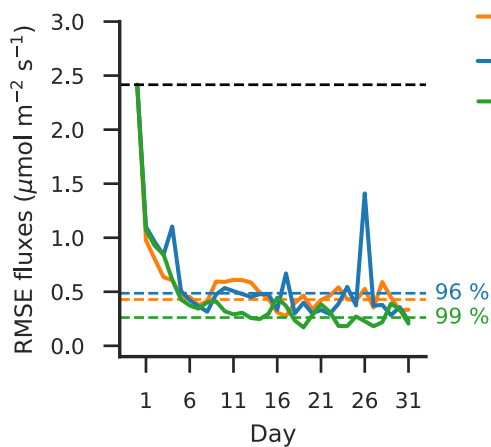
Satellite XCO₂ and fossil fuel emissions



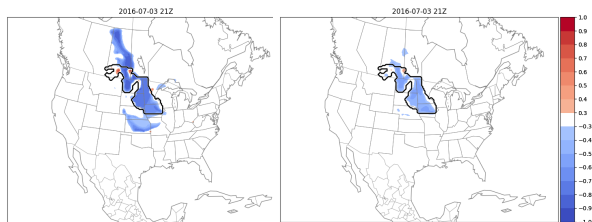
3-hourly synthetic in situ
CO₂ (100 AGL) or XCO₂
observations every 540 km



Atmospheric transport errors



- Deterministic transport with relaxation
- Deterministic transport with localization
- Ensemble of transports



Conclusions

- Ensemble-based simultaneous state and parameter estimation (ESSPE) is a promising approach to enable the assimilation of large volumes of observations
- TRACE provides a platform for developing and testing ESSPE methods for coupled atmosphere–carbon data assimilation

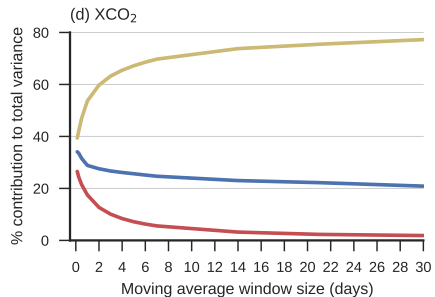
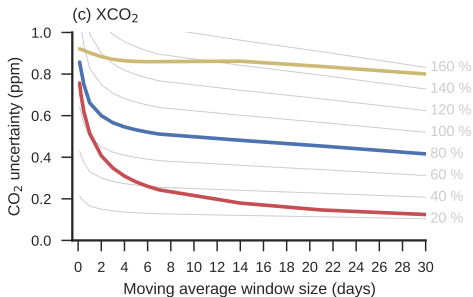
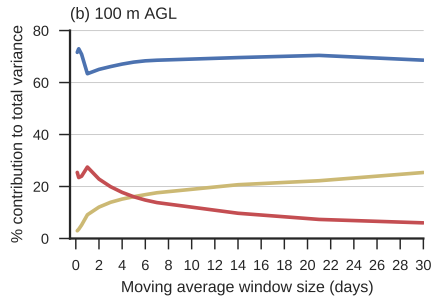
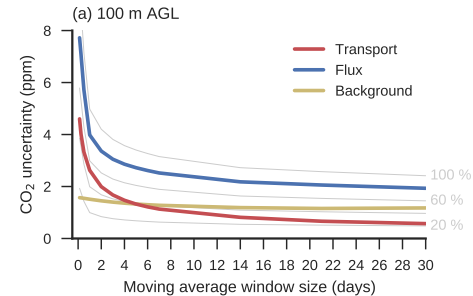
Chen, H. W., F. Zhang, T. Lauvaux, K. J. Davis, S. Feng, M. P. Butler, and R. B. Alley (2019): Characterization of regional-scale CO₂ transport uncertainties in an ensemble with flow-dependent transport errors. *Geophysical Research Letters*, **46**, 4049–4058, doi:10.1029/2018GL081341.

Chen, H. W., F. Zhang, T. Lauvaux, M. Scholze, K. J. Davis, and R. B. Alley (2023): Regional CO₂ inversion through ensemble-based simultaneous state and parameter estimation: TRACE framework and controlled experiments. *Journal of Advances in Modeling Earth Systems*, **15**, e2022MS003208, doi:10.1029/2022MS003208.

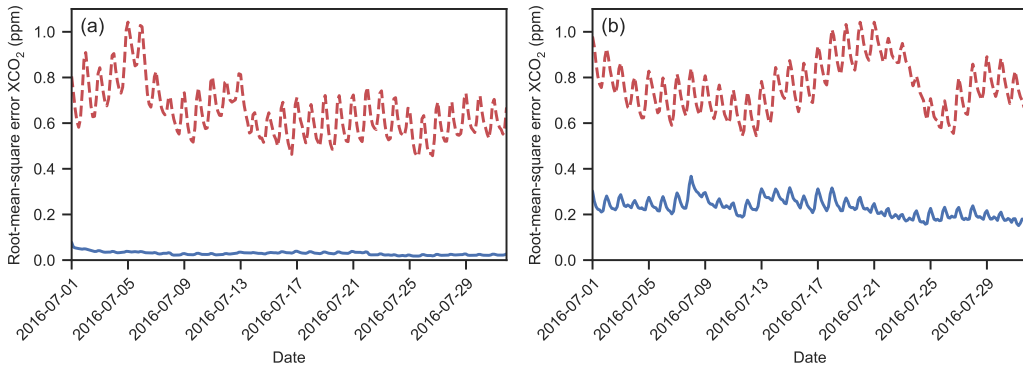
<http://hanschen.org/publications>

Extra

CO₂ errors at different temporal scales



XCO₂ in ideal inversions



Prior (red) and posterior (blue)

XCO₂ in ALT inversions

